



On τ_p^+ Generalized Closed Sets, τ_p^+ g regular and τ_p^+ g normal spaces

¹F. Nirmala Irudayam* and ²Sr. I. Arockiarani

¹Assistant Professor, Department of Mathematics (CA), Nirmala College for Women, Coimbatore, INDIA

²Associate Professor, Department of Mathematics, Nirmala College for Women, Coimbatore, INDIA

*E-mail: nirmalairudayam@ymail.com

(Received on: 02-08-11; Accepted on: 13-08-11)

ABSTRACT

In this paper we introduce two classes of spaces called τ_p^+ g regular and τ_p^+ g normal space. These classes arise as a combination of simple extension topology and pre open sets in (X, τ) . In the light of τ_p^+ g closed sets and τ_p^+ g open sets we study some of the properties of the newly introduced sets.

AMS classification: 54D10, 54D15, 54C08, 54C10.

Key words: τ_p^+ g regular, τ_p^+ g $-T_0$, τ_p^+ g $-R_0$, τ^+-T_2 space, τ_p^+ g irresolute, τ_p^+ g normal.

INTRODUCTION:

In 1963 Levine [2], started the study of generalized open sets with the introduction of semi-open sets. With this notion, the concept of g-regular and g-normal spaces were introduced and studied by Munshi [7]. Further Noiri and Popa [8] investigated the concepts introduced by Munshi[7]. In 2010 M.E.Abd El Monsef [1] have defined the notion of Bg – closed sets, gB – continuity and gB-irresolute map. In this paper we define a τ_p^+ generalized closed set and study its regularity and normality.

1. PRELIMINARIES:

Throughout this paper (X, τ) and (Y, σ) represent non-empty topological spaces on which no separation axioms are assumed unless explicitly stated and they are simply written as X and Y respectively. For a subset A of (X, τ) , the closure of A, the interior of A with respect to τ are denoted by $cl(A)$ and $int(A)$ respectively. The complement of A is denoted by A^c .

Before entering into our work we recall the following definitions.

Definition 1.1: A subset A of a topological space (X, τ) is called pre-open [6] if $A \subseteq intcl(A)$. The complement of pre-open set is called pre-closed.

Definition 1.2: A subset of a topological space (X, τ) is called g-closed [4] if $cl(A) \subseteq G$ whenever $A \subseteq G$ and G is open in (X, τ) . The complement of g-closed is called g-open.

Definition 1.3: Levine [3], in 1963 defined $\tau^+(B) = \{O \cup (O' \cap B) / O, O' \in \tau\}$ and called it the simple expansion of τ by B where $B \notin \tau$.

Definition 1.4: A map $f: X \rightarrow Y$ is called gc-irresolute [5] if $f^{-1}(F)$ is g-closed in X for every g closed set F in Y.

2. τ_p^+ GENERALIZED CLOSED SET:

Definition 2.1: A subset A of a topological space (X, τ) is said to be a τ_p^+ generalized closed (τ_p^+ g closed) if $\tau^+cl(A) \subseteq U$ whenever $A \subseteq U$ and U is pre-open in (X, τ) . Also $\tau^+cl(A) = \bigcap \{S \subseteq X / A \subseteq S \text{ and } S \text{ is closed in } \tau^+(B)\}$. The complement of τ_p^+ generalized closed is known as τ_p^+ generalized open in (X, τ) .

Corresponding author: ¹F. Nirmala Irudayam, *E-mail: nirmalairudayam@ymail.com

Example 2.2: Consider $X = \{a, b, c\}$ $\tau = \{X, \emptyset, \{a\}, \{b\}, \{a, b\}\}$. Let $B = \{c\}$ Here the τ_p^+ generalized closed sets are $\{X, \emptyset, \{a\}, \{b\}, \{c\}, \{a, b\}, \{a, c\}, \{b, c\}\}$.

Theorem 2.3: The union of two τ_p^+ g closed set is τ_p^+ g closed.

Proof: Let A and B be two τ_p^+ g closed sets.

Let U be a pre open set such that $A \cup B \subseteq U$. This implies $A \subseteq U$ and $B \subseteq U$.

Since A is τ_p^+ g closed set, we have $\tau^+ \text{cl}(A) \subseteq U$ also if B is τ_p^+ g closed set, we have $\tau^+ \text{cl}(B) \subseteq U$

ie) $\tau^+ \text{cl}(A) \cup \tau^+ \text{cl}(B) \subseteq U$

ie) $\tau^+ \text{cl}(A \cup B) \subseteq U$ whenever $A \cup B \subseteq U$ where U is pre open.

Hence union of two τ_p^+ g closed set is τ_p^+ g closed.

Definition 2.4: A subset A of a topological space (X, τ) is said to be a τ^+ generalized closed (τ^+ g closed) if $\tau^+ \text{cl}(A) \subseteq U$ whenever $A \subseteq U$ and U is open in (X, τ) .

Example 2.5: Consider $X = \{a, b, c\}$ $\tau = \{X, \emptyset, \{b\}, \{c\}, \{b, c\}\}$. Let $B = \{a, c\}$ Here the τ^+ generalized closed sets are $\{X, \emptyset, \{a\}, \{b\}, \{a, b\}, \{a, c\}\}$.

Proposition 2.6: Every closed set in $\tau^+(B)$ is τ_p^+ g closed set.

Proof: This is true by the definition of τ_p^+ g closed set.

Theorem 2.7: Every τ_p^+ g closed set is τ^+ g closed.

Proof: Obvious

Remark 2.8:

- (i) Every τ^+ g closed set need not be τ_p^+ g closed
- (ii) Every τ_p^+ g closed set need not be $\tau^+(B)$ closed.

Proof: Follows from the following example.

Example 2.9: Consider $X = \{a, b, c\}$ $\tau = \{X, \emptyset, \{a\}, \{a, b\}\}$. Let $B = \{c\}$ Here τ_p^+ generalized closed sets are $\{X, \emptyset, \{b\}, \{c\}, \{b, c\}, \{a, b\}\}$.

The τ^+ generalized closed sets are $\{X, \emptyset, \{b\}, \{c\}, \{a, b\}, \{a, c\}, \{b, c\}\}$.

Here $\{a, c\}$ is τ^+ g closed but neither $\tau^+(B)$ closed nor τ_p^+ g closed

3: τ_p^+ g REGULAR SPACES:

Definition 3.1: A subset A of a space is regular τ^+ -clopen if A is both τ^+ open and τ^+ closed.

Definition 3.2: A space (X, τ) is said to be τ_p^+ generalized regular (τ_p^+ g regular) if for every τ_p^+ g closed set F and a point $x \notin F$, there exist disjoint τ^+ open sets U and V such that $F \subseteq U$ and $x \in V$.

Theorem 3.3: For a topological space, the following are equivalent.

- (i) (X, τ) is τ_p^+ g regular.
- (ii) Every τ_p^+ g open set U is a union of τ^+ regular sets.
- (iii) Every τ_p^+ g closed set A is a intersection of τ^+ regular sets.

Proof:

T.P (i) \Rightarrow (ii)

Let (X, τ) be τ_p^+ g regular. Let U be a τ_p^+ g open set and let $x \in U$. If $A = X \setminus U$, then A is τ_p^+ g closed. By assumption there exists disjoint τ^+ open subsets W_1 & W_2 of X such that $x \in W_1$ and $A \subseteq W_2$.

If $V = \tau^+ \text{cl}(W_1)$, then V is τ^+ closed and $V \cap A \subseteq V \cap W_2 = \emptyset$. It follows that $x \in V \subseteq U$.

Thus U is the union of τ^+ regular sets.

Hence (i) \Rightarrow (ii) and (ii) \Rightarrow (iii) is obvious.

T.P (iii) \Rightarrow (i) Let A be τ_p^+ g closed and $x \in A$. By assumption there exists a τ^+ regular set V such that $A \subseteq V$ and $x \notin V$.

If $U = X \setminus V$ then U is τ^+ open set containing x and $U \cap V = \emptyset$. Thus (X, τ) is τ_p^+ g regular. Hence the proof.

Now τ_p^+ g open sets give rise to various separation properties of which we have the following.

Definition 3.4: A topological space $((X, \tau))$ is said to be

- (i) τ_p^+ g - T_0 if for each pair of distinct points, there exists τ_p^+ g open set containing one point but not the other.
- (ii) τ_p^+ g - R_0 space if $\tau^+ \text{cl}\{x\} \subseteq U$ whenever U is τ_p^+ g open and $x \in U$.

Definition 3.5: A topological space is said to be τ^+ - T_2 if for each pair of the distinct points x and y in X , there exist disjoint τ^+ open sets U and V in X such that $x \in U$ and $y \in V$.

Theorem 3.6: Every τ_p^+ g regular space is both τ^+ - T_2 and τ_p^+ g - R_0 .

Proof: Let (X, τ) be τ_p^+ g regular space and let $x, y \in X$ such that $x \neq y$. By theorem 3.3 $\{x\}$ is either τ^+ open or τ^+ closed.

Since every space is τ^+ - T_2 If $\{x\}$ is τ^+ open, hence τ_p^+ g open.

Thus $\{x\}$ and $X \setminus \{x\}$ are separately τ^+ open sets. If $\{x\}$ is τ^+ closed then $X \setminus \{x\}$ is τ^+ open and by theorem 3.3 is the union of τ^+ regular sets. Hence there is a τ^+ regular set $V \subseteq X \setminus \{x\}$ containing y . This proves that (X, τ) is τ^+ - T_2 . By theorem 3.3 it follows immediately, that (X, τ) is also τ_p^+ g - R_0 .

Definition 3.7: The intersection of all τ_p^+ g closed set containing A is called the τ_p^+ g closure of A and denoted as $\tau_p^+ \text{g cl}(A)$. The characterization of $\tau_p^+ \text{g cl}(A)$ are as follows

Theorem 3.8: Let A be a subset of a space X and $x \in X$, then the following properties hold for of $\tau_p^+ \text{g cl}(A)$:

- (i) $x \in \tau_p^+ \text{g cl}(A)$ iff $A \cap U \neq \emptyset$, for every $U \in \tau^+ \mathcal{O}(X)$, containing x .
- (ii) A is τ_p^+ g closed iff $A = \tau_p^+ \text{g cl}(A)$
- (iii) $\tau_p^+ \text{g cl}(A)$ is τ^+ g closed.
- (iv) $\tau_p^+ \text{g cl}(A) \subseteq \tau_p^+ \text{g cl}(B)$ if $A \subseteq B$
- (v) $\tau_p^+ \text{g}(\tau_p^+ \text{g cl}(A)) = \tau_p^+ \text{g cl}(A)$

Proof: obvious.

Definition 3.9: A subset N of X is called τ_p^+ generalized neighbourhood (τ_p^+ g nbh) of a point $x \in X$, if there exists a τ_p^+ g open set U such that $x \in U \subseteq N$.

Theorem 3.10: Suppose that $B \subseteq A \subseteq X$, B is τ_p^+ g closed set relative to A and that A is open and τ_p^+ g closed in (X, τ) . Then B is τ_p^+ g closed in (X, τ) .

Theorem 3.11: If (X, τ) is a τ_p^+ g regular space and Y is an open and τ_p^+ g closed subset of (X, τ) , then the subspace Y is τ_p^+ g regular.

Proof: Let F be any τ_p^+ g closed subset of Y and $y \in F^c$. By above theorem 3.10, F is τ_p^+ g closed (X, τ) . Since (X, τ) is τ_p^+ g regular, there exists disjoint τ^+ open sets U and V of (X, τ) such that $y \in U$ and $F \subseteq V$. Since Y is open and hence τ^+ open we get $U \cap Y$ and $V \cap Y$ are disjoint τ^+ open sets of the subspace Y such that $y \in U \cap Y$ and $F \subseteq V \cap Y$. Hence the subspace Y is τ_p^+ g regular.

Theorem 3.12: Let (X, τ) be a topological space. Then the following statements are equivalent.

- (i) (X, τ) is τ_p^+ g regular

- (ii) For each point $x \in X$ and for each τ_p^+ g open nbh W of x , there exists a τ^+ open set U of X such that $\tau^+cl(U) \subseteq W$.
 (iii) For each point $x \in X$ and for each τ_p^+ g closed set F not containing x , there exists a τ^+ open set V of X such that $\tau^+cl(V) \cap F = \emptyset$.

Proof: To prove (i) \Rightarrow (ii). Let W be any τ_p^+ g open nbh of x . Then there exists a τ_p^+ g open set G such that $x \in G \subseteq W$. Since G^c is τ_p^+ g closed and $x \notin G^c$ by hypothesis, there exists τ^+ open sets U and V such that $G^c \in U$, $x \in V$ and $U \cap V = \emptyset$ and so $V \subseteq U^c$. Now $\tau^+cl(V) \subseteq \tau^+cl(U^c) = U^c$ and $G^c \subseteq U$ implies $U^c \subseteq G \subseteq W$. Thus $\tau^+cl(U) \subseteq W$.

To prove (ii) \Rightarrow (i). Let F be any τ_p^+ g closed set and $x \notin F$. Then $x \in F^c$ and F^c is a τ_p^+ g open set and so F^c is an τ_p^+ g open nbh of x . By hypothesis, there exists τ^+ open set V of x such that $x \in V$ and $\tau^+cl(V) \subseteq F^c$ which implies $F \subseteq (\tau^+cl(V))^c$.

Then $(\tau^+cl(V))^c$ is τ^+ open containing F and $V \cap (\tau^+cl(V))^c = \emptyset$. Therefore X is τ_p^+ g regular.

To prove (ii) \Rightarrow (iii). Let $x \in X$ and F be a τ_p^+ g closed set such that $x \notin F$. Then F^c is a τ_p^+ g nbhd of x and by hypothesis, there exists a τ^+ open set V of X such that $\tau^+cl(V) \subseteq F^c$ and hence $\tau^+cl(V) \cap F = \emptyset$.

To prove (iii) \Rightarrow (ii). Let $x \in X$ and W be a τ_p^+ g nbhd of x . Then there exists a τ_p^+ g open set G such that $x \in G \subseteq W$. Since G^c is τ_p^+ g closed and $x \notin G^c$ by hypothesis, there exists τ^+ open set U of x such that $\tau^+cl(U) \cap G^c = \emptyset$. Therefore $\tau^+cl(U) \subseteq G \subseteq W$.

Theorem 3.13: A topological space (X, τ) is τ_p^+ g regular if and only if for each τ_p^+ g closed set F of (X, τ) and each $x \in F^c$, there exists τ^+ open sets U and V of (X, τ) such that $x \in U$ and $F \subseteq V$ and $\tau^+cl(U) \cap \tau^+cl(V) = \emptyset$.

Proof: Let F be any τ_p^+ g closed set and $x \notin F$. Then there exists a τ^+ open sets U_x and V such that $x \in U_x$, $F \subseteq V$ and $U_x \cap V = \emptyset$, which implies that $U_x \cap \tau^+cl(V) = \emptyset$. Since (X, τ) is τ_p^+ g regular, there exists τ^+ open sets G and H of (X, τ) such that $x \in G$, $\tau^+cl(V) \subseteq H$ and $G \cap H = \emptyset$. This implies $\tau^+cl(G) \cap H = \emptyset$.

Now let $U = U_x \cap G$, then U and V are τ^+ open sets of (X, τ) such that $x \in U$ and $F \subseteq V$ and $\tau^+cl(U) \cap \tau^+cl(V) = \emptyset$. The converse is straight forward.

Definition 3.14: A map $f: X \rightarrow Y$ is called $M \tau^+$ open if $f(V)$ is τ^+ open set in Y for every τ^+ open set V of X .

Definition 3.15: A map $f: X \rightarrow Y$ is called τ_p^+ g irresolute (resp. τ^+ irresolute) if $f^{-1}(V)$ is τ_p^+ g open (resp. τ^+ open) set in X for every τ_p^+ g open (resp. τ^+ open) set V of Y .

Theorem 3.16: If (X, τ) is τ_p^+ g regular space and if $f: (X, \tau) \rightarrow (Y, \sigma)$ is bijective, τ_p^+ g irresolute and $M \tau^+$ open, then (Y, σ) is τ_p^+ g regular.

Proof: Let $y \in Y$ and F be any τ_p^+ g closed set of (Y, σ) with $y \notin F$. Since f is τ_p^+ g irresolute, $f^{-1}(F)$ is τ_p^+ g closed set in (X, τ) . Since f is bijective let $f(x) = y$, then $x \notin f^{-1}(y)$. By hypothesis, there exists τ^+ open sets U and V such that $x \in U$ and $f^{-1}(F) \subseteq V$. Since f is $M \tau^+$ open and bijective we have $y \in f(U)$ and $F \subseteq f(V)$ and $f(U) \cap f(V) = f(U \cap V) = \emptyset$. Hence (Y, σ) is τ_p^+ g regular space.

Theorem 3.17: If $f: (X, \tau) \rightarrow (Y, \sigma)$ is gc -irresolute, $M \tau^+$ closed and A is a τ_p^+ g closed subset of (X, τ) then $f(A)$ is τ_p^+ g closed.

Theorem 3.18: If $f: (X, \tau) \rightarrow (Y, \sigma)$ is gc -irresolute, $M \tau^+$ closed, injective and (Y, σ) is τ_p^+ g regular then (X, τ) is τ_p^+ g regular.

Proof: Let F be any τ_p^+ g closed set of (X, τ) and $x \notin F$. Since f is gc irresolute, $M \tau^+$ closed by theorem 3.17, $f(F)$ is τ^+ closed in Y and $f(x) \notin f(F)$. Since (Y, σ) is τ_p^+ g regular and so there exists disjoint τ^+ open sets U and V in (Y, σ) such that $f(x) \in U$ and $f(F) \subseteq V$. By hypothesis, $f^{-1}(U)$ and $f^{-1}(V) \in \tau^+O(X)$, such that $x \in f^{-1}(U)$ and $F \subseteq f^{-1}(V)$ and $f^{-1}(U) \cap f^{-1}(V) = \emptyset$. Therefore (X, τ) is τ_p^+ g regular.

4. τ_p^+ g NORMAL SPACES:

Here we introduce a weak form of normality called τ_p^+ g normality in a topological space.

Definition 4.1: A topological space (X, τ) is said to be τ_p^+ generalized normal (τ_p^+ g normal) if for any pair of disjoint τ_p^+ g closed sets A and B, there exists disjoint τ^+ open sets U and V such that $A \subseteq U$ and $B \subseteq V$.

Theorem 4.2: If (X, τ) is τ_p^+ g normal space and Y is an open and τ_p^+ g closed subset of (X, τ) , then the subspace Y is τ_p^+ g normal.

Proof: Let A and B be any two disjoint τ_p^+ g closed sets of Y. By Theorem 3.10, A and B are τ_p^+ g closed in (X, τ) . Since (X, τ) is τ_p^+ g normal, there exists disjoint τ^+ open sets U and V of (X, τ) such that $A \subseteq U$ and $B \subseteq V$. Since Y is open and hence τ^+ open, $U \cap Y$ and $V \cap Y$ are disjoint τ^+ open sets of the subspace Y. Hence the subspace Y is τ_p^+ g normal.

Theorem 4.3: Let (X, τ) be a topological space, then the following statements are equivalent.

- (1) (X, τ) is τ_p^+ g normal
- (2) For each τ_p^+ g closed set F and for τ_p^+ g open set U containing F, there exists a τ^+ open set V containing F such that $\tau^+cl(V) \subseteq U$.
- (3) For each pair of disjoint τ_p^+ g closed set A and B in (X, τ) , there exists a τ^+ open set containing A such that $\tau^+cl(U) \cap B = \emptyset$.
- (4) For each pair of disjoint τ_p^+ g closed set A and B in (X, τ) there exists τ^+ open sets U and V such that $A \subseteq U$ and $B \subseteq V$ and $\tau^+cl(A) \cap \tau^+cl(B) = \emptyset$.

To Prove: (1) \Rightarrow (2)

Let F be a τ_p^+ g closed set U be a τ_p^+ g open set such that $F \subseteq U$. Then $F \cap U^c = \emptyset$, by assumption, there exists τ^+ open set V and W such that $F \subseteq U$ and $U^c \subseteq W$ and $V \cap W = \emptyset \Rightarrow \tau^+cl(V) \cap W = \emptyset$. Now $\tau^+cl(V) \cap U^c \subseteq \tau^+cl(V) \cap W = \emptyset$ and so $\tau^+cl(V) \subseteq U$.

To Prove: (2) \Rightarrow (3)

Let A and B be disjoint τ_p^+ g closed sets of (X, τ) . Since $A \cap B = \emptyset$; $A \subseteq B^c$ and B^c is τ_p^+ g open. By assumption, there exists τ^+ open sets U containing A such that $\tau^+cl(U) \subseteq B^c$ and so $\tau^+cl(U) \cap B = \emptyset$.

To Prove: (3) \Rightarrow (4)

Let A and B be disjoint τ_p^+ g closed sets of (X, τ) . Then by assumption, there exists τ^+ open sets U containing A such that $\tau^+cl(U) \cap B = \emptyset$.

Since $\tau^+cl(A)$ is τ^+ closed, it is τ_p^+ g closed and so B and $\tau^+cl(A)$ are disjoint τ_p^+ g closed sets in (X, τ) .

Hence by assumption, there exists a τ^+ open sets V containing B such that $\tau^+cl(A) \cap \tau^+cl(B) = \emptyset$.

To Prove: (4) \Rightarrow (1)

Let A and B be disjoint τ_p^+ g closed sets of (X, τ) . By assumption, there exists τ^+ open sets U and V such that $A \subseteq U$ and $B \subseteq V$ and $\tau^+cl(U) \cap \tau^+cl(V) = \emptyset$. We have $U \cap V = \emptyset$ and thus (X, τ) is τ_p^+ g normal.

Theorem 4.4: If $f: (X, \tau) \rightarrow (Y, \sigma)$ is τ_p^+ g irresolute, bijective, $M\tau^+$ open mapping and (X, τ) is τ_p^+ g normal, then (Y, σ) is τ_p^+ g normal.

Proof: Let A and B be any two disjoint τ_p^+ g closed sets of (Y, σ) . Since f is τ_p^+ g irresolute, $f^{-1}(A)$ and $f^{-1}(B)$ are disjoint τ_p^+ g closed sets of (X, τ) . As (X, τ) is τ_p^+ g normal, there exists disjoint τ^+ open sets U and V such that $f^{-1}(A) \subseteq U$ and $f^{-1}(B) \subseteq V$. Since f is bijective and $M\tau^+$ open we have f(U) and f(V) are τ^+ open sets in (Y, σ) such that $A \subseteq f(U)$ and $B \subseteq f(V)$ and $f(U) \cap f(V) = \emptyset$. Therefore (Y, σ) is τ_p^+ g normal.

Theorem 4.5: If $f: (X, \tau) \rightarrow (Y, \sigma)$ is gc irresolute, $M\tau^+$ closed and τ^+ irresolute injection and (Y, σ) is τ_p^+ g normal, then (X, τ) is τ_p^+ g normal.

Proof: Let A and B be any two disjoint τ_p^+ g closed sets of (X, τ) . Since f is gc irresolute and $M\tau^+$ closed. $f(A)$ and $f(B)$ are disjoint τ_p^+ g closed sets of (Y, σ) .

By Theorem 3.17 since (Y, σ) is τ_p^+ g normal, there exists disjoint τ^+ open sets U and V such that $f(A) \subseteq U$ and $f(B) \subseteq V$ i.e.) $A \subseteq f^{-1}(U)$ and $B \subseteq f^{-1}(V)$ and $f^{-1}(U) \cap f^{-1}(V) = \emptyset$.

Since f is τ^+ irresolute, $f^{-1}(U)$ and $f^{-1}(V)$ are τ^+ open sets in (X, τ) , we have (X, τ) is τ_p^+ g normal.

REFERENCES:

- [1] M. E Abd El. Monsef, A. M. Kozae and R. A Abu- Gdairi, New approaches for generalized continuous functions, Int. Journal of Math. Analysis, Vol.4, 2010, 1329-1339.
- [2] N. Levine, Semi-open Sets and semi-continuity in topological Spaces, Amer. Math. Monthly, 70(1963), 36-41.
- [3] N. Levine, Simple extension of topologies, Amer. Math. Monthly, 71(1964), 22 -105.
- [4] N. Levine, Generalized Closed Sets in Topology, Rend. Circ. Mat. Palermo, 19(2) (1970) 89- 96.
- [5] H. Maki, P. Sundaram and K Balachandran, On Generalized Homeomorphisms in Topological Spaces, Bull. Fukuoka Univ. Ed. Part III, 40 (1991), 13- 21.
- [6] A. S. Mashhour, M. E. Abd El. Monsef and S N El- Deeb, On Precontinuous and Weak Precontinuous Mappings, Proc. Math. And Phys. Soc. Egypt, 53 (1982), 47 – 53.
- [7] B. M. Munshi, Separation Axioms, Act Cienica India, 12 (1986), 140 – 144.
- [8] T. Noiri and V. Popa, On g-regular Spaces and some functions, Mem. Fac. Sci. Kochi Univ, Ser. A. Math., 20 (1999), 67-74.
- [9] A. Vadivel, R. Vijayalakshmi and D. Krishnaswamy, B-Generalised Regular and B-Generalised Normal spaces, Int. Mathematical Forum, 5, 2010, 2699-2706.
