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ON NANO (1, 2)* REGULAR-GENERALIZED CLOSED SETS IN NANO BITOPOLOGICAL SPACES

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ABSTRACT

The purpose of this paper is to define and study a new class of set called Nano (1,2)* regular-generalized closed sets in nano bitopological spaces. Basic properties of nano (1,2)* regular-generalized closed sets are analyzed. Also we introduce the new notions of nano (1,2)* regular-generalized closure and their relation with already existing well known sets are also investigated.

Keywords: Nano (1,2)* Regular-Generalized Closed sets, Nano (1,2)* Regular-Closure, Nano (1,2)* Regular-Interior, Nano (1,2)* regular closed sets.

1. INTRODUCTION

In 1970, Levine [5] introduced the concept of generalized closed sets as a generalization of closed sets in topological spaces. Later on N.Palaniappan [7] studied the concept of regular generalized closed set in a topological space. In 2011, Sharmistha Bhattacharya [8] have introduced the notion of generalized regular closed sets in topological space. The notion of nano topology was introduced by Lellis Thivagar[6]. In 1963, J.C.Kelly[4] initiated the study of bitopological spaces. In 2014 K.Bhuvaneswari *et al.*, [1, 2] have introduced the notion of nano regular generalized and generalized regular closed sets in nano topological spaces and Nano bitopological spaces. In this paper, we have introduced a new class of sets on nano bitopological spaces called nano (1,2)* regular generalized closed sets and the relation of these new sets with the existing sets.

2. PRELIMINARIES

Definition 2.1 [7]: A subset A of a topological space (X,τ) is called a regular open set if A = Int[cl(A)]. The complement of a regular open set of a space X is called regular closed set in X.

Definition 2.2 [7]: A regular-closure of a subset A of X is the intersection of all regular closed sets that contains A and it is denoted by rcl(A).

Definition 2.3 [7]: The union of all regular open subsets of X contained in A is called regular-interior of A and it is denoted by rInt(A).

Definition 2.4 [7]: A subset A of (X, τ) is called a regular generalized closed set (briefly rg-closed) if $rcl(A) \subseteq U$ whenever $A \subset U$ and U is regular-open in X.

Definition 2.5 [7]: The regular-generalized closure of a subset A of a space X is the intersection of all regular-generalized closed sets containing A and is denoted by rgcl(A). The regular-generalized interior of a subset A of a space X is the union of all regular generalized open sets contained in A and is denoted by rgInt(A).

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Definition 2.6 [6]: Let U be the universe, R be an equivalence relation on U and $\tau_R(X) = \{U, \phi, L_R(X), U_R(X), B_R(X)\}$ where $X \subseteq U$. Then, $\tau_R(X)$ satisfies the following axioms:

- U and $\Phi \in \tau_R(X)$
- The union of the elements of any sub-collection of $\tau_R(X)$ is in $\tau_R(X)$
- The intersection of the elements of any finite sub collection of $\mathcal{T}_R(X)$ is in $\mathcal{T}_R(X)$.

 Then $\mathcal{T}_R(X)$ is a topology on U called the nano topology on U with respect to X. $(U, \mathcal{T}_R(X))$ is called the nano topological space. Elements of the nano topology are known as nano open sets in U. Elements of $[\mathcal{T}_R(X)]^c$ are called nano closed sets in $\mathcal{T}_R(X)$.

Definition 2.7 [6]: If $(U, \mathcal{T}_R(X))$ is a nano topological space with respect to X where $X \subseteq U$ and if $A \subseteq U$, then

- The nano interior of the set A is defined as the union of all nano open subsets contained in A and is denoted by NInt(A). NInt(A) is the largest nano open subset of A.
- The nano closure of the set A is defined as the intersection of all nano closed sets containing A and is denoted by Ncl(A). Ncl(A) is the smallest nano closed set containing A.

Definition 2.8 [6]: Let $(U, \mathcal{T}_R(X))$ be a nano topological space and $A \subseteq U$. Then A is said to be

- Nano regular open if $A \subseteq NInt[Ncl(A)]$
- Nano regular closed if $Ncl[NInt(A)] \subseteq A$

NRO(U,X), NRC(U,X) respectively denote the families of all nano regular open, nano regular closed subsets of U.

Definition 2.9 [6]: If $(U, \mathcal{T}_R(X))$ is a nano topological space with respect to X where $X \subseteq U$ and if $A \subseteq U$, Then

- (i) The nano regular-closure of A is defined as the intersection of all nano regular closed sets containing A and it is denoted by Nrcl(A). Nrcl(A) is the smallest nano regular closed set containing A.
- (ii) The nano regular-interior of A is defined as the union of all nano regular open subsets of A contained in A and it is denoted by NrInt(A). NrInt(A) is the largest nano regular open subset of A.

Definition 2.10 [1]: A subset A of $(U, \tau_R(X))$ is called nano regular-generalized closed set (briefly Nrg-closed) if $Nrcl(A) \subseteq V$ whenever $A \subseteq V$ and V is nano regular open in $(U, \tau_R(X))$.

Definition 2.11 [3]: Let $(X, \mathcal{T}_{1,2})$ be a bitopological space and $A \subseteq U$. Then A is said to be

- $(1,2)^*$ Regular open if $A \subseteq \mathcal{T}_{1,2}Int[\mathcal{T}_{1,2}cl(A)]$
- $(1,2)^*$ Regular closed if $\tau_{1,2}cl[\tau_{1,2}Int(A)] \subseteq A$

(1,2)*RO(X), (1,2)*RC(X) respectively denote the families of all (1,2)* regular open, (1,2)* regular closed subsets of X.

Definition 2.12 [3]: If $(X, \mathcal{T}_{1,2})$ is a bitopological space with respect to X where $X \subseteq U$ and if $A \subseteq U$, then

- (i) The $(1,2)^*$ regular-closure of A is defined as the intersection of all $(1,2)^*$ regular closed sets containing A and it is denoted by $\mathcal{T}_{1,2}$ rcl(A). $\mathcal{T}_{1,2}$ rcl(A) is the smallest $(1,2)^*$ regular closed set containing A.
- (ii) The $(1,2)^*$ regular-interior of A is defined as the union of all $(1,2)^*$ regular open subsets of A contained in A and it is denoted by $\tau_{1,2}$ rInt(A). $\tau_{1,2}$ rInt(A) is the largest $(1,2)^*$ regular open subset of A.

Definition 2.13 [3]: A subset A of $(X, \mathcal{T}_{1,2})$ is called $(1, 2)^*$ regular-generalized closed set (briefly $(1,2)^*$ rg-closed) if $\mathcal{T}_{1,2}rcl(A) \subseteq U$ whenever $A \subseteq U$ and U is $(1,2)^*$ regular open in $(X, \mathcal{T}_{1,2})$.

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Definition 2.14 [2]: Let U be the universe, R be an equivalence relation on U and $\mathcal{T}_{R_{1,2}}(X) = \bigcup \{\mathcal{T}_{R_1}(X), \mathcal{T}_{R_2}(X)\}$ where $\mathcal{T}_R(X) = \{U, \phi, L_R(X), U_R(X), B_R(X)\}$ and $X \subseteq U$ Then $\mathcal{T}_R(X)$ satisfies the following axioms:

- U and $\Phi \in \mathcal{T}_{R}(X)$
- The union of the elements of any sub-collection of $\mathcal{T}_R(X)$ is in $\mathcal{T}_R(X)$.
- The intersection of the elements of any finite sub collection of $\mathcal{T}_R(X)$ is in $\mathcal{T}_R(X)$.

 Then $(U, \mathcal{T}_{R_{1,2}}(X))$ is called the nano bitopological space. Elements of the nano bitopology are known as nano $(1, 2)^*$ open sets in U. Elements of $[\mathcal{T}_{R_{1,2}}(X)]^c$ are called nano $(1, 2)^*$ closed sets in $\mathcal{T}_{R_{1,2}}(X)$.

Definition 2.15 [2]: If $(U, \mathcal{T}_{R_{1,2}}(X))$ is a nano bitopological space with respect to X where $X \subseteq U$ and if $A \subseteq U$, then

- The nano $(1,2)^*$ closure of A is defined as the intersection of all nano $(1,2)^*$ closed sets containing A and it is denoted by $N_{\mathcal{T}_{1,2}}cl(A)$. $N_{\mathcal{T}_{1,2}}cl(A)$ is the smallest nano $(1,2)^*$ closed set containing A.
- The nano $(1, 2)^*$ interior of A is defined as the union of all nano $(1, 2)^*$ open subsets of A contained in A and it is denoted by $N_{\mathcal{T}_{1,2}}Int(A)$. $N_{\mathcal{T}_{1,2}}Int(A)$ is the largest nano $(1, 2)^*$ open subset of A.

3. NANO (1,2)* REGULAR GENERALIZED CLOSED SETS

In this section, the definition of nano $(1,2)^*$ regular closed sets and nano $(1,2)^*$ regular-generalized closed sets are introduced and studied some of its properties.

Definition 3.1: A subset A of $(U, \mathcal{T}_{R_{1,2}}(X))$ is called **nano** (1,2)* **regular open** set if $A \subseteq N_{\mathcal{T}_{1,2}}Int[N_{\mathcal{T}_{1,2}}cl(A)]$. The complement of a nano (1, 2)* regular open set of a space U is called **nano** (1,2)* **regular closed** set in $(U, \mathcal{T}_{R_{1,2}}(X))$.

Definition 3.2: If $(U, \mathcal{T}_{R_{1,2}}(X))$ is a nano bitopological space with respect to X where $X \subseteq U$ and if $A \subseteq U$, then

- (i) The **nano** (1,2)* **regular-closure** of A is defined as the intersection of all nano (1,2)* regular closed sets containing A and it is denoted by $N_{\mathcal{T}_{1,2}}rcl(A)$. $N_{\mathcal{T}_{1,2}}rcl(A)$ is the smallest nano (1,2)* regular closed set containing A.
- (ii) The **nano** (1,2)* **regular-interior** of A is defined as the union of all nano (1,2)* regular open subsets of A contained in A and it is denoted by $N_{\mathcal{T}_{1,2}}rInt(A)$. $N_{\mathcal{T}_{1,2}}rInt(A)$ is the largest nano (1,2)* regular open subsets of A.

Definition 3.3: A subset A of $(U, \mathcal{T}_{R_{1,2}}(X))$ is called **nano** (1,2)* **regular-generalized closed** set (briefly N(1,2)*rg-closed) if $N_{\mathcal{T}_{1,2}}rcl(A) \subseteq V$ whenever $A \subseteq V$ and V is nano (1,2)* regular open in $(U, \mathcal{T}_{R_{1,2}}(X))$.

Example 3.4: Let
$$U = \{a,b,c,d\}$$
 with $U/R = \{\{c\},\{d\},\{a,b\}\}$ $X_1 = \{a,c\}$ and $\mathcal{T}_{R_1}(X) = \{U,\phi,\{c\},\{a,b,c\},\{a,b\}\}$

$$X_2 = \{a,d\}$$
 and $\mathcal{T}_{R_2}(X) = \{U,\phi,\{d\},\{a,b,d\},\{a,b\}\}$

Then $\mathcal{T}_{R_{1,2}}(X) = \{U, \phi, \{c\}, \{d\}, \{a,b\}, \{a,b,c\}, \{a,b,d\}\}$ which are (1,2)* open sets.

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The nano $(1,2)^*$ closed sets = $\{U, \phi, \{c\}, \{d\}, \{c,d\}, \{a,b,c\}, \{a,b,d\}\}$.

The nano (1,2)* regular closed sets = $\{U, \phi, \{c\}, \{d\}, \{a,b\}, \{c,d\}, \{a,b,c\}, \{a,b,d\}\}$

The nano (1,2)* regular open sets = $\{U, \phi, \{a,b,d\}, \{a,b,c\}, \{c,d\}, \{a,b\}, \{d\}, \{c\}\}\}$

The nano (1,2)* regular-generalized open sets are

$$\{U, \phi, \{a\} \{b\}, \{c\}, \{d\}, \{a,b\}, \{a,c\}, \{a,d\}, \{b,c\}, \{b,d\}, \{c,d\}, \{a,b,c\}, \{a,b,d\}, \{a,c,d\}, \{b,c,d\}\}$$

The nano (1,2)* regular-generalized closed sets are

$$\{U, \emptyset, \{a\}\{b\}, \{c\}, \{d\}, \{a,b\}, \{a,c\}, \{a,d\}, \{b,c\}, \{b,d\}, \{c,d\}, \{a,b,c\}, \{a,b,d\}, \{a,c,d\}, \{b,c,d\}\} \}.$$

Theorem 3.5: Let $(U, \tau_{R_{1,2}}(X))$ be a nano bitopological space. If a subset A of a nano bitopological space $(U, \tau_{R_{1,2}}(X))$ is nano $(1,2)^*$ closed set in $(U, \tau_{R_{1,2}}(X))$, then A is a nano $(1,2)^*$ regular closed set in $(U, \tau_{R_{1,2}}(X))$.

Proof: Let A be a nano $(1,2)^*$ closed set in X such that $A \subseteq U$; whenever U is $(1,2)^*$ regular open. That is $N_{\mathcal{T}_{1,2}}cl(A) = A$. To prove that $N_{\mathcal{T}_{1,2}}cl(N_{\mathcal{T}_{1,2}}Int(A)) \subseteq A$. Since A is nano $(1,2)^*$ regular open in U.

Therefore
$$N_{\mathcal{T}_{1,2}}cl(A) = A$$
 which implies $N_{\mathcal{T}_{1,2}}cl(N_{\mathcal{T}_{1,2}}Int(A)) = N_{\mathcal{T}_{1,2}}cl(A) = A$.

Hence A is a nano (1,2)* regular closed set. Also every nano (1,2)* open set is nano (1,2)* regular open set.

The converse of the above Theorem 3.5 is not true from the following example.

Example 3.6: Let
$$U = \{a, b, c, d\}$$
 with $U / R = \{\{c\}, \{d\}, \{a, b\}\}$

$$X_1 = \{a, c\}$$
 and $\mathcal{T}_{R_1}(X) = \{U, \phi, \{c\}, \{a, b, c\}, \{a, b\}\}$

$$X_2 = \{a,d\}$$
 and $\mathcal{T}_{R_2}(X) = \{U,\phi,\{d\},\{a,b,d\},\{a,b\}\}$

Then $\mathcal{T}_{R_{1,2}}(X) = \{U, \phi, \{c\}, \{d\}, \{a,b\}, \{a,b,c\}, \{a,b,d\}\}\$ which are $(1,2)^*$ open sets.

The nano (1,2)* closed sets = $\{U, \phi, \{c\}, \{d\}, \{c,d\}, \{a,b,c\}, \{a,b,d\}\}$.

The nano $(1,2)^*$ regular closed sets = $\{U, \phi, \{c\}, \{d\}, \{a,b\}, \{c,d\}, \{a,b,c\}, \{a,b,d\}\}$

Let $A=\{c, d\}$ be a nano $(1,2)^*$ closed set.

$$N_{\tau_1}cl(A) = \{c, d\}.$$

$$N_{\mathcal{T}_{1,2}}Int(N_{\mathcal{T}_{1,2}}cl(A)) = \{c,d\}$$
 which implies $N_{\mathcal{T}_{1,2}}Int(N_{\mathcal{T}_{1,2}}cl(A)) \subseteq A$.

Hence every nano (1,2)* closed set is a nano (1,2)* regular closed set.

Here $\{a, b\}$ is nano (1,2)* regular closed sets but it is not nano (1,2)* closed set.

Theorem 3.7: Let $(U, \mathcal{T}_{R_{1,2}}(X))$ be a nano bitopological space. If a subset A of a nano bitopological space $(U, \mathcal{T}_{R_{1,2}}(X))$ is nano $(1,2)^*$ regular closed set in $(U, \mathcal{T}_{R_{1,2}}(X))$, then A is a nano $(1,2)^*$ regular-generalized closed set in $(U, \mathcal{T}_{R_{1,2}}(X))$.

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Proof: Let A be a nano $(1, 2)^*$ regular closed set in X and $A \subseteq V$, V is nano $(1, 2)^*$ regular open in U. That is $N_{\mathcal{T}_{1,2}} cl[N_{\mathcal{T}_{1,2}} Int(A)] = A$. Since A is nano $(1,2)^*$ regular open, $N_{\mathcal{T}_{1,2}} Int(A) = A$. Every nano $(1,2)^*$ open set is nano $(1,2)^*$ regular open. Therefore $N_{\mathcal{T}_{1,2}} cl(A) = A \subseteq V$ implies $N_{\mathcal{T}_{1,2}} cl(A) \subseteq V$. Since $A \subseteq V$ then $N_{\mathcal{T}_{1,2}} cl(A) \subseteq V$ whenever V is nano $(1,2)^*$ regular open in U. Hence A is a nano $(1,2)^*$ regular generalized closed set.

The converse of the above Theorem 3.7 is not true from the following example.

Example 3.8: Let
$$U = \{a,b,c,d\}$$
 with $U/R = \{\{c\},\{d\},\{a,b\}\}$
$$X_1 = \{a,c\} \text{ and } \mathcal{T}_{R_1}(X) = \{U,\phi,\{c\},\{a,b,c\},\{a,b\}\}$$

$$X_2 = \{a,d\} \text{ and } \mathcal{T}_{R_2}(X) = \{U,\phi,\{d\},\{a,b,d\},\{a,b\}\}$$
 Then $\mathcal{T}_{R_1}(X) = \{U,\phi,\{c\},\{d\},\{a,b\},\{a,b,c\},\{a,b,d\}\}$ which are (1,2)* open sets.

Here $\{\{a\},\{b\},\{a,c\},\{a,d\},\{b,c\},\{b,d\},\{a,c,d\},\{b,c,d\}\}$ are nano (1,2)* regular generalized closed sets but it is not nano (1,2)* regular closed.

Theorem 3.9: The union of two nano $(1,2)^*$ regular-generalized closed sets in $(U, \mathcal{T}_{R_{1,2}}(X))$ is also a nano $(1,2)^*$ regular-generalized closed set in $(U, \mathcal{T}_{R_{1,2}}(X))$.

Proof: Let A and B be two nano $(1,2)^*$ regular-generalized closed sets in $(U, \mathcal{T}_{R_{1,2}}(X))$. Let V be any nano $(1,2)^*$ regular open set in U such that $A \subseteq V$ and $B \subseteq V$. Then we have $A \bigcup B \subseteq V$. As A and B are nano $(1,2)^*$ regular-generalized closed sets in $(U, \mathcal{T}_{R_{1,2}}(X))$. Therefore $N_{\mathcal{T}_{1,2}}rcl(A) \subseteq V$ and $N_{\mathcal{T}_{1,2}}rcl(B) \subseteq V$.

Now $N_{\mathcal{T}_{1,2}}rcl(A \cup B) = N_{\mathcal{T}_{1,2}}rcl(A) \cup N_{\mathcal{T}_{1,2}}rcl(B) \subseteq V$. Thus we have $N_{\mathcal{T}_{1,2}}rcl(A \cup B) \subseteq V$ whenever $A \cup B \subseteq V$, V is nano (1,2)* regular open set in $(U, \mathcal{T}_{R_{1,2}}(X))$ which implies $A \cup B$ is a nano (1,2)* regular-generalized closed set in $(U, \mathcal{T}_{R_{1,2}}(X))$.

Theorem 3.10: The intersection of any two subsets of nano $(1,2)^*$ regular-generalized closed sets in $(U, \tau_{R_{1,2}}(X))$ is nano $(1,2)^*$ regular-generalized closed set in $(U, \tau_{R_{1,2}}(X))$.

Proof: Let A and B are any two nano $(1,2)^*$ regular-generalized closed sets. $A \subseteq V$; V is an nano $(1,2)^*$ regular open and $B \subseteq V$; V is nano $(1,2)^*$ regular open. Then $N_{\mathcal{T}_{1,2}}rcl(A) \subseteq V$ and $N_{\mathcal{T}_{1,2}}rcl(B) \subseteq V$. Therefore $N_{\mathcal{T}_{1,2}}rcl(A \cap B) \subseteq V$. V is nano $(1,2)^*$ regular open in X. Since A and B nano $(1,2)^*$ regular generalized closed sets. Hence $A \cap B$ is a nano $(1,2)^*$ regular generalized closed set.

Theorem 3.11: If a set A is nano $(1,2)^*$ regular generalized closed set iff $N_{\mathcal{T}_{1,2}}rcl(A) - A$ contains no non-empty, nano $(1,2)^*$ regular closed set.

Proof:

Necessity: Let F be a nano $(1,2)^*$ regular closed set in $(U, \mathcal{T}_{R_{1,2}}(X))$ such that $F \subseteq N_{\mathcal{T}_{1,2}}rcl(A) - A$. Then $A \subseteq X - F$. Since A is nano $(1,2)^*$ regular generalized closed set and X-F is nano $(1,2)^*$ regular open then $N_{\mathcal{T}_{1,2}}rcl(A) \subseteq X - F$. That is $F \subseteq X - N_{\mathcal{T}_{1,2}}rcl(A)$. So $F \subseteq (X - N_{\mathcal{T}_{1,2}}rcl(A)) \cap (N_{\mathcal{T}_{1,2}}rcl(A) - A)$. Therefore $F = \varphi$.

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Sufficiency: Let us assume that $N_{\mathcal{T}_{1,2}}rcl(A) - A$ contains no non empty nano $(1,2)^*$ regular closed set. Let $A \subset V$; V is nano $(1,2)^*$ regular open.

Suppose that $N_{\mathcal{T}_{1,2}}rcl(A)$ is not contained in V, $N_{\mathcal{T}_{1,2}}rcl(A) \cap V^c$ is non empty, nano (1,2)* regular closed set of $N_{\mathcal{T}_{1,2}}rcl(A) - A$ which is contradiction therefore $N_{\mathcal{T}_{1,2}}rcl(A) \subseteq V$. Hence A is nano (1,2)* regular generalized closed.

Theorem 3.12: If A is both nano $(1,2)^*$ regular open and nano $(1,2)^*$ regular generalized closed set in X, then A is nano $(1,2)^*$ regular closed set.

Proof: Since A is nano $(1,2)^*$ regular open and nano $(1,2)^*$ regular generalized closed in X, $N_{\mathcal{T}_{1,2}}rcl(A) \subseteq V$ But $A \subseteq N_{\mathcal{T}_{1,2}}rcl(A)$. Therefore $A = N_{\mathcal{T}_{1,2}}rcl(A)$. Since A is nano $(1,2)^*$ closed $N_{\mathcal{T}_{1,2}}Int(A) = A$. Implies $N_{\mathcal{T}_{1,2}}rcl(A) = A$. Hence A is nano $(1,2)^*$ regular closed.

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