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INTUITIONISTIC FUZZY ASSIGNMENT PROBLEM WITH REPLACEMENT BASED ON INTUITIONISTIC FUZZY AGGREGATION

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ABSTRACT

The objective of this paper is to develop an intuitionistic fuzzy assignment model to draw attention to problems involving breakdowns while assigning. Corporate competitiveness is heavily influenced by the professional (skilled) staff involved in the decision making. The job performance of a professional may correlate to the time taken to task. Two issues being analysed in this approach. The first one is to develop an ideal priority of groups and the second one is to replace the person where we need to avoid breakdowns. Replacement is made in the form of maximum intuitionistic fuzzy scoring by utilizing the intuitionistic fuzzy aggregation operator to aggregate the given intuitionistic fuzzy information and by the weight vector. A numerical example is given to clarify the developed approach under intuitionistic fuzzy environment.

AMS Mathematics subject classification: 90C08, 90C70.

Keywords – Intuitionistic fuzzy; break down; aggregate operator.

1. INTRODUCTION :

The complexity of socioeconomic environments often makes it difficult for a single decision maker to consider all the important aspects of some decision problems. So the corporates employ groups of people in decision making. In the real world many decision making processes take place in group settings. In 1952 Votaw and Orden [16] first proposed the assignment problem. Lin and Wen [10] concentrate on the assignment problem where costs are not deterministic numbers but imprecise ones. Huang and Zhang [12] proposed a mathematical model for the fuzzy assignment problem with restriction on qualification. Chen [6] introduced a fuzzy assignment model that considers all individuals have same skills. Kuhn [9] developed the Hungarian algorithm for the assignment problem. Balinski and Gomory [4] introduced a labeling algorithm for solving assignment problem. Aggarwal *et al.* [1] developed an algorithm for bottleneck assignment problem. Liu and Gao [11] introduced fuzzy weighted equilibrium multi-job assignment problem and genetic algorithm. Yang and Liu [20] proposed a multi – objective fuzzy assignment problem. Mukherjee and Basu [13] proposed intuitionistic fuzzy assignment problem by using similarity measures and score functions. Sakawa *et al.* [15] dealt with problems on production and work force assignment in a firm.

In the information technology, construction work, military operation, election work etc for a single task different characteristics are considered, that is for a single job a team is assigned. In the usual situation the assignment is made with respect to one to one basis in such a way that the total time or total cost involved is minimized and the total sales or total profit is maximized. Some complexity may happen while assigning the jobs to the teams. The job performance of a worker may correlate to the time taken to finish the task. Each team needs a minimum time to perform task to maximize the profit. To reach our goal some replacement is made to avoid breakdowns. In such situation two issues being analysed. The first one is to develop ideal priorties of a group by utilizing intuitionistic fuzzy operators like intuitionistic fuzzy hybrid averaging (IFHA) operator, intuitionistic fuzzy hybrid weighted geometric (IFHWG) operator etc to aggregate the given intuitionistic fuzzy information. The second one is replacement. It is made from the pool of workers which is characterized by priorities by utilizing intuitionistic fuzzy aggregative operators.

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2. PRELIMINARIES ON INTUITIONISTIC FUZZY SETS

This section presents the basic concepts related to Intuitionistic Fuzzy Set, which was originally introduced by Attanassov and Gargov.

2.1. Intuitionistic Fuzzy Sets (IFS)

Let $X = \{x_1, x_2, ..., x_n\}$ be a universe of discourse. A fuzzy set= $\{(x_j, \mu_A(x_j)) | x_j \in X\}$, defined by zadeh [21] is characterized by a membership function $\mu_A: X \to [0,1]$ where $\mu_A(x_j)$ denotes the degree of membership of the element x_j to the set A.

Atanassov [3] introduced a generalized fuzzy set called IFS as follows:

An Intuitionistic Fuzzy Set (IFS) *A* in *X* is an object having the form: $A = \{(x_j, \mu_A(x_j), \vartheta_A(x_j)) | x_j \in X\}$ which is characterized by a membership function μ_A and a nonmembership function ϑ_A where $\mu_A: X \to [0,1], \vartheta_A: X \to [0,1]$ with the condition $\mu_A(x_j) + \vartheta_A(x_j) \leq 1$ for all $x_j \in X$. Attanassov defined $\pi_A(x_j) = 1 - \mu_A(x_j) - \vartheta_A(x_j)$, for all $x_j \in X$ as the degree of indeterminacy or hesitancy of x_j to *A* where *A* is an IFS in *X*. Especially, if $\pi_A(x_j) = 1 - \mu_A(x_j) - \vartheta_A(x_j) = 0$ for each $x_j \in X$ then the IFS A is reduced to a fuzzy set.

2.2 Intuitionistic Fuzzy Number (IFN)

An Intuitionistic fuzzy number A is defined as follows:

- (i) intuitionistic fuzzy sub set of the real line.
- (ii) normal i.e. there is any $x_0 \in \mathbb{R}$ such that $\mu_A(x_0) = 1$ (so $\vartheta_A(x_0) = 0$)
- (iii) a convex set for the membership function $\mu_A(x)$
- $\mu_A(\lambda x_1 + (1 \lambda)x_2) \ge \min(\mu_A(x_1), (\mu_A(x_2)) \text{ for all } x_1, x_2 \in \mathbb{R}, \ \lambda \in [0, 1]$
- (iv) a concave set for the non membership function $\vartheta_A(x)$ i.e $\vartheta_A(\lambda x_1 + (1 - \lambda)x_2) \le max(\vartheta_A(x_1), (\vartheta_A(x_2)))$ for all $x_1, x_2 \in \mathbb{R}, \lambda \in [0,1]$

2.3 Ranking of Intuitionistic Fuzzy Number

Let $a = (\mu_1, \vartheta_1)$ be an intuitionistic fuzzy number. Chen and Tan [7] introduced a score function S of an intuitionistic fuzzy value, which is represented as follows:

$$S(a) = \mu_1 - \vartheta_1 \text{ where } S(a) \in [-1,1].$$
(1)

The larger the score S(a), the greater the intuitionistic fuzzy value *a*. Hong and Choi [8] defined an accuracy function H to evaluate the degree of accuracy of the intuitionistic fuzzy value *a* where $H(a) \in [0,1]$ and $H(a) = \mu_1 + \vartheta_1$ (2)

The larger the value of H(a), the more the degree of accuracy of the degree of membership of the intuitionistic fuzzy value a.

Let $b = (\mu_2, \vartheta_2)$ be another intuitionistic fuzzy number. Based on the score function *S* and the accuracy function *H*, in the following, Xu and Yager [17] give an order relation between two intuitionistic fuzzy value *a* and *b* which is defined as follows:

- If S(a) < S(b) then a < b
- If S(a) > S(b) then a > b
- If S(a) = S(b) and
- If H(a) = H(b) then a = b
- If H(a) < H(b) then a < b
- If H(a) > H(b) then a > b.

2.4 Operational Laws of Intuitionistic Fuzzy Number (Xu and Yager, 2006)

Let $\alpha = (\mu_{\alpha}, \vartheta_{\alpha}), \alpha_1 = (\mu_{\alpha_1}, \vartheta_{\alpha_1})$ and $\alpha_2 = (\mu_{\alpha_2}, \vartheta_{\alpha_2})$ be IFNs. Then

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(1) $\bar{\alpha} = (\vartheta_{\alpha}, \mu_{\alpha})$ where $\bar{\alpha}$ is the complement of α (2) $\alpha_1 \wedge \alpha_2 = (\min\{\mu_{\alpha_1}, \mu_{\alpha_2}\}, \max\{\vartheta_{\alpha_1}, \vartheta_{\alpha_2}\});$ (3) $\alpha_1 \vee \alpha_2 = (\max\{\mu_{\alpha_1}, \mu_{\alpha_2}\}, \min\{\vartheta_{\alpha_1}, \vartheta_{\alpha_2}\});$ (4) $\alpha_1 \oplus \alpha_2 = (\mu_{\alpha_1} + \mu_{\alpha_2} - \mu_{\alpha_1}\mu_{\alpha_2}, \vartheta_{\alpha_1}\vartheta_{\alpha_2});$ (5) $\alpha_1 \oplus \alpha_2 = \mu_{\alpha_1} + \mu_{\alpha_2} - \mu_{\alpha_1}\mu_{\alpha_2}, \vartheta_{\alpha_1}\vartheta_{\alpha_2}$ (6) $\lambda \alpha = (1 - (1 - \mu_{\alpha})^{\lambda}, \vartheta_{\alpha}^{\lambda}), \lambda > 0;$ (7) $\alpha^{\lambda} = (\mu_{\alpha}^{\lambda}, 1 - (1 - \vartheta_{\alpha})^{\lambda}), \lambda > 0.$

Theorem 1 (Xu, 2007): Let $\dot{\alpha}_1 = \alpha_1 \oplus \alpha_2$, $\dot{\alpha}_2 = \alpha_1 \otimes \alpha_2$, $\dot{\alpha}_3 = \lambda \alpha$, $\dot{\alpha}_4 = \alpha^{\lambda}$ and $\lambda > 0$. Then all $\dot{\alpha}_i$ (i = 1, 2, 3, 4) are IFNs.

Definition (Xu, 2007): Let Θ be the set of all IFNs. An intuitionistic fuzzy hybrid averaging (IFHA) operator is a mapping IFHA: $\Theta^n \to \Theta$, such that

 $IFHA_{\omega,\omega}(\alpha_1,\alpha_2,\ldots,\alpha_n) = \omega_1 \dot{\alpha}_{\sigma(1)} \oplus \omega_2 \dot{\alpha}_{\sigma(2)} \oplus \ldots \oplus \omega_n \dot{\alpha}_{\sigma(n)}$ (3)

where $\omega = (\omega_1, \omega_2, ..., \omega_n)^T$ is the weighting vector associated with the IFHA operator, with $\omega_j \in [0, 1]$ (j = 1, 2, ..., n) and $\sum_{j=1}^{n} \omega_j = 1$; $\dot{\alpha}_j = n \omega_j \alpha_j$, j = 1, 2, ..., n, $(\dot{\alpha}_{\sigma(1)}, \dot{\alpha}_{\sigma(2)}, ..., \dot{\alpha}_{\sigma(n)})$ is any permutation of a collection of the weighted IFNs $(\dot{\alpha}_1, \dot{\alpha}_2, ..., \dot{\alpha}_n)$, such that $\dot{\alpha}_{\sigma(j)} \ge \dot{\alpha}_{\sigma(j+1)}$ (j = 1, 2, ..., n-1); $\omega = (\omega_1, \omega_2, \dots, \omega_n)^T$ is weight vector of α_j $(j = 1, 2, \dots, n)$, with $\omega_j \in [0, 1]$ $(j = 1, 2, \dots, n)$ and $\sum_{i=1}^n \omega_i = 1$, and *n* is the balancing coefficient.

Let $\dot{\alpha}_{\sigma(j)} = (\mu_{\dot{\alpha}_{\sigma(j)}}, \vartheta_{\dot{\alpha}_{\sigma(j)}})$ (j = 1, 2, ..., n). Then by (Xu 2007), we have $IFHA_{\omega,\omega}(\alpha_1,\alpha_2,\ldots,\alpha_n) = \left(1 - \prod_{j=1}^n \left(1 - \mu_{\dot{\alpha}_{\sigma(j)}}\right)^{\omega_j}, \prod_{j=1}^n \vartheta_{\dot{\alpha}_{\sigma(j)}}^{\omega_j}\right)$ and the aggregated value by using the IFHA operator is also an IFN. (4)

3. MULTI-ATTRIBUTE DECISION MAKING PROBLEM

Let $P = \{P_1, P_2, ..., P_n\}$ be a finite set of alternatives, $Q = \{Q_1, Q_2, ..., Q_m\}$ a set of attributes, and $\omega = (\omega_1, \omega_2, ..., \omega_n)^T$ the weight vector of attributes, where $\omega_j \in [0, 1]$ (j = 1, 2, ..., m) and $\sum_{j=1}^n \omega_j = 1$. Suppose that the characteristics of the alternatives P_i (i = 1, 2, ..., n) are represented by the IFNs:

$$P_{i} = \{ \langle Q_{j}, \mu_{P_{i}}(Q_{j}), \vartheta_{P_{i}}(Q_{j}) \rangle | Q_{j} \in Q \}, \quad i = 1, 2, ..., n$$
(5)

where $\mu_{P_i}(Q_j)$ indicates the degree that the alternative P_i satisfies the attributes Q_j , $\vartheta_{P_i}(Q_j)$ indicates the degree that the alternative P_i does not satisfy the attribute Q_j , and $\mu_{P_i}(Q_j) \in [0,1]$, $\vartheta_{P_i}(Q_j) \in [0,1]$,

 $\mu_{P_i}(Q_i) + \vartheta_{P_i}(Q_i) \le 1$ (6)

Let $r'_{ii} = (k_{ij}, l_{ij})$ denote the characteristic of the alternative P_i with respect to the attribute Q_j , where k_{ij} indicates the degree that the alternative P_i satisfies the attribute Q_j , and l_{ij} indicates the degree that the alternative P_i does not satisfy the attribute Q_i . Therefore, the characteristics of all the alternatives P_i (i = 1, 2, ..., n) with respect to the attributes Q_i (j = 1, 2, ..., m) can be contained in an intuitionistic fuzzy decision matrix $R' = (r'_{ij})_{n \times m}$ where $r'_{ij} = (k_{ij}, l_{ij}), k_{ij} \in [0,1], l_{ij} \in [0,1]$ and $k_{ij} + l_{ij} \leq 1$.

	Q_1	Q_2		Q_m				
P_1	(k_{11}, l_{11})	(k_{12}, l_{12})		(k_{1m}, l_{1m})				
P_2	(k_{21}, l_{21})	(k_{22}, l_{22})		(k_{2m}, l_{2m})				
:	:			•••				
P_n	(k_{n1}, l_{n1})	(k_{n2}, l_{n2})		(k_{nm}, l_{nm})				

Table-1: Intuitionistic fuzzy decision matrix *R*[']

If all the attributes Q_j (j = 1, 2, ..., m) are of the same type, then the attribute values do not need normalization. However, there are generally benefit attributes (the bigger the attribute values the better) and cost attributes (the smaller the attribute values the better) in multi-attribute decision making. In such cases, we may transform the attribute values of cost type into the attribute values of benefit type then $R' = (r'_{ij})_{n \times m}$ can be transformed into the intuitionistic fuzzy decision matrix $R = (r_{ij})_{n \times m}$,

where

whe

$$r_{ij} = (\mu_{ij}, \vartheta_{ij}) = \begin{cases} r'_{ij}, \text{ for benifit attribute } Q_j, \\ \bar{r}'_{ij}, \text{ for cost attribute } Q_j, i = 1, 2, ... n \end{cases}$$

$$re \bar{r}'_{ij} \text{ is the complement of } r'_{ij}, \text{ such that } \bar{r}'_{ij} = (l_{ij}, k_{ij}).$$

$$(7)$$

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4. MATHEMATICAL MODEL OF INTUITIONISTIC FUZZY ASSIGNMENT PROBLEM

An assignment problem is a special type of transportion problem which can be stated in the form of $n \times n$ cost matrix $[\tilde{c}_{ii}]$ of intuitionistic fuzzy numbers as follows:

Job				
Group	1	2		n
1	\tilde{c}_{11}	\tilde{c}_{12}		\tilde{c}_{1n}
2	\tilde{c}_{21}	<i>Ĉ</i> 22		\tilde{c}_{2n}
:	:	:	:	:
n	\tilde{c}_{n1}	\tilde{c}_{n2}		\tilde{c}_{nn}

Table-2: Cost matrix of an assignment problem

The objective is to assign a number of origins to an equal number of destinations at a minimum cost or maximum profit. Each job must be done by exactly one group and one group can do, at most one job. Mathematically assignment problem can be denoted as

$$Min Z = \sum_{i=1}^{n} \sum_{j=1}^{n} \tilde{c}_{ij} x_{ij}$$

subject to
$$\sum_{j=1}^{n} x_{ij} = 1, \ i = 1, 2, ..., n$$
(8)
$$\sum_{i=1}^{n} x_{ii} = 1, \ j = 1, 2, ..., n$$
(9)

 $\begin{aligned} \sum_{i=1}^{j} x_{ij} &= 1, j = 1, 2, ..., n \end{aligned}$ where x_{ij} is the decision variable defined as $x_{ij} = \begin{cases} 1, if \ the \ i^{th} \ group \ is \ assigned \ to \ the \ j^{th} \ job; \ where \ i, j = 1, 2, ..., n. \end{cases}$ (5)

The cost of a group *i* doing the job *j* is considered as an intuitionistic fuzzy number $\tilde{c}_{ij} = \{(\mu_{ij}, \vartheta_{ij}), i, j = 1, 2, ..., n\}$ where μ_{ij} denotes the degree of acceptance and ϑ_{ij} denotes the degree of rejection.

As our objective is to minimize the cost and maximize the profit, we should go for maximize the acceptance degree μ_{ii} .

Then the objective function becomes a multi-objective function as $Max \ z_1 = \sum_{i=1}^n \sum_{j=1}^n \mu_{ij} \ x_{ij}$ and $Min \ z_2 = \sum_{i=1}^n \sum_{j=1}^n \vartheta_{ij} \ x_{ij}$

subject to
$$(\mu_{ij} + \vartheta_{ij} - 1)x_{ij} \le 0$$
 (10)

 $\mu_{ij} x_{ij} \ge \vartheta_{ij} x_{ij} \tag{11}$

$$\partial_{ij} x_{ij} \ge 0 \tag{12}$$

Thus the model becomes $\max Z = \sum_{i=1}^{n} \sum_{j=1}^{n} (\mu_{ij} - \vartheta_{ij}) x_{ij}.$ subject to the conditions (8), (9), (10), (11) and (12).

5. SOLUTION PROCEDURE

Step-1: Identify the teams with members and jobs. Fix the number of persons (alternatives) in a team and fix characteristics (attributes) to develop ideal priorities to each job.

Step-2: Represent attributes of the alternatives by the IFNs in an intuitionistic fuzzy decision matrix $R' = (r'_{ij})_{n \times m}$

Step-3: Transform the attribute value of cost type of each job into attribute values of benefit type using equation (7) and represent the transformed matrix as $R = (r_{ij})_{n \times m}$

Step-4: Weight all the alternative values r_{ij} by the weight vector ω_j of the attributes and multiply these values by the coefficient values n and then get the weighted attribute values $n\omega_j r_{ij}$ and represent in an intuitionistic fuzzy decision matrix $\dot{R} = (n\omega_j r_{ij})_{n \times m}$

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Step-5: Utilize the IFHA operator $\dot{r}_i = IFHA_{\omega,\omega}$ $(r_{i1}, r_{i2}, ..., r_{im}), i = 1, 2, ..., n$ calculate the aggregated values of \dot{r}_i .

Step-6: Utilize equation (1) calculate the scores of \dot{r}_i (i = 1, 2, ..., n) and get the ideal priorities among persons of a team to each job according to the heirarchical score values. If two scores are equal we may use the accuracy function given in equation (2) to compare the two IFNs.

Step-7: If there is no breakdown find the maximum of acceptance and minimum of rejection of the cost to do each job by the persons of the teams. Assign these IFNs representing the cost in a matrix R_1 to a particular team to do a particular job.

Step-8: Find the score values of the entries of the matrix R_1 and represent in a matrix R_2 . Using Hungarian method or any other software find the assignment.

Step-9: If there exist a break down in a team with a particular person then the assignment will be affected. Replace the person corresponding to the break down from the pool whose priority is higher than the priority of the relieved person.

Step-10: Find the score values of the matrix R_1 and represent in a matrix R_2 . Using Hungarian method find the assignment.

6. ILLUSTRATIVE EXAMPLE

Let us consider five teams (alternatives) Y_i (i = 1, 2, ..., 5) to do five jobs. Each team consists of four skilled persons. By considering the following five attributes to decide the priorities of the persons in the team: w_1 : capacity, w_2 : performance, w_3 : cost to do job, w_4 : time management and w_5 : Experience. Assume that the characteristics of the alternatives Y_i (i = 1, 2, ..., 5) and the attribute values corresponding to the person of the teams are represented by the IFNs.

Team Y₁

a) Let us consider team Y_1 correspondings to job J_1 and it has four alternatives $P_i(i = 1,2,3,4)$ and five attributes $w_j (j = 1,2,...5)$. The weight vector of the attributes $\omega = (0.19, 0.16, 0.24, 0.21, 0.20)^T$. Assume that the characteristics of the alternatives $P_i (i = 1,2,3,4)$ are represented by the IFNs, as shown in the intuitionistic fuzzy decision matrix $R' = (r'_{ij})_{A \to E}$

	W_1	W_2	I_1	W3	W_A
P_1	(0.3, 0.5)	(0.5, 0.2)	(0.1, 0.4)	(0.4 ,0.2)	(0.6, 0.4)
P_2	(0.4 ,0.3)	(0.7 ,0.2)	(0.6 ,0.2)	(0.6 ,0.3)	(0.2 ,0.4)
P_3	(0.8 ,0.2)	(0.2 ,0.6)	(0.5,0.5)	(0.7 ,0.2)	(0.9, 0.0)
P_4	(0.1,0.2)	(0.3 ,0.2)	(0.1,0.8)	(0.6,0.1)	(0.3 ,0.3)
J_1 :	max(0.1, 0.6	5, 0.5, 0.1) =	0.6 and min	(0.4, 0.2, 0.5	,0.8) = 0.2

Table-3: Intuitionistic fuzzy decision matrix R'

Transform the attribute values of cost type in the attribute values of benefit type by using equation (7). Then $R' = (r_{ij})_{4\times 5}$ is transformed into $R = (r_{ij})_{4\times 5}$

	Table-4. Intultionistic fuzzy decision matrix R						
	w_1	<i>w</i> ₂	J_1	<i>W</i> ₃	w_4		
P_1	(0.3, 0.5)	(0.5, 0.2)	(0.4, 0.1)	(0.4 ,0.2)	(0.6, 0.4)		
P_2	(0.4 ,0.3)	(0.7 ,0.2)	(0.2 ,0.6)	(0.6 ,0.3)	(0.2 ,0.4)		
<i>P</i> ₃	(0.8 ,0.2)	(0.2 ,0.6)	(0.5 ,0.5)	(0.7 ,0.2)	(0.9 ,0.0)		
P_4	(0.1 ,0.2)	(0.3 ,0.2)	(0.8 ,0.1)	(0.6 ,0.1)	(0.3 ,0.3)		

Table-4: Intuitionistic fuzzy decision matrix R

To get the ideal priorities the following steps are followed:

First weight all the attribute values r_{ij} (i = 1,2,3,4; j = 1,2,...,5) by weight vector $\omega = (0.19, 0.16, 0.24, 0.21, 0.20)^T$ of the attributes w_j (j = 1,2,...,5) and multiply these values by the balancing coefficient m = 5, and then get the weighted attribute values $5\omega_j r_{ij}$ (i = 1,2,3,4; j = 1,2,...,5), as listed in the weighted intuitionistic fuzzy decision matrix $\dot{R} = (5\omega_i r_{ij})_{4\times5}$.

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From table 4 we utilize the operational laws (4) and (6) in section 2.4 to get weighted IFNs: $\dot{r}_{11} = (1 - (1 - 0.3)^{5 \times 0.19}, 0.5^{5 \times 0.19}) = (0.288, 0.518),$ $\dot{r}_{12} = (1 - (1 - 0.5)^{5 \times 0.16}, 0.2^{5 \times 0.16}) = (0.426, 0.276),$ $\dot{r}_{13} = (1 - (1 - 0.4)^{5 \times 0.24}, 0.1^{5 \times 0.24}) = (0.459, 0.064),$ $\dot{r}_{14} = (1 - (1 - 0.4)^{5 \times 0.21}, 0.2^{5 \times 0.21}) = (0.416, 0.185),$ $\dot{r}_{15} = (1 - (1 - 0.6)^{5 \times 0.20}, 0.4^{5 \times 0.20}) = (0.6, 0.4)$

Similarly \dot{r}_{2i} , \dot{r}_{3i} and \dot{r}_{4i} where j = 1, 2, ..., 5.

Table-5:	The weighted	intuitionistic fuzzy	decision	matrix R
		1		

	w_1	<i>w</i> ₂	J_1	<i>W</i> ₃	w_4
P_1	(0.288, 0.518)	(0.426, 0.276)	(0.459, 0.064)	(0.416 ,0.185)	(0.6, 0.4)
P_2	(0.385 ,0.319)	(0.619 ,0.276)	(0.235 ,0.542)	(0.618 ,0.283)	(0.2 ,0.4)
P_3	(0.784 ,0.217)	(0.164 ,0.665)	(0.565 ,0.436)	(0.718 ,0.185)	(0.9 ,0.0)
P_4	(0.096, 0.217)	(0.249 ,0.276)	(0.856, 0.064)	(0.618,0.09)	(0.3,0.3)

The scores of \dot{r}_{ij} (i = 1,2,3,4) and (j = 1,2,...,5) by equation (1) are $s(\dot{r}_{11}) = (0.288 - 0.518) = -0.23$, $s(\dot{r}_{12}) = (0.426 - 0.276) = 0.15$, $s(\dot{r}_{13}) = (0.459 - 0.064) = 0.395$, $s(\dot{r}_{14}) = (0.416 - 0.185) = 0.231$ and $s(\dot{r}_{15}) = (0.6 - 0.4) = 0.2$

since $s(\dot{r}_{13}) > s(\dot{r}_{14}) > s(\dot{r}_{15}) > s(\dot{r}_{12}) > s(\dot{r}_{11})$ we have $\dot{\alpha}_{\sigma(1)} = (0.459, 0.064), \, \dot{\alpha}_{\sigma(2)} = (0.416, 0.276), \, \dot{\alpha}_{\sigma(3)} = (0.6, 0.2)$ $\dot{\alpha}_{\sigma(4)} = (0.426, 0.276), \, \dot{\alpha}_{\sigma(5)} = (0.288, 0.518).$

Similarly we can calculate the values of other rows.

Let $\omega = (0.1117, 0.2365, 0.3036, 0.2365, 0.1117)^T$ be its weighting vector as derived by the normal distribution based method of Xu (2005). Utilize the IFHA operator (4) derive the overall attribute values \dot{r}_i (i = 1,2,3,4) of alternatives P_i (i = 1,2,3,4)

 $\dot{r}_{1} = (1 - (1 - 0.459)^{0.1117} \times (1 - 0.416)^{0.2365} \times (1 - 0.6)^{0.3036} \times (1 - 0.426)^{0.2365} \times (1 - 0.288)^{0.1117}, 0.064^{0.1117} \times 0.276^{0.2365} \times 0.2^{0.3036} \times 0.276^{0.2365} \times 0.518^{0.1117}) = (0.474, 0.256).$

We obtained $\dot{r}_1 = (0.474, 0.256), \dot{r}_2 = (0.432, 0.342), \dot{r}_3 = (0.705, 0), \dot{r}_4 = (0.468, 0.18)$

The scores of \dot{r}_i (i = 1,2,3,4) by equation (1) are $s(\dot{r}_1) = 0.474 - 0.256 = 0.218$, $s(\dot{r}_2) = 0.432 - 0.342 = 0.09$, $s(\dot{r}_3) = 0.705 - 0 = 0.705$ and $s(\dot{r}_4) = 0.468 - 0.18 = 0.288$.

Since $s(\dot{r}_3) > s(\dot{r}_4) > s(\dot{r}_1) > s(\dot{r}_2)$, we represent the ideal priorities of the persons of team Y_1 corresponding to job J_1 as $P_3 > P_4 > P_1 > P_2$.

b) Consider the cost values of the persons of the team Y_1 to the job J_2 as $P_1: (0.1, 0.3), P_2: (0.4, 0.3), P_3: (0.3, 0.6)$ and $P_4: (0.1, 0.5)$ and the remaining values of attributes are as in Table 3. The ideal priorities of the persons of team Y_1 corresponding to job J_2 represented by $P_3 > P_4 > P_1 > P_2$.

c) Consider the cost values of the person of the team Y_1 to the job J_3 as $P_1: (0.7, 0.2), P_2: (0.5, 0.4), P_3: (0.6, 0.3)$ and $P_4: (0.2, 0.6)$ and the remaining values of attributes are as in Table 3. The ideal priorities of the persons of team Y_1 corresponding to job J_3 represented by $P_3 > P_4 > P_2 > P_1$.

d) Consider the cost values of the person of the team Y_1 to the job J_4 as $P_1: (0.1, 0.5), P_2: (0.9, 0.1), P_3: (0.7, 0.1)$ and $P_4: (0.4, 0.3)$ and the remaining values of attributes are as in Table 3. The ideal priorities of the persons of team Y_1 corresponding to job J_4 represented by $P_3 > P_1 > P_4 > P_2$.

e) Consider the cost values of the person of the team Y_1 to the job J_5 as $P_1: (0.2, 0.5), P_2: (0.4, 0.6), P_3: (0.1, 0.7)$ and $P_4: (0.3, 0.4)$ and the remaining values of attributes are as in Table 3. The ideal priorities of the persons of team Y_1 corresponding to job J_5 represented by $P_3 > P_2 > P_1 > P_4$.

Team Y₂

a) Let us consider team Y_2 correspondings to job J_1 and it has four alternatives $P_i(i = 1,2,3,4)$ and five attributes $w_j (j = 1,2,...5)$. The weight vector of the attributes $\omega = (0.15, 0.19, 0.18, 0.26, 0.22)^T$. Assume that the characteristics of the alternatives $P_i (i = 1,2,3,4)$ are represented by the IFNs, as shown in the intuitionistic fuzzy decision matrix $R' = (r'_{ij})_{a < 5}$.

	w_1	<i>w</i> ₂	J_1	<i>W</i> ₃	W_4
P_1	(0.4, 0.2)	(0.7, 0.1)	(0.3, 0.4)	(0.1,0.6)	(0.1, 0.8)
<i>P</i> ₂	(0.3 ,0.5)	(0.2 ,0.6)	(0.6 ,0.1)	(0.2 ,0.4)	(0.2 ,0.6)
<i>P</i> ₃	(0.1 ,0.7)	(0.1 ,0.8)	(0.2 ,0.5)	(0.5,0.4)	(0.7 ,0.3)
P_4	(0.6 ,0.3)	(0.5 ,0.3)	(0.4 ,0.5)	(0.3 ,0.5)	(0.8 ,0.1)

Table-6: Intuitionistic fuzzy decision matrix R'

 J_1 : max(0.3, 0.6, 0.2, 0.5) = 0.6 and min(0.4, 0.1, 0.5, 0.5) = 0.1

Following similar process of team Y_1 we get the ideal priorities of the persons of team Y_2 corresponding to job J_1 represented by $P_4 > P_3 > P_1 > P_2$.

b) Consider the cost values of the persons of the team Y_2 to the job J_2 as $P_1: (0.5, 0.3), P_2: (0.2, 0.6), P_3: (0.4, 0.6)$ and $P_4: (0.1, 0.8)$ and the remaining values of attributes are as in Table 6. The ideal priorities of the persons of team Y_2 corresponding to job J_2 represented by $P_4 > P_3 > P_1 > P_2$.

c) Consider the cost values of the person of the team Y_2 to the job J_3 as $P_1: (0.9, 0.1), P_2: (0.5, 0.4), P_3: (0.6, 0.3)$ and $P_4: (0.4, 0.5)$ and the remaining values of attributes are as in Table 6. The ideal priorities of the persons of team Y_2 corresponding to job J_3 represented by $P_4 > P_3 > P_1 > P_2$.

d) Consider the cost values of the person of the team Y_2 to the job J_4 as $P_1: (0.6, 0.4), P_2: (0.2, 0.3), P_3: (0.3, 0.6)$ and $P_4: (0.4, 0.5)$ and the remaining values of attributes are as in Table 6. The ideal priorities of the persons of team Y_2 corresponding to job J_4 represented by $P_4 > P_3 > P_1 > P_2$.

e) Consider the cost values of the person of the team Y_2 to the job J_5 as $P_1: (0.3, 0.6), P_2: (0.3, 0.4), P_3: (0.4, 0.2)$ and $P_4: (0.2, 0.7)$ and the remaining values of attributes are as in Table 6. The ideal priorities of the persons of team Y_2 corresponding to job J_5 represented by $P_4 > P_1 > P_3 > P_2$.

Team Y₃

a) Let us consider team Y_3 correspondings to job J_1 and it has four alternatives $P_i(i = 1,2,3,4)$ and five attributes $w_j (j = 1,2,...5)$. The weight vector of the attributes $\omega = (0.18, 0.23, 0.17, 0.22, 0.20)^T$. Assume that the characteristics of the alternatives $P_i (i = 1,2,3,4)$ are represented by the IFNs, as shown in the intuitionistic fuzzy decision matrix $R' = (r'_{ij})_{A < c}$.

	<i>w</i> ₁	<i>w</i> ₂	J_1	<i>W</i> ₃	W_4
P_1	(0.6, 0.2)	(0.3, 0.5)	(0.6, 0.4)	(0.1 ,0.7)	(0.8, 0.1)
<i>P</i> ₂	(0.2 ,0.7)	(0.4 ,0.3)	(0.7 ,0.3)	(0.3 ,0.4)	(0.1 ,0.2)
P_3	(0.4 ,0.5)	(0.3 ,0.6)	(0.1 ,0.9)	(0.5,0.1)	(0.4 ,0.4)
P_4	(0.5,0.4)	(0.7,0.1)	(0.2, 0.1)	(0.2, 0.3)	(0.3 ,0.4)

Table-7: Intuitionistic fuzzy decision matrix R'

 J_1 : max(0.6, 0.7, 0.1, 0.2) = 0.7 and min(0.4, 0.3, 0.9, 0.1) = 0.1

Following similar process of the team Y_1 we get the ideal priorities of the persons of team Y_3 corresponding to job J_1 as $P_3 > P_4 > P_1 > P_2$.

b) Consider the cost values of the person of the team Y_3 to the job J_2 as $P_1: (0.1, 0.2), P_2: (0.3, 0.5), P_3: (0.6, 0.3)$ and $P_4: (0.7, 0.1)$ and the remaining values of attributes are as in Table 7. The ideal priorities of the persons of team Y_3 corresponding to job J_2 represented by $P_1 > P_4 > P_2 > P_3$.

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c) Consider the cost values of the person of the team Y_3 to the job J_3 as $P_1: (0.4, 0.6), P_2: (0.5, 0.4), P_3: (0.7, 0.1)$ and $P_4: (0.2, 0.7)$ and the remaining values of attributes are as in Table 7. The ideal priorities of the persons of team Y_3 corresponding to job J_3 represented by $P_4 > P_3 > P_1 > P_2$.

d) Consider the cost values of the person of the team Y_3 to the job J_4 as $P_1: (0.7, 0.2), P_2: (0.3, 0.6), P_3: (0.5, 0.4)$ and $P_4: (0.6, 0.3)$ and the remaining values of attributes are as in Table 7. The ideal priorities of the persons of team Y_3 corresponding to job J_4 represented by $P_4 > P_1 > P_2 > P_3$.

e) Consider the cost values of the person of the team Y_3 to the job J_5 as $P_1: (0.3, 0.7), P_2: (0.4, 0.3), P_3: (0.7, 0.2)$ and $P_4: (0.5, 0.4)$ and the remaining values of attributes are as in Table 7. The ideal priorities of the persons of team Y_3 corresponding to job J_5 represented by $P_1 > P_4 > P_3 > P_2$.

Team Y₄

a) Let us consider team Y_4 correspondings to job J_1 and it has four alternatives $P_i(i = 1,2,3,4)$ and five attributes $w_j (j = 1,2,...5)$. The weight vector of the attributes $\omega = (0.16, 0.21, 0.19, 0.27, 0.17)^T$. Assume that the characteristics of the alternatives $P_i (i = 1,2,3,4)$ are represented by the IFNs, as shown in the intuitionistic fuzzy decision matrix $R' = (r'_{ij})_{A < c}$.

	<i>w</i> ₁	<i>w</i> ₂	J_1	<i>w</i> ₃	w_4
P_1	(0.1, 0.2)	(0.2, 0.3)	(0.9, 0.1)	(0.4 ,0.6)	(0.6, 0.3)
<i>P</i> ₂	(0.2 ,0.4)	(0.5 ,0.2)	(0.6 ,0.3)	(0.3 ,0.5)	(0.7 ,0.2)
P_3	(0.6 ,0.3)	(0.4 ,0.5)	(0.1 ,0.4)	(0.2 ,0.7)	(0.2 ,0.8)
P_4	(0.4 ,0.6)	(0.3 ,0.7)	(0.2 ,0.5)	(0.5,0.4)	(0.5, 0.3)

Table-8: Intuitionistic fuzzy decision matrix *R*[']

 J_1 : max(0.9, 0.6, 0.1, 0.2) = 0.9 and min(0.1, 0.3, 0.4, 0.5) = 0.1

Following similar process of the team Y_1 we get the ideal priorities of the persons of team Y_4 corresponding to job J_1 as $P_2 > P_4 > P_3 > P_1$.

b) Consider the cost values of the person of the team Y_4 to the job J_2 as $P_1: (0.1, 0.3), P_2: (0.4, 0.5), P_3: (0.6, 0.2)$ and $P_4: (0.9, 0.1)$ and the remaining values of attributes are as in Table 8. The ideal priorities of the persons of team Y_4 corresponding to job J_2 represented by $P_2 > P_1 > P_4 > P_3$.

c) Consider the cost values of the person of the team Y_4 to the job J_3 as $P_1: (0.4, 0.3), P_2: (0.7, 0.1), P_3: (0.1, 0.4)$ and $P_4: (0.3, 0.5)$ and the remaining values of attributes are as in Table 8. The ideal priorities of the persons of team Y_4 corresponding to job J_3 represented by $P_2 > P_4 > P_1 > P_3$.

d) Consider the cost values of the person of the team Y_4 to the job J_4 as $P_1: (0.7, 0.2), P_2: (0.8, 0.1), P_3: (0.2, 0.5)$ and $P_4: (0.4, 0.6)$ and the remaining values of attributes are as in Table 8. The ideal priorities of the persons of team Y_4 corresponding to job J_4 represented by $P_2 > P_4 > P_1 > P_3$.

e) Consider the cost values of the person of the team Y_4 to the job J_5 as $P_1: (0.6, 0.1), P_2: (0.3, 0.4), P_3: (0.5, 0.3)$ and $P_4: (0.1, 0.9)$ and the remaining values of attributes are as in Table 8. The ideal priorities of the persons of team Y_4 corresponding to job J_5 represented by $P_4 > P_2 > P_3 > P_1$.

Team Y₅

a) Let us consider team Y_5 correspondings to job J_1 and it has four alternatives $P_i(i = 1,2,3,4)$ and five attributes $w_j (j = 1,2,...5)$. The weight vector of the attributes $\omega = (0.15, 0.22, 0.21, 0.26, 0.16)^T$. Assume that the characteristics of the alternatives $P_i (i = 1,2,3,4)$ are represented by the IFNs, as shown in the intuitionistic fuzzy decision matrix $R' = (r'_{ij})_{A \to C}$.

	w_1	<i>w</i> ₂	J_1	<i>W</i> ₃	w_4
P_1	(0.5, 0.4)	(0.3, 0.7)	(0.1, 0.7)	(0.6, 0.2)	(0.1, 0.4)
P_2	(0.4,0.5)	(0.5,0.3)	(0.4 ,0.6)	(0.9, 0.1)	(0.7, 0.2)
P_3	(0.7,0.1)	(0.2, 0.4)	(0.3,0.4)	(0.5, 0.2)	(0.6, 0.1)
P_4	(0.3,0.6)	(0.1,0.2)	(0.5, 0.5)	(0.4 ,0.6)	(0.2, 0.3)

Table-9: Intuitionistic fuzzy decision matrix R'

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 J_1 : max(0.1, 0.4, 0.3, 0.5) = 0.5 and min(0.7, 0.6, 0.4, 0.5) = 0.4

Following similar process of the team Y_1 we get the ideal priorities of the persons of team Y_5 corresponding to job J_1 as $P_2 > P_3 > P_1 > P_4$.

b) Consider the cost values of the person of the team Y_5 to the job J_2 as $P_1: (0.9, 0.1), P_2: (0.4, 0.6), P_3: (0.7, 0.2)$ and $P_4: (0.1, 0.4)$ and the remaining values of attributes are as in Table 9. The ideal priorities of the persons of team Y_5 corresponding to job J_2 represented by $P_2 > P_3 > P_4 > P_1$.

c) Consider the cost values of the person of the team Y_5 to the job J_3 as $P_1: (0.3, 0.6), P_2: (0.5, 0.2), P_3: (0.6, 0.3)$ and $P_4: (0.2, 0.5)$ and the remaining values of attributes are as in Table 9. The ideal priorities of the persons of team Y_5 corresponding to job J_3 represented by $P_2 > P_3 > P_1 > P_4$.

d) Consider the cost values of the person of the team Y_5 to the job J_4 as $P_1: (0.2, 0.4), P_2: (0.3, 0.6), P_3: (0.8, 0.1)$ and $P_4: (0.7, 0.2)$ and the remaining values of attributes are as in Table 9. The ideal priorities of the persons of team Y_5 corresponding to job J_4 represented by $P_2 > P_3 > P_1 > P_4$.

e) Consider the cost values of the person of the team Y_5 to the job J_5 as $P_1: (0.4, 0.1), P_2: (0.2, 0.5), P_3: (0.5, 0.4)$ and $P_4: (0.8, 0.1)$ and the remaining values of attributes are as in Table 9. The ideal priorities of the persons of team Y_5 corresponding to job J_5 represented by $P_2 > P_3 > P_1 > P_4$.

Team pool Y₆

a) Let us consider team Y_6 correspondings to job J_1 and it has four alternatives $P_i(i = 1,2,3,4)$ and five attributes $w_j (j = 1,2,...5)$. The weight vector of the attributes $\omega = (0.17, 0.21, 0.23, 0.24, 0.15)^T$. Assume that the characteristics of the alternatives $P_i (i = 1,2,3,4)$ are represented by the IFNs, as shown in the intuitionistic fuzzy decision matrix $R' = (r_{ij}')_{4\times 5}$.

	<i>w</i> ₁	<i>w</i> ₂	J_1	<i>W</i> ₃	w_4
P_1	(0.3, 0.4)	(0.7, 0.1)	(0.4, 0.4)	(0.8, 0.2)	(0.4 ,0.5)
<i>P</i> ₂	(0.5 ,0.3)	(0.5 ,0.2)	(0.1 ,0.7)	(0.6, 0.1)	(0.6 ,0.2)
<i>P</i> ₃	(0.4 ,0.5)	(0.6 ,0.1)	(0.1,0.5)	(0.6, 0.2)	(0.7 ,0.3)
P_4	(0.3,0.4)	(0.4 ,0.2)	(0.1,0.8)	(0.8,0.1)	(0.3 ,0.4)

Table-10: Intuitionistic fuzzy decision matrix R'

 J_1 : max(0.4, 0.1, 0.1, 0.1) = 0.4 and min(0.4, 0.7, 0.5, 0.8) = 0.4

Following similar process of the team Y_1 we get the ideal priorities of the persons of team Y_6 corresponding to job J_1 as $P_2 > P_4 > P_3 > P_1$.

b) Consider the cost values of the person of the team Y_6 to the job J_2 as $P_1: (0.2, 0.5), P_2: (0.2, 0.7), P_3: (0.1, 0.8)$ and $P_4: (0.1, 0.7)$ and the remaining values of attributes as in Table 10. The ideal priorities of the persons of team Y_6 corresponding to job J_2 represented by $P_3 > P_2 > P_1 > P_4$.

c) Consider the cost values of the person of the team Y_6 to the job J_3 as $P_1: (0.5, 0.1), P_2: (0.6, 0.3), P_3: (0.5, 0.4)$ and $P_4: (0.5, 0.2)$ and the remaining values of attributes are as in Table 10. The ideal priorities of the persons of team Y_6 corresponding to job J_3 represented by $P_3 > P_2 > P_1 > P_4$.

d) Consider the cost values of the person of the team Y_6 to the job J_4 as $P_1: (0.4, 0.5), P_2: (0.3, 0.4), P_3: (0.2, 0.3)$ and $P_4: (0.1, 0.7)$ and the remaining values of attributes are as in Table 10. The ideal priorities of the persons of team Y_6 corresponding to job J_4 represented by $P_4 > P_1 > P_3 > P_2$.

e) Consider the cost values of the person of the team Y_6 to the job J_5 as $P_1: (0.3, 0.5), P_2: (0.6, 0.4), P_3: (0.3, 0.6)$ and $P_4: (0.1, 0.8)$ and the remaining values of attributes are as in Table 10. The ideal priorities of the persons of team Y_6 corresponding to job J_5 represented by $P_4 > P_3 > P_1 > P_2$.

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Final Table

	J_1	J_2	J_3	J_4	J_5
<i>Y</i> ₁	(0.6,0.2)	(0.4,0.3)	(0.7,0.2)	(0.9,0.1)	(0.4,0.4)
<i>Y</i> ₂	(0.6,0.1)	(0.5,0.3)	(0.9,0.1)	(0.6,0.3)	(0.4,0.2)
<i>Y</i> ₃	(0.7,0.1)	(0.7,01)	(0.7,0.1)	(0.7,0.2)	(0.7,0.2)
<i>Y</i> ₄	(0.9,0.1)	(0.9,0.1)	(0.7,0.1)	(0.8,0.1)	(0.6,0.1)
Y_5	(0.5,0.4)	(0.9,0.1)	(0.6,0.2)	(0.8,0.1)	(0.8,0.1)

Table-11: *R*₁: Cost matrix of the teams corresponding to jobs

Suppose the person P_2 is absent the team Y_2 . Choose the person from the pool whose priority is higher than P_2 corresponding to job J_1 and replace the value of above said person in the team Y_2 with the place P_2 corresponding to job J_1 . Find the maximum of acceptance and minimum of rejection of the cost to do job J_1 by the person of the team Y_2 . Put the value in the table R_1 with respect to the team Y_2 corresponding to the job J_1 . Similarly we do for other values of J_2, J_3, J_4 and J_5 by the team Y_2 . Suppose more than one person are absent replacement is made above.

Table-12: After break down the cost matrix R_1

	J_1	J_2	J_3	J_4	J_5
<i>Y</i> ₁	(0.6,0.2)	(0.4,0.3)	(0.7,0.2)	(0.9,0.1)	(0.4,0.4)
<i>Y</i> ₂	(0.4,0.4)	(0.5,0.3)	(0.9,0.1)	(0.6,0.4)	(0.4,0.2)
<i>Y</i> ₃	(0.7,0.1)	(0.7,01)	(0.7,0.1)	(0.7,0.2)	(0.7,0.2)
Y_4	(0.9,0.1)	(0.9,0.1)	(0.7,0.1)	(0.8,0.1)	(0.6,0.1)
<i>Y</i> ₅	(0.5,0.4)	(0.9,0.1)	(0.6,0.2)	(0.8,0.1)	(0.8,0.1)

Utilizing equation (1) calculate the score matrix of R_1

Table-13: Score matrix of R_1									
	J_1	J_2	J_3	J_4	J_5				
<i>Y</i> ₁	0.4	0.1	0.5	0.8	0				
<i>Y</i> ₂	0	0.2	0.8	0.2	0.2				
<i>Y</i> ₃	0.6	0.6	0.6	0.5	0.5				
Y_4	0.8	0.8	0.6	0.7	0.5				
Y_5	0.1	0.8	0.4	0.7	0.7				

The table 13 is the cost matrix of the assignment problem in the maximization form and it can be solved by Hungarian method or by using any standard software.

The optimal assignment without break down is

- 1^{st} job is assigned to the 5^{th} team. 2^{nd} job is assigned to the 2^{nd} team. 3^{rd} job is assigned to the 4^{th} team. 4^{th} job is assigned to the 3^{rd} team.
- 5^{th} job is assigned to the 1^{st} team.

The optimal assignment after break down is

- 1^{st} job is assigned to the 2^{nd} team.
- 2^{nd} job is assigned to the 1^{st} team.
- 3^{rd} job is assigned to the 1^{-t} team. 4^{th} job is assigned to the 3^{rd} team. 5^{th} job is assigned to the 4^{th} team.

7. CONCLUSION

In this paper a new real life intuitionistic fuzzy assignment model with replacement is proposed. Two stages of solution procedure are discussed with intuitionistic fuzzy aggregation operators. By an example ideal priorities of the professionals of teams are found and replacement is made where it is necessary by means of the priorities to do the job in time.

REFERENCES

- 1. Aggarwal V, Tikekar V G, Hsu L F., Bottleneck assignment problems under categorization, Computers and Operation Research 13 (1986), 11 –26.
- Angelov P P., Optimization in an intuitionistic fuzzy environment, Fuzzy Sets and Systems 86 (1997), 299 306.
- 3. Atanassov K T., Intuitionistic fuzzy sets, Fuzzy Sets and Systems 20(1986), 87 96.
- 4. Balinski M L and Gomory R E., A primal method for the assignment and transportation problems, Management Science 10 (1967), 578 593.
- Burillo P, Bustince H, Mohedano V., Some definition of Intuitionistic Fuzzy Numbers, First Properties, In Proceedings of the 1st workshop on Fuzzy Based Expert Systems, D.Lakoy (Ed.) (1994), pp. 53-55.
- 6. Chen M S., On a fuzzy assignment problem, Tamkang Journal 22 (1985), 407–411.
- 7. Chen S M , Tan J M., Handling multicriteria fuzzy decision-making problems based on vague set theory , Fuzzy sets and Systems 67 (1994) , 163–172.
- 8. Hong D H, Choi C H., Multicriteria fuzzy decision-making problems based on vague set theory, Fuzzy Sets and Systems 114 (2000), 103–113.
- 9. Kuhn H W., The Hungarian method for the assignment and transportation problems, Naval Research Logistics Quartely 2 (1955), 83 97.
- 10. Lin Chi Jen, Wen Ue pyng., A labeling algorithm for the fuzzy assignment problem, Fuzzy Sets and Systems 142 (2004), 373 391.
- 11. Liu C J, and Gao X, Fuzzy weighted equilibrium multi objective assignment problem and genetic algorithm. Applied Mathematical Modelling 33 (2009), 3926 3935.
- 12. Long Sheng, Huang Li pu, Zhang., Solution method for Fuzzy Assignment Problem with Restriction of Qualification, Proceedings of the Sixth International Conference on Intelligent Systems Design and Applications (2006), (ISDA'06).
- 13. Mukherjee S, Basu K., Solving intuitionistic fuzzy assignment problem by using similarity measures and score Functions, International journal of pure and Applied Sciences and Technology, 2 (2011), pp 1 18
- 14. Mukherjee S, Basu K., Solution of a class of Intuitionistic Fuzzy Assignment Problem by using similarity measures. Knowledge Based Systems 27 (2012), 170 179.
- 15. Sakawa M, Nishizaki I, Uemura Y., Interactive fuzzy programming for two level linear and linear fractional production and assignment problems: a case study, European Journal on Operation Research 135 (2001), 142 157.
- 16. Votaw D F, Orden A., The personal assignment problem, symposium on linear inequalities and programming , Project SCOOP 10,US Air Force, Washington (1952), 155 163.
- 17. Xu Z S, Yager R R., Some geometric aggregation operators based on intuitionistic fuzzy sets, International Journal of General Systems 35 (2006), 417-433.
- 18. Xu Z S., An overview of methods for determining OWA weights. International Journal of Intelligent Systems, 20 (2005), 843-865.
- 19. Xu Z S., Intuitionistic fuzzy aggregation operators. IEEE transactions of Fuzzy Systems 15 (2007),1179–1187.
- 20. Yang L, Liu B., A multi objective fuzzy assignment problem New model and algorithm, IEEE International conference on Fuzzy Systems (2005), 551 556.
- 21. Zadeh L., A Fuzzy sets, Information and Control 8 (1965), 338–353.

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