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# SOME NEW RESULTS ON 1-NEAR MEAN CORDIAL LABELING OF GRAPHS 

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#### Abstract

Let $G=(V, E)$ be a simple graph. A surjective function $f: V(G) \rightarrow\{0,1,2\}$ is said to be a 1-Near Mean Cordial Labeling if for each edge $u v$, the induced map $$
f^{*}(u v)=\left\{\begin{array}{ccc} 0 & \text { if } & \frac{f(u)+f(v)}{2} \text { is an integer } \\ 1 & \text { otherwise } \end{array}\right.
$$

Satisfies the condition $\left|e_{f}(0)-e_{f}(1)\right| \leq 1$ where $e_{f}(0)$ is the number of edges with 0 label and $e_{f}(1)$ is the number of edges with 1 label.

G is said to be a 1-Near Mean Cordial Graph if it has a 1- Near Mean Cordial Labeling. In this paper ,we proved that wheel, complete bipartite, helm, closed helm, flower, sunflower, and $S\left(K_{1, n}\right)$ are 1- Near Mean Cordial Graphs.


Keywords: 1-Near Mean Cordial Labeling, 1-Near Mean Cordial Graph.

## 1. INTRODUCTION

All graphs considered here are finite, simple and undirected. Gallian [2] has given a dynamic survey of labeling. For graph theoretic terminologies and notations we follow Harary [3]. The concept of mean cordial labeling was introduced by Raja Ponraj, Muthirulan Sivakumar and Murugesan Sundaram in the year 2012 [1,4,5,7]. Let f be a function from $V(G)$ to $\{0,1,2\}$. For each edge uv of $G$, assign the label $\left\lceil\frac{\mathrm{f}(\mathrm{u})+\mathrm{f}(\mathrm{v})}{2}\right\rceil$. f is called a mean cordial labeling of G if $\left|v_{f}(0)-v_{f}(1)\right| \leq 1$ and $\left|e_{f}(0)-e_{f}(1)\right| \leq 1, i, j \in\{0,1,2\}$ where $v_{f}(x)$ and $e_{f}(x)$ denote the number of vertices and edges labeled with $x(x=0,1,2)$ respectively. A graph with a mean cordial labeling is called Mean Graph. K.Palani, J.Rejila Jeya Surya [6] introduced a new concept called 1-Near Mean Cordial Labeling and investigated some standard graphs.

## 2. PRELIMINARIES

We define the concept of 1-Near Mean Cordial Labeling as follows,
Let $\mathrm{G}=(\mathrm{V}, \mathrm{E})$ be a simple graph. A surjective function $\mathrm{f}: \mathrm{V}(\mathrm{G}) \rightarrow\{0,1,2\}$ said to be a 1-Near Mean Cordial Labeling if for each edge uv, the induced map

$$
\mathrm{f}^{*}(\mathrm{uv})=\left\{\begin{array}{lrr}
0 & \text { if } & \frac{\mathrm{f}(\mathrm{u})+\mathrm{f}(\mathrm{v})}{2} \text { is an integer } \\
1 & \text { otherwise }
\end{array}\right.
$$

Satisfies the condition $\left|e_{f}(0)-e_{f}(1)\right| \leq 1$ where $e_{f}(0)$ is the number of edges with 0 label and $e_{f}(1)$ is the number of edges with 1 label.

G is said to be a 1-Near Mean Cordial Graph if it has a 1- Near Mean Cordial Labeling. we proved that wheel, complete bipartite, helm, closed helm, flower, sunflower, and $\mathrm{S}\left(\mathrm{K}_{1, \mathrm{n})}\right.$ are 1- Near Mean Cordial Graphs.

Definition 2.1: A graph $\mathrm{C}_{\mathrm{n}}+\mathrm{K}_{1}$ is called a wheel with n spokes and is denoted by $\mathrm{W}_{\mathrm{n}}$.

Definition 2.2: A graph $G$ is called a complete bipartite graph $K_{m, n}$ with bipartition $V(G)=V_{1} \cup V_{2}$ where $\mathrm{V}_{1}=\left\{\mathrm{x}_{1}, \mathrm{x}_{2}, \ldots, \mathrm{x}_{\mathrm{m}}\right\}$ and $\mathrm{V}_{2}=\left\{\mathrm{y}_{1}, \mathrm{y}_{2}, \ldots, \mathrm{y}_{\mathrm{n}}\right\}$ and all vertices in $\mathrm{V}_{1}$ are adjacent to all vertices in $\mathrm{V}_{2}$ but no vertices in $\mathrm{V}_{1}$ and $\mathrm{V}_{2}$.

Definition 2.3: The helm $H_{n}$, is the graph obtained from a wheel by attaching a pendant edge at each vertex of the n - cycle.

Definition 2.4: A closed helm $\mathrm{CH}_{\mathrm{n}}$, is a graph obtained from a helm by joining each pendent vertex to the central vertex of the helm.

Definition 2.5: A flower $\mathrm{Fl}_{\mathrm{n}}$, is the graph obtained from a helm graph by joining each pendant vertex to the central vertex of the helm graph.

Definition 2.6: The sunflower graph $v[n, s, t]$ is the resultant graph obtained from the flower graph of wheels $W_{n}$ by adding $n-1$ pendant edges to the central vertex.

Definition 2.7: For each vertex $v$ of a graph $G$ take a new vertex $v_{0}$. join $v_{0}$ to all the vertices of $G$ adjacent to $v$. The graph $S(G)$ thus obtained is called splitting graph of $G$.

## 3. MAIN RESULTS

Theorem 3.1: The wheel $W_{n}$ is a 1-Near Mean Cordial Graph.
Proof: Let $G=(V, E)$ be a simple graph.
Let $G$ be $W_{n}$.
Let $\mathrm{V}(\mathrm{G})=\left\{\mathrm{u}, \mathrm{v}_{\mathrm{i}}: 1 \leq \mathrm{i} \leq \mathrm{n}\right\}$ and $\mathrm{E}(\mathrm{G})=\left\{\left[\left(\mathrm{uv}_{\mathrm{i}}\right): 1 \leq \mathrm{i} \leq \mathrm{n}\right] \cup\left[\left(\mathrm{v}_{\mathrm{i}} \mathrm{v}_{\mathrm{i}+1}\right): 1 \leq \mathrm{i} \leq \mathrm{n}-1\right] \cup\left[\mathrm{v}_{\mathrm{n}} \mathrm{v}_{1}\right]\right\}$
Define f: $V(G) \rightarrow\{0,1,2\}$ by
$\mathrm{f}(\mathrm{u})=1$
$\mathrm{f}\left(\mathrm{v}_{\mathrm{i}}\right)=\left\{\begin{array}{ll}0 & i \equiv 1 \bmod 2 \\ 2 & i \equiv 0 \bmod 2\end{array} \quad 1 \leq \mathrm{i} \leq \mathrm{n}\right.$
The induced edge labeling are
$\mathrm{f}^{*}\left(\mathrm{uv}_{\mathrm{i}}\right)=1, \quad 1 \leq \mathrm{i} \leq \mathrm{n}$
$\mathrm{f}^{*}\left(\mathrm{v}_{\mathrm{i}} \mathrm{V}_{\mathrm{i}+1}\right)=0, \quad 1 \leq \mathrm{i} \leq \mathrm{n}-1$
$\mathrm{f}^{*}\left(\mathrm{v}_{\mathrm{n}} \mathrm{v}_{1}\right)=0$
Here, $e_{f}(0)=e_{f}(1)=n$
Hence the graph satisfies the condition $\left|\mathrm{e}_{\mathrm{f}}(0)-\mathrm{e}_{\mathrm{f}}(1)\right| \leq 1$
Therefore, the wheel $\mathrm{W}_{\mathrm{n}}$ is a 1-near mean cordial graph.
Illustration 1: The 1- near mean cordial graph of $W_{5}$ is shown in the figure 1


Figure 1: $W_{5}$

Theorem 3.2: The complete bipartite graph, $\mathrm{K}_{\mathrm{m}, \mathrm{n}}$ is a 1-Near Mean Cordial Graph.
Proof: Let $G=(V, E)$ be a simple graph.
Let $G$ be $K_{m, n}$
Let $\mathrm{V}(\mathrm{G})=\left\{\mathrm{u}_{\mathrm{i}}: 1 \leq \mathrm{i} \leq \mathrm{m}, \mathrm{v}_{\mathrm{j}}: 1 \leq \mathrm{j} \leq \mathrm{n}\right\}$ and $\mathrm{E}(\mathrm{G})=\left\{\left(\mathrm{u}_{\mathrm{i}} \mathrm{v}_{\mathrm{j}}: 1 \leq \mathrm{i} \leq \mathrm{m}, 1 \leq \mathrm{j} \leq \mathrm{n}\right\}\right.$
Define f: V (G) $\rightarrow\{0,1,2\}$ by
$\mathrm{f}\left(\mathrm{u}_{\mathrm{i}}\right)=\left\{\begin{array}{rl}0 & i \equiv 1 \bmod 4 \\ 1 & i \equiv 0,2 \bmod 4 \quad 1 \leq \mathrm{i} \leq \mathrm{m}, \\ 2 & i \equiv 3 \bmod 4\end{array}\right.$
$\mathrm{f}\left(\mathrm{v}_{\mathrm{j}}\right)=\left\{\begin{array}{ll}0 & i \equiv 0 \bmod 2 \\ 1 & i \equiv 1 \bmod 2\end{array} \quad 1 \leq \mathrm{j} \leq \mathrm{n}\right.$,
The induced edge labeling are
Case-(i): when $m$ is even and $n$ is even or odd
$\mathrm{f}^{*}\left(\mathrm{u}_{2 \mathrm{i}-1} \mathrm{v}_{\mathrm{j}}\right)=\left\{\begin{array}{ll}0 & j \equiv 0 \bmod 2 \\ 1 & j \equiv 1 \bmod 2\end{array} \quad 1 \leq \mathrm{i} \leq \frac{m}{2}, 1 \leq \mathrm{j} \leq \mathrm{n}\right.$
$\mathrm{f}^{*}\left(\mathrm{u}_{2 \mathrm{i}} \mathrm{V}_{\mathrm{j}}\right)=\left\{\begin{array}{ll}0 & j \equiv 1 \bmod 2 \\ 1 & j \equiv 0 \bmod 2\end{array} \quad 1 \leq \mathrm{i} \leq \frac{m}{2}, 1 \leq \mathrm{j} \leq \mathrm{n}\right.$
Here, $e_{f}(0)=e_{f}(1)=m n$
Case-(ii): when $m$ is odd and $n$ is even or odd
$\mathrm{f}^{*}\left(\mathrm{u}_{2 \mathrm{i}-1} \mathrm{v}_{\mathrm{j}}\right)=\left\{\begin{array}{ll}0 & j \equiv 0 \bmod 2 \\ 1 & j \equiv 1 \bmod 2\end{array} \quad 1 \leq \mathrm{i} \leq \frac{m+1}{2}, 1 \leq \mathrm{j} \leq \mathrm{n}\right.$
$\mathrm{f}^{*}\left(\mathrm{U}_{2 \mathrm{i}} \mathrm{V}_{\mathrm{j}}\right)=\left\{\begin{array}{ll}0 & j \equiv 1 \bmod 2 \\ 1 & j \equiv 0 \bmod 2\end{array} \quad 1 \leq \mathrm{i}<\frac{m+1}{2}, 1 \leq \mathrm{j} \leq \mathrm{n}\right.$
Here, $\mathrm{e}_{\mathrm{f}}(0)=\left\{\begin{array}{cc}\frac{m n-1}{2} & n \text { is odd } \\ \frac{m n}{2} & n \text { is even }\end{array}\right.$

$$
\mathrm{e}_{\mathrm{f}}(1)=\left\{\begin{array}{cc}
\frac{m n+1}{2} & n \text { is odd } \\
\frac{m n}{2} & n \text { is even }
\end{array}\right.
$$

Hence the graph satisfies the condition $\left|e_{f}(0)-e_{f}(1)\right| \leq 1$
Therefore, the complete bipartite graph, $\mathrm{K}_{\mathrm{m}, \mathrm{n}}$, is a 1-near mean cordial graph.
Illustration 2: The 1-near mean cordial graph of $\mathrm{K}_{4,3}$ and $\mathrm{K}_{3,3}$ are shown in the figure 2(a) and figure 2(b)


Figure 2(a): $K_{4,3}$


Figure 2(b): $K_{3,3}$

Theorem 3.3: The helm $H_{n}$ is a 1-Near Mean Cordial Graph.
Proof: Let $G=(V, E)$ be a simple graph.
Let $G$ be $\mathrm{H}_{\mathrm{n}}$.
Let $\mathrm{V}(\mathrm{G})=\left\{\mathrm{u}, \mathrm{v}_{\mathrm{i}}: 1 \leq \mathrm{i} \leq \mathrm{n}, \mathrm{w}_{\mathrm{i}}: 1 \leq \mathrm{i} \leq \mathrm{n}\right\}$ and
$\mathrm{E}(\mathrm{G})=\left\{\left[\left(\mathrm{uv}_{\mathrm{i}}\right),\left(\mathrm{w}_{\mathrm{i}} \mathrm{v}_{\mathrm{i}}\right): 1 \leq \mathrm{i} \leq \mathrm{n}\right] \cup\left[\left(\mathrm{v}_{\mathrm{i}} \mathrm{v}_{\mathrm{i}+1}\right): 1 \leq \mathrm{i} \leq \mathrm{n}-1\right] \cup\left[\mathrm{v}_{\mathrm{n}} \mathrm{v}_{1}\right]\right\}$
Define $\mathrm{f}: \mathrm{V}(\mathrm{G}) \rightarrow\{0,1,2\}$ by
$f(u)=1$
$\mathrm{f}\left(\mathrm{v}_{\mathrm{i}}\right)=\left\{\begin{array}{ll}0 & i \equiv 1 \bmod 2 \\ 2 & i \equiv 0 \bmod 2\end{array} \quad 1 \leq \mathrm{i} \leq \mathrm{n}\right.$
$\mathrm{f}\left(\mathrm{w}_{\mathrm{i}}\right)=\left\{\begin{array}{ll}1 & i \equiv 0 \bmod 2 \\ 2 & i \equiv 1 \bmod 2\end{array} \quad 1 \leq \mathrm{i} \leq \mathrm{n}\right.$
The induced edge labeling are
$\mathrm{f}^{*}\left(\mathrm{uv}_{\mathrm{i}}\right)=1, \quad 1 \leq \mathrm{i} \leq \mathrm{n}$
$\mathrm{f}^{*}\left(\mathrm{v}_{\mathrm{i}} \mathrm{V}_{\mathrm{i}+1}\right)=0, \quad 1 \leq \mathrm{i} \leq \mathrm{n}-1$
$\mathrm{f}^{*}\left(\mathrm{v}_{\mathrm{n}} \mathrm{v}_{1}\right)=0$
$\mathrm{f}^{*}\left(\mathrm{w}_{\mathrm{i}} \mathrm{v}_{\mathrm{i}}\right)=\left\{\begin{array}{ll}0 & i \equiv 1 \bmod 2 \\ 1 & i \equiv 0 \bmod 2\end{array} \quad 1 \leq \mathrm{i} \leq \mathrm{n}\right.$
Here, $\mathrm{e}_{\mathrm{f}}(0)=\left\{\begin{array}{cc}\frac{3 n+1}{2} & n \text { is odd } \\ \frac{3 n}{2} & n \text { is even }\end{array}\right.$

$$
\mathrm{e}_{\mathrm{f}}(1)=\left\{\begin{array}{rc}
\frac{3 n-1}{2} & n \text { is odd } \\
\frac{3 n}{2} & n \text { is even }
\end{array}\right.
$$

Hence the graph satisfies the condition $\left|e_{f}(0)-e_{f}(1)\right| \leq 1$
Therefore, the helm $\mathrm{H}_{\mathrm{n}}$ is a 1-near mean cordial graph.
Illustration 3: The 1-near mean cordial graph of $\mathrm{H}_{5}$ is shown in the figure 3


Figure 3: $\mathrm{H}_{5}$

Theorem 3.4: A closed helm $\mathrm{CH}_{\mathrm{n}}$ is a 1-Near Mean Cordial Graph.
Proof: Let $G=(V, E)$ be a simple graph.
Let G be $\mathrm{CH}_{\mathrm{n}}$.
Let $\mathrm{V}(\mathrm{G})=\left\{\mathrm{u}, \mathrm{v}_{\mathrm{i}}: 1 \leq \mathrm{i} \leq \mathrm{n}, \mathrm{w}_{\mathrm{i}}: 1 \leq \mathrm{i} \leq \mathrm{n}\right\}$ and
$E(G)=\left\{\left[\left(u v_{i}\right),\left(w_{i} v_{i}\right): 1 \leq i \leq n\right] \cup\left[\left(v_{i} v_{i+1}\right),\left(w_{i} w_{i+1}\right): 1 \leq i \leq n-1\right] \cup\left[\left(v_{n} v_{1}\right),\left(w_{n} w_{1}\right)\right]\right\}$
Define $f: V(G) \rightarrow\{0,1,2\}$ by
$f(u)=1$
$\mathrm{f}\left(\mathrm{v}_{\mathrm{i}}\right)=\left\{\begin{array}{ll}0 & i \equiv 1 \bmod 2 \\ 2 & i \equiv 0 \bmod 2\end{array} \quad 1 \leq \mathrm{i} \leq \mathrm{n}\right.$
$\mathrm{f}\left(\mathrm{w}_{\mathrm{i}}\right)=1, \quad 1 \leq \mathrm{i} \leq \mathrm{n}$
The induced edge labeling are
$\mathrm{f}^{*}\left(\mathrm{uv}_{\mathrm{i}}\right)=1, \quad 1 \leq \mathrm{i} \leq \mathrm{n}$
$\mathrm{f}^{*}\left(\mathrm{v}_{\mathrm{i}} \mathrm{W}_{\mathrm{i}}\right)=1, \quad 1 \leq \mathrm{i} \leq \mathrm{n}$
$\mathrm{f}^{*}\left(\mathrm{v}_{\mathrm{i}} \mathrm{v}_{\mathrm{i}+1}\right)=0, \quad 1 \leq \mathrm{i} \leq \mathrm{n}-1$
$\mathrm{f}^{*}\left(\mathrm{w}_{\mathrm{i}} \mathrm{W}_{\mathrm{i}+1}\right)=0, \quad 1 \leq \mathrm{i} \leq \mathrm{n}-1$
$\mathrm{f}^{*}\left(\mathrm{~V}_{\mathrm{n}} \mathrm{V}_{1}\right)=0$
$\mathrm{f}^{*}\left(\mathrm{w}_{\mathrm{n}} \mathrm{W}_{1}\right)=0$
Here, $e_{f}(0)=e_{f}(1)=2 n$
Hence the graph satisfies the condition $\left|e_{f}(0)-e_{f}(1)\right| \leq 1$
Therefore, the closed helm $\mathrm{CH}_{\mathrm{n}}$ is a 1-near mean cordial graph.
Illustration 4: The 1-near mean cordial graph of $\mathrm{CH}_{4}$ is shown in the figure 4,


Figure 4 : $\mathrm{CH}_{4}$

Theorem 3.5: A flower graph $F l_{n}$ is a 1- Near Mean Cordial Graph.
Proof: Let $G=(V, E)$ be a simple graph.
Let $G$ be $\mathrm{Fl}_{n}$.
Let $\mathrm{V}(\mathrm{G})=\left\{\mathrm{u}, \mathrm{v}_{\mathrm{i}}: 1 \leq \mathrm{i} \leq \mathrm{n}, \mathrm{w}_{\mathrm{i}}: 1 \leq \mathrm{i} \leq \mathrm{n}\right\}$ and
$\mathrm{E}(\mathrm{G})=\left\{\left[\left(\mathrm{uv}_{\mathrm{i}}\right),\left(\mathrm{uw}_{\mathrm{i}}\right),\left(\mathrm{w}_{\mathrm{i}} \mathrm{v}_{\mathrm{i}}\right): 1 \leq \mathrm{i} \leq \mathrm{n}\right] \cup\left[\left(\mathrm{v}_{\mathrm{i}} \mathrm{v}_{\mathrm{i}+1}\right): 1 \leq \mathrm{i} \leq \mathrm{n}-1\right] \cup\left(\mathrm{v}_{\mathrm{n}} \mathrm{v}_{1}\right)\right\}$

Define f:V(G) $\rightarrow\{0,1,2\}$ by
$f(u)=1$
$\mathrm{f}\left(\mathrm{v}_{\mathrm{i}}\right)=\left\{\begin{array}{ll}0 & i \equiv 1 \bmod 2 \\ 2 & i \equiv 0 \bmod 2\end{array} \quad 1 \leq \mathrm{i} \leq \mathrm{n}\right.$
$\mathrm{f}\left(\mathrm{w}_{\mathrm{i}}\right)=\left\{\begin{array}{ll}1 & i \equiv 0 \bmod 2 \\ 2 & i \equiv 1 \bmod 2\end{array} \quad 1 \leq \mathrm{i} \leq \mathrm{n}\right.$
The edge induced labeling are,
$\mathrm{f}^{*}\left(\mathrm{uv}_{\mathrm{i}}\right)=1, \quad 1 \leq \mathrm{i} \leq \mathrm{n}$
$\mathrm{f}^{*}\left(\mathrm{v}_{\mathrm{i}} \mathrm{V}_{\mathrm{i}+1}\right)=0, \quad 1 \leq \mathrm{i} \leq \mathrm{n}-1$
$\mathrm{f}^{*}\left(\mathrm{v}_{\mathrm{n}} \mathrm{V}_{1}\right)=0$,
$\mathrm{f}^{*}\left(\mathrm{uw}_{\mathrm{i}}\right)=\left\{\begin{array}{ll}0 & i \equiv 0 \bmod 2 \\ 1 & i \equiv 1 \bmod 2\end{array} \quad 1 \leq \mathrm{i} \leq \mathrm{n}\right.$
$\mathrm{f}^{*}\left(\mathrm{w}_{\mathrm{i}} \mathrm{v}_{\mathrm{i}}\right)=\left\{\begin{array}{ll}0 & i \equiv 1 \bmod 2 \\ 1 & i \equiv 0 \bmod 2\end{array} \quad 1 \leq \mathrm{i} \leq \mathrm{n}\right.$
Here, $\mathrm{e}_{\mathrm{f}}(0)=\mathrm{e}_{\mathrm{f}}(1)=2 \mathrm{n}$
Hence the graph satisfies the condition $\left|e_{f}(0)-e_{f}(1)\right| \leq 1$
Therefore, a flower graph $\mathrm{Fl}_{n}$ is a 1-near mean cordial graph.
Illustration 5: The 1-near mean cordial graph of $\mathrm{Fl}_{5}$ is shown in the figure 5,


Figure 5 : $\mathrm{Fl}_{5}$
Theorem 3.6: The sunflower graph $S_{n}$ is a 1-Near Mean Cordial Graph.
Proof: Let $G=(V, E)$ be a simple graph.
Let $G$ be $S_{n}$.
Let $\mathrm{V}(\mathrm{G})=\left\{\mathrm{u}, \mathrm{v}_{\mathrm{i}}: 1 \leq \mathrm{i} \leq \mathrm{n}, \mathrm{w}_{\mathrm{i}}: 1 \leq \mathrm{i} \leq \mathrm{n}, \mathrm{x}_{\mathrm{i}}: 1 \leq \mathrm{i} \leq \mathrm{n}\right\}$ and
$E(G)=\left\{\left[\left(u v_{i}\right),\left(u w_{i}\right),\left(u x_{i}\right),\left(w_{i} v_{i}\right): 1 \leq i \leq n\right] \cup\left[\left(v_{i} v_{i+1}\right): 1 \leq i \leq n-1\right] \cup\left(v_{n} v_{1}\right)\right\}$
Define $\mathrm{f}: \mathrm{V}(\mathrm{G}) \rightarrow\{0,1,2\}$ by
$f(u)=1$
$\mathrm{f}\left(\mathrm{v}_{\mathrm{i}}\right)=\left\{\begin{array}{ll}0 & i \equiv 1 \bmod 2 \\ 2 & i \equiv 0 \bmod 2\end{array} \quad 1 \leq \mathrm{i} \leq \mathrm{n}\right.$
$\mathrm{f}\left(\mathrm{w}_{\mathrm{i}}\right)=\left\{\begin{array}{ll}1 & i \equiv 0 \bmod 2 \\ 2 & i \equiv 1 \bmod 2\end{array} \quad 1 \leq \mathrm{i} \leq \mathrm{n}\right.$
$\mathrm{f}\left(\mathrm{x}_{\mathrm{i}}\right)=\left\{\begin{array}{ll}0 & i \equiv 0 \bmod 2 \\ 1 & i \equiv 1 \bmod 2\end{array} \quad 1 \leq \mathrm{i} \leq \mathrm{n}\right.$
The edge induced labeling are,
$\mathrm{f}^{*}\left(\mathrm{uv}_{\mathrm{i}}\right)=1, \quad 1 \leq \mathrm{i} \leq \mathrm{n}$
$\mathrm{f}^{*}\left(\mathrm{v}_{\mathrm{i}} \mathrm{V}_{\mathrm{i}+1}\right)=0, \quad 1 \leq \mathrm{i} \leq \mathrm{n}-1$
$\mathrm{f}^{*}\left(\mathrm{v}_{\mathrm{n}} \mathrm{v}_{1}\right)=0$,
$\mathrm{f}^{*}\left(\mathrm{uw}_{\mathrm{i}}\right)=\left\{\begin{array}{ll}0 & i \equiv 0 \bmod 2 \\ 1 & i \equiv 1 \bmod 2\end{array} \quad 1 \leq \mathrm{i} \leq \mathrm{n}\right.$
$\mathrm{f}^{*}\left(\mathrm{w}_{\mathrm{i}} \mathrm{v}_{\mathrm{i}}\right)=\left\{\begin{array}{ll}0 & i \equiv 1 \bmod 2 \\ 1 & i \equiv 0 \bmod 2\end{array} \quad 1 \leq \mathrm{i} \leq \mathrm{n}\right.$
$\mathrm{f} *\left(\mathrm{ux}_{\mathrm{i}}\right)=\left\{\begin{array}{ll}0 & i \equiv 1 \bmod 2 \\ 1 & i \equiv 0 \bmod 2\end{array} \quad 1 \leq \mathrm{i} \leq \mathrm{n}\right.$
Here, $\mathrm{e}_{\mathrm{f}}(0)=\left\{\begin{array}{rc}\frac{5 n+1}{2} & n \text { is odd } \\ \frac{5 n}{2} & n \text { is even }\end{array}\right.$
$e_{f}(1)=\left\{\begin{array}{cc}\frac{5 n-1}{2} & n \text { is odd } \\ \frac{5 n}{2} & n \text { is even }\end{array}\right.$
Hence the graph satisfies the condition $\left|e_{f}(0)-e_{f}(1)\right| \leq 1$
Therefore, the sunflower graph $S_{n}$ is a 1-near mean cordial graph.
Illustration 6: The 1-near mean cordial graph of $S_{4}$ is shown in the figure 6


Fiqure 6: $S_{4}$

Theorem 3.7: The splitting graph $\mathrm{S}\left(\mathrm{K}_{1, \mathrm{n}}\right)$ is a 1- Near Mean Cordial Graph
Proof: Let $G=(V, E)$ be a simple graph.
Let $G$ be $S\left(K_{1, n}\right)$.
Let $\mathrm{V}(\mathrm{G})=\left\{\mathrm{u}, \mathrm{v}, \mathrm{u}_{\mathrm{i}}: 1 \leq \mathrm{i} \leq \mathrm{n}, \mathrm{v}_{\mathrm{i}}: 1 \leq \mathrm{i} \leq \mathrm{n}\right\}$ and $\mathrm{E}(\mathrm{G})=\left\{\left(\mathrm{uu}_{\mathrm{i}}\right),\left(\mathrm{uv}_{\mathrm{i}}\right),\left(\mathrm{vu}_{\mathrm{i}}\right): 1 \leq \mathrm{i} \leq \mathrm{n}\right\}$
Define f: V (G) $\rightarrow\{0,1,2\}$ by
$f(u)=1$
$f(v)=0$
$\mathrm{f}\left(\mathrm{u}_{\mathrm{i}}\right)=\left\{\begin{array}{ll}0 & i \equiv 0 \bmod 3 \\ 1 & i \equiv 1 \bmod 3 \\ 2 & i \equiv 2 \bmod 3\end{array} \quad 1 \leq \mathrm{i} \leq \mathrm{n}\right.$
$\mathrm{f}\left(\mathrm{v}_{\mathrm{i}}\right)=\left\{\begin{array}{ll}0 & i \equiv 0 \bmod 2 \\ 1 & i \equiv 1 \bmod 2\end{array} \quad 1 \leq \mathrm{i} \leq \mathrm{n}\right.$
The edge induced labeling are,
$\mathrm{f}^{*}\left(\mathrm{uu}_{\mathrm{i}}\right)=\left\{\begin{array}{ll}0 & i \equiv 1 \bmod 3 \\ 1 & i \equiv 0,2 \bmod 3\end{array} \quad 1 \leq \mathrm{i} \leq \mathrm{n}\right.$
$\mathrm{f}^{*}\left(\mathrm{vu}_{\mathrm{i}}\right)=\left\{\begin{array}{ll}0 & i \equiv 0,2 \bmod 3 \\ 1 & i \equiv 1 \bmod 3\end{array} \quad 1 \leq \mathrm{i} \leq \mathrm{n}\right.$
$\mathrm{f}^{*}\left(\mathrm{uv}_{\mathrm{i}}\right)=\left\{\begin{array}{ll}0 & i \equiv 1 \bmod 2 \\ 1 & i \equiv 0 \bmod 2\end{array} \quad 1 \leq \mathrm{i} \leq \mathrm{n}\right.$
Here, $\mathrm{e}_{\mathrm{f}}(0)=\left\{\begin{aligned} \frac{3 n+1}{2} & n \text { is odd } \\ \frac{3 n}{2} & n \text { is even }\end{aligned}\right.$
$\mathrm{e}_{\mathrm{f}}(1)=\left\{\begin{array}{cc}\frac{3 n-1}{2} & n \text { is odd } \\ \frac{3 n}{2} & n \text { is even }\end{array}\right.$
Hence the graph satisfies the condition $\left|e_{f}(0)-e_{f}(1)\right| \leq 1$
Therefore, the splitting graph $\mathrm{S}\left(\mathrm{K}_{1, \mathrm{n}}\right)$ is a 1-near mean cordial graph.
Illustration 7: The 1- near mean cordial graph of $\mathrm{S}\left(\mathrm{K}_{1,4}\right)$ is shown in the figure 7,


Figure 7 : $S\left(K_{1,4}\right)$

## REFERENCES

1. Albert Williami, Indra Rajasingh and Roy.S, Mean Cordial Labeling of Certain Graphs, Journal of Computer and Mathematical Sciences, vol 4, Issue 4, 31 Augest, 2013 pages (201-321)
2. Gallian.J.A, A Dynamic Survey of Graph Labeling. The Electronic Journal of Combinatorics 6, \#D4, 5S6, 2001.
3. Harary.F, Graph Theory, Addison-Wesley Publishing Company Inc, USA, 1969
4. Nellai Murugan.A and Esther.G, Path related Mean Cordial Graphs, Journal of Global Research in Mathematical Archives, ISSN:2320-5822, Volume 11,No.3, March 2014
5. Nellai Murugan.A and Esther.G, Some Results on Mean Cordial Graphs, International Journal of Mathematics Trends and Technology, ISSN:2231-5373, Volume 11, No.2, July 2014
6. Palani.K, Rejila Jeya Surya.J, 1-Near Mean Cordial Labeling of Graphs, IJMA-6(7), Jully 2015 PP15-20
7. Raja Ponraj, Muthirulan Sivakumar and Murugesan Sundaram, Mean Cordial Labeling of Graphs, Open Journal of Discrete Mathematics, 2012, 2, 145-148.

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