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ON $\delta(\delta g)^{-}$ CLOSED SETS IN TOPOLOGICAL SPACES

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ABSTRACT

In this paper, a new class of generalized closed sets called $\delta(\delta g)^{\wedge}$ -closed sets is introduced and its properties are studied in topological spaces. Moreover the relation between $\delta(\delta g)^{\wedge}$ -closed sets and various other classes of closed sets already defined are investigated.

Keywords: g-closed sets, \hat{g} -closed sets, δg -closed sets, δg^* -closed sets, $\delta(\delta g)^*$ -closed sets, $\delta \hat{g}$ - closed sets and $\delta(\delta g)^{\wedge}$ -closed sets.

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1. INTRODUCTION

The concept of generalized closed (briefly g-closed) sets was introduced and investigated by Norman Levine [6] in 1970. Velicko [10] introduced δ –open sets in 1968 which are stronger than open sets. By combining the concepts of δ - closedness and g –closedness, Julian Dontchev [2] proposed a class of generalised closed sets called δg –closed sets in 1996. Lellis Thivagar [5] defined a new class of closed set called δg - closed set in 2010. Veerakumar [8] and [9]

introduced \hat{g} -closed sets in 2003 and $\delta g^{\#}$ -closed sets in 2006. Meena and Sivakamasundari [7] defined a new class of generalised closed sets called $\delta(\delta g)^*$ -closed sets and various properties were analysed.

Motivated by the development of various classes of δ -closed sets, we extend the concept of δ -generalized closed sets to a new class of closed sets called $\delta(\delta g)^{\wedge}$ -closed sets and investigate their relationship with other existing closed sets in topological spaces. This new class contains the class of $\delta(\delta g)^*$ -closed sets. The following inclusion relation holds.

 $\delta(\delta g)^*$ -closed sets $\subset \delta(\delta g)^{\wedge}$ -closed $\subset \delta g^{\#}$ -closed sets

2. PRELIMINARIES

Definition 2.1 [4]: A Topology on a set X is a collection τ of subsets of X having the following properties:

- a. ϕ and X are in τ .
- b. The union of elements of any sub collection of τ is in τ .
- c. The intersection of the elements of any finite sub collection of τ is in τ .

A set X for which a topology τ has been specified is called a Topological space.

Definition 2.2[7]: A subset A of a Topologica 1 space (X, τ) is called

- 1. Regular open if A = int(cl(A))
- 2. Semi-open if $A \subseteq cl(int(A))$
- 3. Pre-open if $A \subseteq int(cl(A))$
- 4. α -open if A \subseteq int(cl(int(A)))
- 5. semi preopen if $A \subseteq cl(int(cl(A)))$
- 6. π open if it is the finite union of regular open sets.
- 7. δ open if it is the union of regular open sets.

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The complement of a regular open (resp.Semi open, pre-open, α -open, semi preopen, π -open, δ -open) set is called regular closed (resp.semi closed, pre-closed, α - closed, semi preclosed, π -closed and δ -closed).

Definition 2.3[7]: The intersection of all regular closed (resp.semi-closed, pre-closed, α -closed, semi preclosed, π -closed, δ -closed) subsets of (X, τ) containing A is called the regular closure (resp.semi-closure, pre-closure, α -closure, semi preclosure, π -closure, δ -closure) of A and is denoted by rcl(A) ((resp. scl(A), pcl(A), α cl(A), spcl(A), π cl(A) and δ cl(A)).

Definition 2.4: A subset A of a topological space (X, τ) is called

- 1. generalized closed(briefly g-closed) [6] if $cl(A) \subseteq U$ whenever $A \subseteq U$, U is open in (X, τ) .
- 2. regular generalized closed(briefly rg-closed) [7] if $cl(A) \subseteq U$ whenever $A \subseteq U$, U regular is open in (X, τ) .
- 3. δ -generalized closed (briefly δg closed) [2] if $\delta cl(A) \subseteq U$ whenever $A \subseteq U, U$ is open in (X, τ) .
- 4. δ -generalized semi closed(briefly δ gs- closed) [3] if δ scl(A) \subseteq U whenever A \subseteq U, U is δ -open in (X, τ).
- 5. δg^* closed [7] if $\delta cl(A) \subseteq U$ whenever $A \subseteq U$, U is g-open in (X, τ) .
- 6. \hat{g} -closed [10] if cl(A) \subseteq U whenever A \subseteq U, U is semi open in (X, τ).
- 7. $\delta \hat{g}$ -closed [5] if $\delta cl(A) \subseteq U$ whenever $A \subseteq U$, U is \hat{g} -open in (X, τ) .
- 8. $\delta(\delta g)^*$ closed [7] if $\delta cl(A) \subseteq U$ whenever $A \subseteq U$, U is δg -open in (X, τ) .
- 9. α -generalized closed (briefly α g-closed) [7] if α cl(A) \subseteq U whenever A \subseteq U, U is open in (X, τ).
- 10. $\alpha \hat{g}$ closed [7] if $\alpha cl(A) \subseteq U$ whenever $A \subseteq U$, U is \hat{g} -open in (X, τ) .
- 11. generalised pre-closed(briefly gp- closed) [7] if $pcl(A) \subseteq U$ whenever $A \subseteq U$, U is open in (X, τ) .
- 12. generalised pre regular closed(briefly gpr- closed) [7] if $pcl(A) \subseteq U$ whenever $A \subseteq U$, U is regular open in (X, τ) .
- 13. g*p- closed [7] if $pcl(A) \subseteq U$ whenever $A \subseteq U$, U is g open in (X, τ) .
- 14. *g- closed [7] if pcl(A) \subseteq U whenever A \subseteq U, U is \hat{g} -open in (X, τ).
- 15. g*s- closed [7] if scl(A) \subseteq U whenever A \subseteq U, U is gs open in (X, τ).
- 16. generalised semi pre regular closed(briefly gspr- closed) [7] if $spcl(A) \subseteq U$ whenever $A \subseteq U$, U is regular open in (X, τ) .
- 17. (gs)*- closed [7] if cl(A) \subseteq U whenever A \subseteq U, U is gs- open in (X, τ).
- 18. regular weakly generalised closed(briefly rwg- closed) [7] if $cl(int(A)) \subseteq U$ whenever $A \subseteq U$, U is regular open in (X, τ) .
- 19. generalised δ -closed(briefly g δ closed) [7] if cl(A) \subseteq U whenever A \subseteq U, U is δ -open in (X, τ).
- 20. #gs- closed [5] if scl(A) \subseteq U whenever A \subseteq U, U is *g-open in (X, τ).
- 21. $\delta g^{\#}$ closed [9] if $\delta cl(A) \subseteq U$ whenever $A \subseteq U$, U is δ -open in (X, τ) .
- 22. π -generalised closed(briefly π g- closed) [3] if cl(A) \subseteq U whenever A \subseteq U, U is π open in (X, τ).
- 23. π -generalised pre closed(briefly π gp- closed) [3] if pcl(A) \subseteq U whenever A \subseteq U, U is π -open in (X, τ).
- 24. π -generalised semi pre closed(briefly π gsp- closed) [3] if spcl(A) \subseteq U whenever A \subseteq U, U is π open in (X, τ).
- 25. π -generalised b-closed(briefly π gb- closed) [3] if bcl(A) \subseteq U whenever A \subseteq U, U is π open in (X, τ).
- 26. π -generalised semi closed(briefly π gs- closed) [3] if scl(A) \subseteq U whenever A \subseteq U, U is π -open in (X, τ).
- 27. π -generalised α -closed(briefly π g α closed) [3] if α cl(A) \subseteq U whenever A \subseteq U, U is π -open in (X, τ).
- 28. ψ -closed set [1] if scl(A) \subseteq U whenever A \subseteq U and U is sg-open in X.
- 29. ψ g-closed set [1] if ψ cl(A) \subseteq U whenever A \subseteq U and U is open in X.
- 30. ψ g*-closed set [1] if ψ cl(A) \subseteq U whenever A \subseteq U and U is g*-open in X.
- 31. g*-closed set [1] if $cl(A) \subseteq U$ whenever $A \subseteq U$ and U is g-open in X.

Remark 2.5: r-closed(open) $\rightarrow \pi$ -closed(open) $\rightarrow \delta$ -closed(open) $\rightarrow \delta g^*$ -closed(open) $\rightarrow \delta (\delta g)^*$ - closed(open) $\rightarrow \delta g^{\#}$ -closed(open) $\rightarrow g\delta$ -closed(open) [7].

Remark 2.6: For every subset A of X,

- i. $\operatorname{spcl}(A) \subseteq \operatorname{pcl}(A) \subseteq \delta \operatorname{cl}(A)$ [7].
- ii. $\operatorname{spcl}(A) \subseteq \operatorname{scl}(A) \subseteq \operatorname{\deltacl}(A) \subseteq \operatorname{\deltacl}(A)$ (Lemma 3.4 of [3]).
- iii. $bcl(A) \subseteq \delta scl(A)$ (Corollary 3.28 of [3]).

Remark 2.7:

- i. Every $\delta \hat{g}$ -closed set is g-closed and δg –closed (Proposition 3.5 and 3.14 of [5]).
- ii. Every δ -closed set is $\delta \hat{g}$ -closed (Proposition 3.2 of [5]).

3. $\delta(\delta g)^{-}$ -CLOSED SETS

In this section we introduce a new class of closed sets called $\delta(\delta g)^{-1}$ -closed sets which lie between the class of $\delta(\delta g)^{+1}$ -closed sets and the class of $\delta g^{\#}$ -closed sets.

Definition 3.1: A subset A of a topological space (X, τ) is said to be $\delta(\delta g)^{-1}$ -closed sets if $\delta cl(A) \subseteq U$ whenever $A \subseteq U$, U is $\delta \hat{g}$ -open in (X, τ) . The class of all $\delta(\delta g)^{-1}$ -closed sets of (X, τ) is denoted by $\delta(\delta g)^{-1}C(X, \tau)$.

Theorem 3.2: Let A and B are $\delta(\delta g)^{-1}$ -closed sets in a topological space (X, τ), then

- i. $A \bigcup B$ is $\delta(\delta g)^{-closed}$ in (X, τ) .
- ii. A \bigcap B need not be $\delta(\delta g)^{\wedge}$ -closed in (X, τ).

Proof:

- i. Suppose that $A \bigcup B \subseteq U$ where U is any $\delta \hat{g}$ -open in (X, τ) . Then $A \subseteq U$ and $B \subseteq U$. Since A and B are $\delta(\delta g)^{\wedge}$ -closed sets of (X, τ) , $\delta cl(A) \subseteq U$ and $\delta cl(B) \subseteq U$. Also, $\delta cl(A \bigcup B) = \delta cl(A) \bigcup \delta cl(B)$. It follows that, $\delta cl(A \bigcup B) \subset U$. Therefore $A \bigcup B$ is a $\delta(\delta g)^{\wedge}$ -closed set in (X, τ) .
- ii. Let $X = \{a, b, c\}, \tau = \{X, \phi, \{a\}, \{b\}, \{a, b\}\}$. In this topology, the set $\{c\}$ and $\{a, c\}$ are $\delta(\delta g)^{\wedge}$ -closed but their intersection $\{c\}$ is not $\delta(\delta g)^{\wedge}$ -closed.

Theorem 3.3: In a topological space (X, τ) , every δ -closed set is $\delta(\delta g)^{\wedge}$ -closed but the converse need not be true.

Proof: Let A be a δ -closed set and let U be any $\delta \hat{g}$ -open set containing A in (X, τ) . Since A is δ -closed, $\delta cl(A)=A$. Therefore $\delta cl(A) = A \subseteq U$ and hence A is $\delta(\delta g)^{\wedge}$ -closed.

Example: Let $X = \{a, b, c\}, \tau = \{x, \phi, \{a, c\}\}$. In this topology the set $\{b\}$ is $\delta(\delta g)^{-1}$ -closed but not δ -closed.

Theorem 3.4: Let (X, τ) be a topological space and $A \subseteq X$. Then the class of δg^* -closed sets and the class of $\delta(\delta g)^*$ -closed sets are proper subsets of the class of $\delta(\delta g)^*$ -closed sets.

Proof:

- i. Let A be δg^* -closed set and U be any $\delta \hat{g}$ -open set containing A in (X, τ). By Remark 2.7(i), every $\delta \hat{g}$ -open set is g-open. Since A is δg^* -closed, $\delta cl(A) \subseteq U$. Hence A is $\delta(\delta g)^{\wedge}$ -closed.
- ii. Let A be $\delta(\delta g)^*$ -closed set and U be any $\delta \hat{g}$ -open set containing A in (X, τ) . By Remark 2.7(i), every $\delta \hat{g}$ open set is δg -open. Since A is $\delta(\delta g)^*$ -closed, $\delta cl(A) \subseteq U$. Hence A is $\delta(\delta g)^*$ -closed.

Remark 3.5: A $\delta(\delta g)^{-1}$ -closed set need not be a δg^{*-1} -closed and need not be $\delta(\delta g)^{*-1}$ -closed.

Example: Let $X = \{a, b, c\}, \tau = \{X, \phi, \{a, b\}, \{b, c\}, \{b\}\}$. In this topology, the set $\{b\}$ is $\delta(\delta g)^{\wedge}$ -closed but not δg^* closed.

Example: Let $X = \{a, b, c\}, \tau = \{X, \phi, \{c\}, \{a, b\}\}$. In this topology the set $\{a\}$ is $\delta(\delta g)^{\wedge}$ -closed but not $\delta(\delta g)^{*}$ closed.

Remark 3.6: The following diagram gives a diagrammatic representation of the above Theorems.



In the above diagram, $A \longrightarrow B$ means, A implies B but, B does not imply A.

Remark 3.7: r-closed(open) $\rightarrow \pi$ -closed(open) $\rightarrow \delta$ -closed(open) $\rightarrow \delta g^*$ -closed(open) $\rightarrow \delta(\delta g)^*$ -closed(open) $\rightarrow \delta(\delta g)^*$ -closed(open) $\rightarrow \delta g^{\#}$ -closed(open) $\rightarrow g\delta$ -closed(open).

Theorem 3.8: Let (X, τ) be a topological space and $A \subseteq X$ be a $\delta(\delta g)^{-1}$ -closed set. Then A is

i. gδ-closed ii. gpr-closed iii. gspr-closed. The converse part of this Theorem need not be true.

Proof:

- Let A be δ(δg)^-closed set and U be any δ-open set containing A in (X, τ). By Remark 2.7(ii), every δ-open is δĝ -open. Since A is δ(δg)^-closed, δcl(A) ⊆ U. For every subset A of X, cl(A) ⊆ δcl(A). Therefore cl(A) ⊆ U. Hence A is gδ-closed.
- ii. Let A be $\delta(\delta g)^{-1}$ -closed set and U be any regular open set containing A in (X, τ) . By Remark 2.5&7(ii), every regular open is $\delta \hat{g}$ -open and A is $\delta(\delta g)^{-1}$ -closed, $\delta cl(A) \subseteq U$. By Remark 2.6(i), For every subset A of X, $pcl(A) \subseteq \delta cl(A)$ and so we have $pcl(A) \subseteq U$. Hence A is gpr-closed.
- iii. Let A be $\delta(\delta g)^{-1}$ -closed set and U be any regular open set containing A in (X, τ) . By Remark 2.5 and 2.7(ii), every regular open is $\delta \hat{g}$ -open and A is $\delta(\delta g)^{-1}$ -closed, $\delta cl(A) \subseteq U$. By Remark 2.6(i), spcl(A) $\subseteq \delta cl(A)$. And so we have, spcl(A) $\subseteq U$. Hence A is gspr -closed.

Example: Let $X = \{a, b, c\}, \tau = \{X, \varphi, \{a, c\}\}$. In this topology, the set $\{a\}$ is g δ -closed but not $\delta(\delta g)^{\wedge}$ -closed.

Example: Let $X = \{a, b, c\}, \tau = \{X, \phi, \{a, b\}, \{b, c\}, \{b\}\}$. In this topology, the set $\{b\}$ is gpr-closed but not $\delta(\delta g)^{\wedge}$ -closed.

Example: Let $X = \{a, b, c\}, \tau = \{X, \phi, \{a, b\}, \{b, c\}, \{b\}\}$. In this topology, the set $\{b\}$ is gspr-closed but not $\delta(\delta g)^{\wedge}$ closed.

Theorem 3.9: Let (X, τ) be a topological space and $A \subseteq X$. Then,

- i. A is $\delta(\delta g)^{-1}$ -closed set implies, A is $\delta g^{\#}$ -closed.
- ii. A is $\delta(\delta g)^{-1}$ -closed set implies, A is δgs -closed.. The converse part of (i) and (ii) need not be true.

Proof:

- i. Let A be $\delta(\delta g)^{-1}$ -closed and U be any δ -open set containing A in (X, τ). By Remark 2.7(ii), every δ -open set is $\delta \hat{g}^{-1}$ -closed, $\delta cl(A) \subseteq U$. Hence A is $\delta g^{\#}$ -closed.
- ii. Let A be $\delta(\delta g)^{-closed}$ set and U be any δ -open set containing A in (X, τ) . By Remark 2.7(ii), every δ -open is $\delta \hat{g}$ -open and A is $\delta(\delta g)^{-closed}$, $\delta cl(A) \subseteq U$. By Remark 2.6 (iii), $\delta scl(A) \subseteq \delta cl(A)$. And hence, $\delta scl(A) \subseteq U$ and A is δgs -closed.

Example: Let $X = \{a, b, c\}, \tau = \{X, \varphi, \{a, c\}\}$. In this topology, the set $\{c\}$ is $\delta g^{\#}$ -closed but not $\delta(\delta g)^{\wedge}$ -closed.

Example: Let $X = \{a, b, c\}, \tau = \{X, \varphi, \{a, c\}\}$. In this topology, the set $\{c\}$ is δ gs-closed but not $\delta(\delta g)^{\wedge}$ -closed

Theorem 3.10: Let (X, τ) be a topological space and $A \subseteq X$. Then the class of $\delta(\delta g)^{-1}$ -closed sets is a proper subset of each of the classes of rg-closed, rwg-closed, πg -closed, πg -closed and πg -closed sets.

Proof:

- i. Let A be $\delta(\delta g)^{\wedge}$ -closed set and U be any regular open set containing A in (X, τ) . By Remark 2.5 and 2.7(ii), every regular open is $\delta \hat{g}$ -open and A is $\delta(\delta g)^{\wedge}$ -closed, $\delta cl(A) \subseteq U$. For every subset A of X, $cl(A) \subseteq \delta cl(A)$ and so we have $cl(A) \subseteq U$. Hence A is rg-closed.
- ii. Let A be $\delta(\delta g)^{\wedge}$ -closed set and U be any regular open set containing A in (X, τ) . By Remark 2.5 and 2.7(ii), every regular open is $\delta \hat{g}$ -open and A is $\delta(\delta g)^{\wedge}$ -closed, $\delta cl(A) \subseteq U$. As $int(A) \subseteq U$, we have $cl(int(A)) \subseteq cl(A) \subseteq \delta cl(A)$. Then $cl(int(A)) \subseteq U$. Hence A is rwg-closed.
- iii. Let A be $\delta(\delta g)^{-1}$ -closed set and U be any π -open set containing A in (X, τ). By Remark 2.5 and 2.7(ii), every π -open is $\delta \hat{g}$ -open and A is $\delta(\delta g)^{-1}$ -closed, $\delta cl(A) \subseteq U$. By Remark 2.6, $cl(A) \subseteq \delta cl(A)$. And so we have, $cl(A) \subseteq U$. Hence A is πg -closed.
- iv. Let A be $\delta(\delta g)^{-}$ -closed set and U be any π -open set containing A in (X, τ). By Remark 2.5 and 2.7(ii), every π -open is δg -open and A is $\delta(\delta g)^{-}$ -closed, $\delta cl(A) \subseteq U$. By Remark 2.6, $pcl(A) \subseteq \delta cl(A)$. And so we have, $pcl(A) \subseteq U$. Hence A is πgp -closed.

v. Let A be $\delta(\delta g)^{-closed}$ set and U be any π -open set containing A in (X, τ). By Remark 2.5 and 2.7(ii), every π open is $\delta \hat{g}$ -open and A is $\delta(\delta g)^{-closed}$, $\delta cl(A) \subseteq U$. By Remark 2.6(iii), $bcl(A) \subseteq \delta cl(A)$. And so we have, $bcl(A) \subseteq U$. Hence A is πgb -closed.

Remark 3.11: The converse of the above Theorem need not be true.

Example: Let $X = \{a, b, c\}, \tau = \{X, \phi, \{a, c\}\}$. In this topology, the set $\{a\}$ is rg-closed but not $\delta(\delta g)^{\wedge}$ -closed.

Example: Let $X = \{a, b, c\}, \tau = \{X, \phi, \{a, c\}\}$. In this topology, the set $\{a\}$ is rwg-closed but not $\delta(\delta g)^{\wedge}$ -closed.

Example: Let $X = \{a, b, c\}, \tau = \{X, \varphi, \{a, c\}\}$. In this topology, the set $\{a\}$ is πg -closed but not $\delta(\delta g)^{\wedge}$ -closed.

Example: Let $X = \{a, b, c\}, \tau = \{X, \phi, \{a, b\}, \{b, c\}, \{b\}\}$. In this topology, the set $\{b\}$ is π gp-closed but not $\delta(\delta g)^{\wedge}$ closed.

Example: Let $X = \{a, b, c\}, \tau = \{X, \phi, \{a, c\}\}$. In this topology, the set $\{a\}$ is π gb-closed but not $\delta(\delta g)^{\wedge}$ -closed.

Theorem 3.12: Let (X, τ) be a topological space and $A \subseteq X$ be a $\delta(\delta g)^{\wedge}$ -closed set. Then A is (i) $\pi g \alpha$ -closed. (ii) $\pi g s$ -closed (iii) $\pi g s$ -closed. The converse need not be true.

Proof:

- i. Let A be $\delta(\delta g)^{-c}$ -closed set and U be any π -open set containing A in (X, τ). By Remark 2.5 and 2.7(ii), every π -open is $\delta \hat{g}$ -open and A is $\delta(\delta g)^{-c}$ -closed, $\delta cl(A) \subseteq U$. For every subset A of X, $\alpha cl(A) \subseteq \delta cl(A)$. And so we have, $\alpha cl(A) \subseteq U$. Hence A is $\pi g \alpha$ -closed.
- ii. Let A be $\delta(\delta g)^{-c}$ -closed set and U be any π -open set containing A in (X, τ). By Remark 2.5 and 2.7(ii), every π -open is $\delta \hat{g}$ -open and A is $\delta(\delta g)^{-c}$ -closed, $\delta cl(A) \subseteq U$. By Remark 2.6(ii), $scl(A) \subseteq \delta cl(A)$. And so we have, $scl(A) \subseteq U$. Hence A is πgs -closed.
- iii. Let A be $\delta(\delta g)^{\wedge}$ -closed set and U be any π -open set containing A in (X, τ). By Remark 2.5 and 2.7(ii), every π -open is δg -open and A is $\delta(\delta g)^{\wedge}$ -closed, $\delta cl(A) \subseteq U$. By Remark 2.6(i), spcl(A) $\subseteq \delta cl(A)$. And so we have, spcl(A) $\subseteq U$. Hence A is πgsp -closed.

Example: $X = \{a, b, c\}, \tau = \{X, \phi, \{a, b\}, \{b, c\}, \{b\}\}$. In this topology, the set $\{b\}$ is $\pi g\alpha$ -closed but not $\delta(\delta g)^{\wedge}$ -closed.

Example: Let $X = \{a, b, c\}, \tau = \{X, \phi, \{a, b\}, \{b, c\}, \{b\}\}$. In this topology, the set $\{b\}$ is π gs-closed but not $\delta(\delta g)$ -losed

Example: Let $X = \{a, b, c\}, \tau = \{X, \phi, \{a, b\}, \{a\}, \{b\}\}$. In (X, τ) the set $\{a, b\}$ is π gsp-closed but not $\delta(\delta g)^{\wedge}$ -closed.

Remark 3.13: The results of Theorem 3.7 to Theorem 3.12 are illustrated in the following diagram.



In the above diagram, $A \rightarrow B$ means, A implies B, but B does not imply A.

Remark 3.14: The following examples show that, the class $\delta(\delta g)^{\wedge}$ -closed sets are independent from the classes of gclosed sets, δg -closed sets, sg-closed sets, gs-closed sets, αg -closed sets, $\alpha \hat{g}$ -closed sets, #gs-closed sets, g^*p -closed sets, $\delta \hat{g}$ -closed sets, gp-closed sets, gsp-closed sets, ψ -closed sets, ψg -closed sets, gb-closed sets, ψg^* -closed sets.

Example: Let $X = \{a, b, c\}, \tau = \{X, \varphi, \{a\}\}$. In this topology the set $\{c\}$ is g-closed, δg -closed, sg-closed, gs-closed, gs-closed, αg -closed, #g-closed, g = -closed, δg -closed, gs-closed, gs-closed, ψg -closed, ψg -c

Example: Let $X = \{a, b, c\}, \tau = \{X, \phi, \{a, b\}, \{b, c\}, \{b\}\}$. In this topology the set $\{a, b\}$ is $\delta(\delta g)^{-1}$ -closed but not g-closed, δg -closed, gg-closed, gg-closed, αg -closed, αg -closed, $g^* p$ -closed, $g^* p$ -closed, g g-closed, gg-closed, g

Example: Let $X = \{X, \phi, \{a\}\}, \tau = \{X, \phi, \{a\}\}$. In this topology the set $\{b\}$ is g*s-closed but not $\delta(\delta g)^{-1}$ -closed.

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