

$g^{*\alpha}$ - CLOSED SETS IN BITOPOLOGICAL SPACES

MRS.VERONICA VIJAYAN*

Department of Mathematics, Nirmala College for Women (Autonomous),
Coimbatore-6410018, Tamil Nadu, India

A. DHANIS ARUL MARY

Department of Mathematics with Computer Application, Nirmala College for Women (Autonomous),
Coimbatore-6410018, Tamil Nadu, India

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ABSTRACT

In this paper we introduce a new class of sets $(i, j) - g^{*\alpha}$ - closed sets in bitopological spaces. Properties of these sets are investigated and we introduce new bitopological spaces $(i, j) - T_{1/2}^{*\alpha}$ and $(i, j) - {}^{*\alpha}T_{1/2}$ as applications.

Key words: (i, j) -g-closed sets, (i, j) - g^* -closed sets, $(i, j) - g^{*\alpha}$ - closed sets; $(i, j) - T_{1/2}^{*\alpha}$ spaces, and $(i, j) - {}^{*\alpha}T_{1/2}$ space.

1. INTRODUCTION

A triple (X, τ_1, τ_2) where X is non-empty set and τ_1 and τ_2 are topologies on X is called a bitopological space and Kelly [10] initiated the study of such spaces. In 1985, Fukutake introduced the concepts of g -closed sets [8] in bitopological spaces. Recently Veera Kumar introduced and studied the concepts of g^* -closed set [19] and g^* -continuity in topological spaces.

The purpose of this paper is to introduce the new class of sets, namely $g^{*\alpha}$ - closed sets. Applying these sets, the author introduced the new class of spaces, namely $(i, j) - T_{1/2}^{*\alpha}$ spaces, $(i, j) - {}^{*\alpha}T_{1/2}$ spaces for bitopological spaces and investigate some of their properties. In this paper we study the relationship of $g^{*\alpha}$ - closed sets with the class of closed sets namely (i, j) - g^* -closed [17], (i, j) -gs-closed [5], (i, j) - α g-closed [14], (i, j) -gsp-closed [5], (i, j) -rg-closed set [16], (i, j) -sg-closed [6], and (i, j) -gpr-closed sets. Also we study the relationship of $(i, j) - T_{1/2}^{*\alpha}$, $(i, j) - {}^{*\alpha}T_{1/2}$ spaces with $(i, j) - T_{1/2}$ [7], $(i, j) - T_{1/2}^*$ [17], $(i, j) - T_b$ spaces.

2. PRELIMINARIES

If A is a subset of X with a topology τ , then the closure of A is denoted by $\tau\text{-cl}(A)$ or $\text{cl}(A)$, the interior of A is denoted by $\tau\text{-int}(A)$, or $\text{int}(A)$ and the complement of A in X is denoted by A^c .

Definitions 2.1: A subset A of a bitopological space (X, τ_1, τ_2) is called

- a generalized open (g -open) set [17] if $F \subseteq \text{int}(A)$ whenever $F \subseteq A$ and F is closed in (X, τ) .
- a α -open set [15] if $A \subseteq \text{int}(\text{cl}(\text{int}(A)))$.
- a regular closed set [16] if $A = \text{cl}(\text{int}(A))$.
- a semi-open set [12] if $A \subseteq \text{cl}(\text{int}(A))$.
- a semi-pre-open set [1] if $\text{cl}(\text{int}(\text{cl}(A))) \subseteq A$.
- a preclosed set [17] if $A = \text{int}(\text{cl}(A))$.

Definition 2.2: A subset A of a bitopological space (X, τ_1, τ_2) is called

- (i, j) - g^* -closed [17] if $\tau_j\text{-cl}(A) \subseteq U$ whenever $A \subseteq U$ and $U \in \text{GO}(X, \tau)$
- (i, j) -gs-closed [5] if $\tau_j\text{-scl}(A) \subseteq U$ whenever $A \subseteq U$ and U is open in τ_i .
- (i, j) - α g-closed [14] if $\tau_j\text{-}\alpha\text{cl}(A) \subseteq U$ whenever $A \subseteq U$ and $U \in \tau_i$.
- (i, j) -gsp-closed [5] if $\tau_j\text{-spcl}(A) \subseteq U$ whenever $A \subseteq U$ and U is open in τ_i .
- (i, j) -rg-closed set [16] if $\tau_j\text{-cl}(A) \subseteq U$ whenever $A \subseteq U$ is and U is regular open in τ_i .
- (i, j) -sg-closed [7] if $\tau_j\text{-scl}(A) \subseteq U$ whenever $A \subseteq U$ and U is semi open in τ_i .
- (i, j) -gpr-closed [9] if $\tau_j\text{-pcl}(A) \subseteq U$ whenever $A \subseteq U$ and U is regular open in τ_i .

Corresponding author: MRS.VERONICA VIJAYAN*

Department of Mathematics, Nirmala College for Women (Autonomous), Coimbatore-6410018, Tamil Nadu, India

The family of all (i, j) - g -closed (resp (i, j) -gsp-closed, (i, j) -gp-closed, (i, j) -gpr-closed, (i, j) - α gr-closed, (i, j) - α g-closed, (i, j) -gs-closed) subsets of a bitopological space (X, τ_1, τ_2) is denoted by $D(i, j)$.

Definition 2.3: (i) A bitopological space (X, τ_1, τ_2) is said to be an $(i, j) - T_{1/2}^*$ space if every (i, j) - g^* -closed set is τ_j -closed.

(ii) A bitopological space (X, τ_1, τ_2) is said to be an (i, j) - T_b space if every (i, j) -gs-closed set is τ_j -closed.

3. $(i, j) - g^{*\alpha}$ -CLOSED SETS

In this section we introduce the concept of $(i, j) - g^{*\alpha}$ -closed sets in bitopological spaces.

Definition 3.1: A subset A of a bitopological space (X, τ_1, τ_2) is said to be an $(i, j) - g^{*\alpha}$ -closed set if $\tau_j - \alpha cl(A) \subseteq U$ whenever $A \subseteq U$ and $U \in GO(X, \tau_i)$.

We denote the family of all $(i, j) - g^{*\alpha}$ -closed sets in (X, τ_1, τ_2) by $D^{*\alpha}(i, j)$.

Remark 3.2: By setting $\tau_1 = \tau_2$, in Definition 3.1, a $(i, j) - g^{*\alpha}$ -closed set is a g^* -closed set.

If A is (i) τ_j -closed, (ii) τ_j - α -closed, (iii) $(i, j) - g^*$ -closed subset of (X, τ_1, τ_2) , then A is $(i, j) - g^{*\alpha}$ -closed.

The following examples show that the reverse implications of the above proposition are not true.

Example 3.4: Let $X = \{a, b, c\}$, $\tau_1 = \{\phi, \{a\}, X\}$, $\tau_2 = \{\phi, \{a\}, \{a, b\}, X\}$. Then the subset $A = \{b\}$ is $(1, 2) - g^{*\alpha}$ -closed but not τ_2 -closed in (X, τ_1, τ_2) .

Example 3.5: Let $X = \{a, b, c\}$, $\tau_1 = \{\phi, \{a\}, \{b\}, \{a, b\}, X\}$, $\tau_2 = \{\phi, \{a\}, X\}$. Then the subset $\{a, c\}$ is $g^{*\alpha}$ -closed but not τ_2 - α -closed.

Example 3.6: let $X = \{a, b, c\}$, $\tau_1 = \{\phi, \{a\}, X\}$; $\tau_2 = \{\phi, \{a\}, \{a, b\}, X\}$. The subset $\{b\}$ is $(1, 2) - g^{*\alpha}$ -closed but not $(1, 2)$ - g^* -closed.

Proposition 3.7: In a bitopological space (X, τ_1, τ_2) every $(i, j) - g^{*\alpha}$ -closed set is (i) (i, j) -gs-closed, (ii) (i, j) - α g-closed, (iii) (i, j) - α gr-closed, (iv) (i, j) -gsp-closed.

The following examples support that the converse of the above theorem is not true.

Example 3.8: Let $X = \{a, b, c\}$, $\tau_1 = \{\phi, \{a\}, X\}$, $\tau_2 = \{\phi, \{a\}, \{a, b\}, X\}$. In this example, the subsets $\{a, b\}$, $\{a, c\}$ are $(1, 2) - g$ -closed but not $(1, 2) - g^{*\alpha}$ -closed.

Example 3.9: Let $X = \{a, b, c\}$, $\tau_1 = \{\phi, \{c\}, \{a, b\}, X\}$, $\tau_2 = \{\phi, \{a\}, X\}$. The subset $\{a, c\}$ is $(1, 2)$ - α g-closed but not $(1, 2) - g^{*\alpha}$ -closed.

Example 3.10: let $X = \{a, b, c\}$, $\tau_1 = \{\phi, \{a\}, X\}$; $\tau_2 = \{\phi, \{a\}, \{b, c\}, X\}$. The subsets $\{b\}$, $\{c\}$, $\{a, b\}$, $\{a, c\}$ are $(1, 2)$ - α gr-closed but not $(1, 2) - g^{*\alpha}$ -closed.

Example 3.11: let $X = \{a, b, c\}$, $\tau_1 = \{\phi, \{a\}, X\}$; $\tau_2 = \{\phi, \{a\}, \{a, b\}, X\}$. The subsets $\{a, b\}$, $\{a, c\}$ are $(1, 2)$ -gsp-closed sets but not $(1, 2) - g^{*\alpha}$ -closed.

Proposition 3.12: In a bitopological space (X, τ_1, τ_2) every $(i, j) - g^{*\alpha}$ -closed set is (i) (i, j) -gpr-closed, (ii) (i, j) -gp-closed, (iii) (i, j) -pre-semi-closed.

The following examples support that the reverse implications of the above propositions are not true.

Example 3.13: Let $X = \{a, b, c\}$, $\tau_1 = \{\phi, \{a, b\}, X\}$, $\tau_2 = \{\phi, \{c\}, X\}$. Then the subsets $\{a, c\}$, $\{b, c\}$ are $(1, 2)$ -gpr-closed but not $(1, 2) - g^{*\alpha}$ -closed.

Example 3.14: Let $X = \{a, b, c\}$, $\tau_1 = \{\phi, \{a, b\}, X\}$, $\tau_2 = \{\phi, \{b\}, \{a, c\}, X\}$. Then the subsets $\{a\}$, $\{c\}$, $\{a, b\}$, $\{b, c\}$ are $(1, 2)$ -gp-closed but not $(1, 2) - g^{*\alpha}$ -closed.

Example 3.15: Let $X = \{a, b, c\}$, $\tau_1 = \{\phi, \{a, b\}, X\}$, $\tau_2 = \{\phi, \{b\}, \{a, c\}, X\}$. Then the subsets $\{a\}$, $\{c\}$, $\{a, b\}$, $\{b, c\}$ are $(1, 2)$ -pre semi-closed but not $(1, 2) - g^{*\alpha}$ -closed.

Remark 3.16: The following examples show that (i, j) - g - closed sets and (i, j) - $g^{*\alpha}$ - closed sets are independent.

Example 3.17: Let $X = \{a, b, c\}$, $\tau_1 = \{\emptyset, \{a\}, X\}$, $\tau_2 = \{\emptyset, \{a\}, \{a, b\}, X\}$. Then the subsets $A = \{a, b\}$, $\{a, c\}$ are $(1, 2)$ -g-closed but not $(1, 2)$ - $g^{*\alpha}$ -closed.

Example 3.18: Let $X = \{a, b, c\}$, $\tau_1 = \{\emptyset, \{a\}, \{b\}, \{a, b\}, X\}$, $\tau_2 = \{\emptyset, \{a\}, X\}$. Then the subset $B = \{b\}$ is $(1, 2) - g^{\alpha\alpha}$ -closed set but not $(1, 2)$ -g-closed set.

Remark 3.19: The following examples show that $(i, j) - g^{*\alpha}$ - closed sets and (i, j) - rg- closed sets are independent.

Example 3.20: Let $X = \{a, b, c\}$, $\tau_1 = \{\emptyset, \{c\}, \{a, b\}, X\}$, $\tau_2 = \{\emptyset, \{a\}, X\}$. Then the subsets $A = \{b\}, \{c\}$ are $(1, 2)$ - $q^{*\alpha}$ -closed sets but not $(1, 2)$ -rg-closed sets.

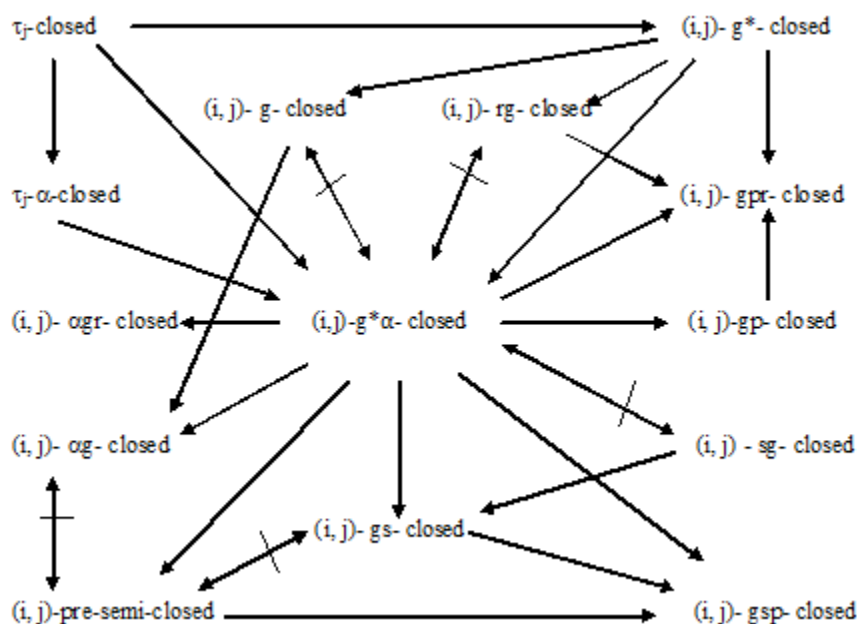
In the same example 3.20, the subset $B = \{a, c\}$ is a $(1, 2)$ -rg-closed set but not a $(1, 2) - g^{*\alpha}$ -closed set.

Remark 3.21: The following examples show that (i, j) - sg- closed sets and (i, j) - $g^{*\alpha}$ - closed sets are independent.

Example 3.22: Let $X = \{a, b, c\}$, $\tau_1 = \{\emptyset, \{a, b\}, X\}$, $\tau_2 = \{\emptyset, \{b\}, \{a, c\}, X\}$. Then the subsets $A = \{c\}$, $\{b, c\}$ are $(1, 2)$ -sg-closed but not $(1, 2) - g^{*\alpha}$ -closed.

Example 3.23: Let $X = \{a, b, c\}$, $\tau_1 = \{\emptyset, \{a\}, X\}$, $\tau_2 = \{\emptyset, \{a\}, \{b, c\}, X\}$. Then the subset $B = \{a\}$ is $(1, 2) - g^{*\alpha}$ -closed set but not a $(1, 2)$ -sg-closed set.

All the above results can be represented by the following diagram.



Where $A \rightarrow B$ (resp. $A \nleftrightarrow B$) represents A implies B but not conversely (resp. A and B are independent)

Proposition 3. 24: If $A, B \in D^{*\alpha}(i, j)$, then $A \cup B \in D^{*\alpha}(i, j)$.

Remark 3.25: $D^{*\alpha}(1, 2)$ is generally not equal to $D^{*\alpha}(2, 1)$. This is proved by an example below.

Example 3.26: Let $X = \{a, b, c\}$, $\tau_1 = \{\emptyset, \{a\}, \{b\}, \{a, b\}, X\}$, $\tau_2 = \{\emptyset, \{a\}, X\}$. Then the subset $\{b\}$ is in $D^{*\alpha}(1, 2)$ but not in $D^{*\alpha}(2, 1)$.

Proposition 3.27: If $\tau_1 \subset \tau_2$, then $D^{*\alpha}(2, 1) \subset D^{*\alpha}(1, 2)$.

The converse of the above proposition is not true as seen from the following example.

Example 3.28: Let $X = \{a, b, c\}$, $\tau_1 = \{\emptyset, \{a\}, \{b\}, \{a, b\}, X\}$, $\tau_2 = \{\emptyset, \{a\}, X\}$. Then $D^{*\alpha}(2, 1) \subseteq D^{*\alpha}(1, 2)$ but the subsets $\{b\}$, $\{a, b\}$ of τ_1 not contained in τ_2 .

Proposition 3.29: If A is (i, j) - $g^{*\alpha}$ -closed set, then $\tau_j - \alpha cl(A) - A$ contains no non-empty $\tau_i - g$ -closed set.

Proof: Let A be (i, j) - $g^{*\alpha}$ -closed set and F be a τ_j - g -closed set such that $F \subseteq \tau_j - \alpha cl(A) - A$ then $F^c \supset A$, And F^c is g -open. We have $\tau_j - \alpha cl(A) \subseteq F^c$. Thus $F \subseteq \tau_j - \alpha cl(A) \cap (\tau_j - \alpha cl(A))^c = \phi$

Corollary 3.30: If A is (i, j) - $g^{*\alpha}$ -closed in (X, τ_1, τ_2) , then A is τ_j - α -closed if and only if $\tau_j - \alpha cl(A) - A$ is τ_i - g -closed.

Proof: Necessity: If A is τ_j - α -closed then, $\tau_j - \alpha cl(A) = A$. i.e., $\tau_j - \alpha cl(A) - A = \phi$ and hence $\tau_j - \alpha cl(A) - A$ is τ_i - g -closed.

Sufficiency: Suppose $\tau_j - \alpha cl(A) - A = F \neq \phi$, Then by the proposition 3.29, F contains a g -closed set B . $\tau_j - \alpha cl(A) - A = \phi$, since A is $g^{*\alpha}$ -closed. Therefore A is τ_j - α -closed.

Proposition 3.31: If A is an (i, j) - $g^{*\alpha}$ -closed in (X, τ_1, τ_2) , then $\tau_i - cl(x) \cap A \neq \phi$ holds for each $x \in \tau_j - \alpha cl(A)$.

Proof: If A is (i, j) - $g^{*\alpha}$ -closed set. And let $x \in \tau_j - \alpha cl(A)$. Suppose $\tau_i - cl(x) \cap A = \phi$. Then, $A \subseteq (\tau_i - cl(x))^c = U$ where U is open in τ_i . Thus $A \subseteq U$ where U is g -open in τ_i . Then $\tau_j - \alpha cl(A) \subseteq U$, since A is (i, j) - $g^{*\alpha}$ -closed. Hence $\tau_i - cl(x) \cap A \neq \phi$.

Proposition 3.32: If A is (i, j) - $g^{*\alpha}$ -closed set of (X, τ_1, τ_2) such that $A \subseteq B \subseteq \tau_j - \alpha cl(A)$, then B is also a (i, j) - $g^{*\alpha}$ -closed set of (X, τ_i, τ_j) .

Proof: If A is (i, j) - $g^{*\alpha}$ -closed of (X, τ_1, τ_2) such that $A \subseteq B \subseteq \tau_j - \alpha cl(A)$. Let $B \subseteq U$ where U is g -open in τ_i . Since $A \subseteq B$, $A \subseteq U$ where U is g -open in τ_i . Then, $\tau_j - \alpha cl(A) \subseteq U$ since A is (i, j) - $g^{*\alpha}$ -closed. i.e., $B \subseteq \tau_j - \alpha cl(A) \subseteq U$. Hence $\tau_j - \alpha cl(B) \subseteq U$. Therefore B is (i, j) - $g^{*\alpha}$ -closed set of (X, τ_i, τ_j) .

4. (i, j) - $T_{1/2}^{*\alpha}$ and (i, j) - $^{*\alpha}T_{1/2}$ spaces

In this section, we introduce (i, j) - $T_{1/2}^{*\alpha}$ and (i, j) - $^{*\alpha}T_{1/2}$ bitopological spaces.

Definition 4.1: A bitopological space (X, τ_1, τ_2) is said to be an (i, j) - $T_{1/2}^{*\alpha}$ space if every (i, j) - $g^{*\alpha}$ -closed set is τ_j -closed.

Proposition 4.2: If (X, τ_1, τ_2) is said to be an (i, j) - $T_{1/2}^{*\alpha}$ space. Then it is an (i, j) - $T_{1/2}^*$ space but not conversely.

Example 4.3: Let $X = \{a, b, c\}$, $\tau_1 = \{\phi, \{a\}, X\}$, $\tau_2 = \{\phi, \{a\}, \{a, b\}, X\}$. Then (X, τ_1, τ_2) is $(1, 2)$ - $T_{1/2}^{*\alpha}$ space, since the subsets $\{b\}$, $\{c\}$, $\{b, c\}$ are $(1, 2)$ - $g^{*\alpha}$ -closed and τ_2 -closed, but (X, τ_1, τ_2) is not $(1, 2)$ - $T_{1/2}^{*\alpha}$, since the subset $\{b\}$ is $(1, 2)$ - $g^{*\alpha}$ -closed but not τ_2 -closed.

Proposition 4.4: Every (i, j) - T_b -space is (i, j) - $T_{1/2}^{*\alpha}$ space but not conversely.

Example 4.5: Let $X = \{a, b, c\}$, $\tau_1 = \{\phi, \{a\}, X\}$, $\tau_2 = \{\phi, \{a\}, \{b, c\}, X\}$. Then the space (X, τ_1, τ_2) is $(1, 2)$ - $T_{1/2}^{*\alpha}$ space since the subsets $\{a\}$, $\{b, c\}$ are $(1, 2)$ - $g^{*\alpha}$ -closed and τ_2 -closed but (X, τ_1, τ_2) is not $(1, 2)$ - T_b , since the subsets $\{b\}$, $\{c\}$, $\{a, b\}$, $\{a, c\}$ are $(1, 2)$ - g -closed but not τ_2 -closed.

Definition 4.12: A bitopological space (X, τ_1, τ_2) is said to be an (i, j) - $^{*\alpha}T_{1/2}$ space if every (i, j) - $g^{*\alpha}$ -closed set is (i, j) - g^* -closed.

Proposition 4.13: Every (i, j) - $T_{1/2}^{*\alpha}$ space is (i, j) - $^{*\alpha}T_{1/2}$ but not conversely.

Example 4.14: Let $X = \{a, b, c\}$, $\tau_1 = \{\phi, \{c\}, \{a, c\}, X\}$, $\tau_2 = \{\phi, \{a\}, X\}$. Then (X, τ_1, τ_2) is an $(1, 2)$ - $^{*\alpha}T_{1/2}$ space, since the subsets $\{b\}$, $\{c\}$, $\{a, b\}$, $\{b, c\}$ are $(1, 2)$ - $g^{*\alpha}$ -closed and g^* -closed but not an $(1, 2)$ - $T_{1/2}^{*\alpha}$ -space, since the subset $\{b\}$ is $(1, 2)$ - $g^{*\alpha}$ -closed but not τ_2 -closed.

Proposition 4.15: Every (i, j) - T_b -space is (i, j) - $^{*\alpha}T_{1/2}$ space but not conversely.

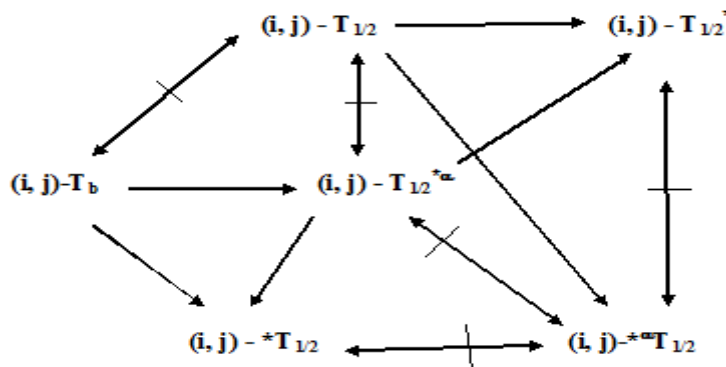
Example 4.16: Let $X = \{a, b, c\}$, $\tau_1 = \{\phi, \{c\}, \{a, c\}, X\}$, $\tau_2 = \{\phi, \{a\}, X\}$. Then (X, τ_1, τ_2) is an $(1, 2)$ - $^{*\alpha}T_{1/2}$ space, since the subsets $\{b\}$, $\{c\}$, $\{a, b\}$, $\{b, c\}$ are $(1, 2)$ - $g^{*\alpha}$ -closed and g^* -closed but not an $(1, 2)$ - T_b -space, since the subsets $\{b\}$, $\{c\}$, $\{a, b\}$ are $(1, 2)$ - g -closed and not τ_2 -closed.

Proposition 4.17: $(i, j) - T_{1/2}^{*\alpha}$ and $(i, j) - {}^{*\alpha}T_{1/2}$ are independent as seen from the following two examples.

Example 4.18: Let $X = \{a, b, c\}$, $\tau_1 = \{\emptyset, \{c\}, \{a, c\}, X\}$, $\tau_2 = \{\emptyset, \{a\}, X\}$. Then (X, τ_1, τ_2) is an $(1, 2) - {}^{*\alpha}T_{1/2}$ space since the subsets $\{b\}$, $\{c\}$, $\{a, b\}$, $\{b, c\}$ are $(1, 2) - g^{*\alpha}$ -closed and g^* -closed but not an $(1, 2) - T^*$ -space, since the subsets $\{b\}$, $\{c\}$, $\{a, b\}$ are $(1, 2) - g^*$ -closed and not τ_2 -closed.

Example 4.19: Let $X = \{a, b, c\}$, $\tau_1 = \{\emptyset, \{a\}, X\}$, $\tau_2 = \{\emptyset, \{a\}, \{a, b\}, X\}$. Then (X, τ_1, τ_2) is $(1, 2) - T^*_{1/2}$ - space since the subsets $\{c\}$, $\{b, c\}$ are $(1, 2) - g^*$ -closed and τ_2 -closed but not an $(1, 2) - {}^{*\alpha}T_{1/2}$ space, since the subset $\{b\}$ is $(1, 2) - g^{*\alpha}$ -closed and not τ_2 -closed.

All the above results can be represented by the following diagram.



Where $A \rightarrow B$ (resp. $A \not\rightarrow B$) represents A implies B but not conversely (resp. A and B are independent)

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