HEAT AND MASS TRANSFER IN RADIATIVE MHD FLUID FLOW OVER A PERMEABLE VERTICAL PLATE IN THE PRESENCE OF THE HEAT SOURCE

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ABSTRACT

Numerical investigation is carried out for analyzing the heat and mass transfer in radiative magneto hydrodynamics fluid flow over a permeable vertical plate in the presence of the heat source. The governing systems of partial differential equations are transformed to dimensionless equations using dimensionless variables. The dimensionless equations are solved numerically by using finite element method. With the help of graphs, the effects of the various important parameters entering into the problem on the dimensionless velocity, dimensionless temperature and dimensionless concentration fields within the boundary layer are discussed. Numerical values of friction factor, local Nusselt and Sherwood numbers are tabulated.

Key words: Heat and Mass transfer, MHD, Heat source, FEM.

1. INTRODUCTION

In many transport processes existing in nature and in industrial applications in which heat and mass transfer is a consequence of buoyancy effects caused by diffusion of heat and chemical species, the study of such processes is useful for improving a number of chemical technologies such as polymer production, enhanced oil recovery, underground energy transport, manufacturing of ceramics and food processing. Heat and mass transfer from different geometries embedded in porous media has many engineering and geophysical applications such as drying of porous solids, thermal insulations, and cooling of nuclear reactors. At high operating temperature, radiation effects can be quite significant. Many processes in engineering areas occur at high temperature and knowledge of radiation heat transfer becomes very important for the design of reliable equipment’s, nuclear plants, gas turbines and various propulsion devices or aircraft, missiles, satellites and space vehicles.

Ahmed et al. [1] analyzed the convective MHD oscillatory flow past a uniformly moving infinite vertical plate taking into account variable suction velocity and heat generation. The effects of Hall current on the fluid flow and heat transfer in rotating channels have many engineering applications inflows of laboratory plasmas, in MHD power generation, in MHD accelerators, and in several astrophysical and geophysical situations. Takhar et al. [2] extended the problem with variable suction and heat generation. Deka et al. [3] investigated the effect of first order homogeneous chemical reaction on the process of an unsteady flow past an infinite vertical plate with a constant heat and mass transfer. Muthucumaraswamy and Ganesan [4] discussed the effect of the chemical reaction and injection on flow characteristics in an unsteady upward motion of an isothermal plate. MHD flow of a uniformly stretched vertical permeable surface in the presence of heat generation/absorption and a chemical reaction has been considered by Chamkha [5]. Ibrahim et al. [6] obtained the analytical solution for unsteady MHD free convection flow past a semi – infinite vertical permeable moving plate with heat source and chemical reaction. Rahman et al. [7] studied heat transfer in micro polar fluid with temperature dependent fluid properties along a non – stretching sheet.

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Based on these applications, Cogley et al. [8] showed that in the optically thin limit, the fluid does not absorb its own emitted radiation but the fluid does absorb radiation emitted by the boundaries. Satter and Hamid [9] investigated the unsteady free convection interaction with thermal radiation in a boundary layer flow past a vertical porous plate. Vajravelu [10] studied the flow of a steady viscous fluid and heat transfer characteristic in a porous medium by considering different heating processes. Hossain and Takhar [11] have considered the radiation effect on mixed convection boundary layer flow of an optically dense viscous incompressible fluid along a vertical plate with uniform surface temperature. Raptis [12] investigate the steady flow of a viscous fluid through a porous medium bounded by a porous plate subjected to a constant suction velocity by the presence of thermal radiation. Makinde [13] examined the transient free convection interaction with thermal radiation of an absorbing emitting fluid along moving vertical permeable plate. The effect of the chemical reaction and radiation absorption on the unsteady MHD free convection flow past a semi – infinite vertical permeable moving plate with heat source and suction has been studied by Ibrahim et al. [14].


The object of the present work is to study the heat and mass transfer in radiative magneto hydrodynamics fluid flow over a permeable vertical plate in the presence of the heat source. Similarity transformation is used to transform the governing partial differential equations to ordinary differential equations which are then solved numerically by finite element method.

2. MATHEMATICAL FORMULATION

We consider the unsteady flow of an incompressible viscous, radiating hydro magnetic fluid past an infinite porous heated vertical plate with time – dependent suction in an optically thin environment. The physical model and the coordinate system are shown in figure 1.

"Figure-1: The physical model and coordinate system of the problem"

We made the following assumptions:

1. The $\chi'$ – axis is taken along the vertical infinite porous plate in the upward direction and the $y'$ – axis normal to the plate.

2. At time $\tau' = 0$, the plate is maintained at a temperature $T_w'$, which is high enough to initiate radiative heat transfer.

3. A constant magnetic field $H_0'$ is maintained in the $y'$ direction and the plate moves uniformly along the positive $\chi'$ direction with velocity $U_0$.

Under Boussinesq’s approximation the flow is governed by the following equations:

**Equation of Continuity:**

$$\frac{\partial w'}{\partial y'} = 0$$ (1)
Momentum Equation:
\[
\frac{\partial u'}{\partial t'} + w' \frac{\partial u'}{\partial y'} = \frac{\partial^2 u'}{\partial y'^2} + \frac{\partial U'}{\partial t'} - \left( \frac{\mu^2 \sigma_c H_0^2}{\rho} + \frac{v}{k} \right) (u' - U') + g\beta \left( T' - T_\infty' \right) + g\beta^* \left( C' - C'_\infty \right)
\]

Energy Equation:
\[
\frac{\partial T'}{\partial t'} + w' \frac{\partial T'}{\partial y'} = \frac{k}{\rho c_p} \left( \frac{\partial^2 T'}{\partial y'^2} - \nabla q_z' \right) - \frac{Q_p}{\rho c_p} (T' - T_\infty')
\]

Species Diffusion Equation:
\[
\frac{\partial C'}{\partial t'} + w' \frac{\partial C'}{\partial y'} = D \frac{\partial^2 C'}{\partial y'^2}
\]

The boundary conditions are
\[
\begin{align*}
    u' &= 0, \quad T' = T_w', \quad C' = C_w' \text{ on } y' = 0 \\
    u' &= U'(t') = w_0' \left( 1 + \varepsilon e^{i\omega t} \right), \quad T' = T_c', \quad C' = C_c' \text{ as } y' \to \infty
\end{align*}
\]

Since the medium is optically thin with relatively low density and \( \alpha << 1 \) the radiative heat flux given by equation (4) in the spirit of Cogley et al. [8] becomes
\[
\frac{\partial q_z'}{\partial y'} = 4\alpha^2 \left( T' - T_\infty' \right)
\]

Where \( \alpha^2 = \int_0^\infty \delta \lambda \frac{\partial B}{\partial T'} \frac{\partial T'}{\partial T'} \)

Here \( \lambda \) is a frequency.

Further, from equation (1) it is clear that \( w' \) is a constant or a function of time only and so we assume
\[
w' = -w_0' \left( 1 + \varepsilon A e^{i\omega t} \right)
\]

Such that \( \varepsilon A << 1 \), and the negative sign indicates that the suction velocity is towards the plate.

In view of equations (4), (8) and (9) equations (2), (3) and (5) become
\[
\begin{align*}
    \frac{1}{4} \frac{\partial u}{\partial t} &- \left( 1 + \varepsilon A e^{i\omega t} \right) \frac{\partial u}{\partial y} + \frac{1}{4} \frac{\partial U}{\partial t} + \frac{\partial^2 u}{\partial y^2} - (M^2)(u - U) + Gr\theta + GcC = 0 \\
    \frac{1}{4} \left( Pr \right) \frac{\partial \theta}{\partial t} &- \left( Pr \right) \left( 1 + \varepsilon A e^{i\omega t} \right) \frac{\partial \theta}{\partial y} = \left( \frac{\partial^2 \theta}{\partial y^2} - R^2 \right) \theta - \left( Pr \right) (S) \theta \\
    \frac{1}{4} \left( Sc \right) \frac{\partial C}{\partial t} &- \left( Sc \right) \left( 1 + \varepsilon A e^{i\omega t} \right) \frac{\partial C}{\partial y} = \frac{\partial^2 C}{\partial y^2} + \frac{\partial^2 C}{\partial y^2}
\end{align*}
\]

Where we have used the following dimensionless variables
\[
\begin{align*}
    t &= \frac{w_0'^2 t'}{4v}, \quad y = \frac{w_0' y'}{v}, \quad u = \frac{u'}{U_0}, \quad w = \frac{4w_0'}{w_0'^2}, \quad U = \frac{U'}{U_0}, \quad \theta = \frac{T' - T_\infty'}{T_w' - T_\infty'} \\
    Pr &= \frac{\mu c_p}{k}, \quad Gr = \frac{g\beta \nu (T_w' - T_\infty')}{U_0 w_0'^2}, \quad Gc = \frac{g\beta^* \nu (C_w' - C_\infty')}{U_0 w_0'^2}, \quad R^2 = \frac{4\alpha^2}{\rho c_p k w_0'^2} (T_w' - T_\infty'), \\
    S &= \frac{\nu Q_p}{\rho c_p w_0'^4}, \quad M^2 = \frac{\mu^2 \sigma_c H_0^2}{\rho w_0'^2}, \quad Sc = \frac{w_0'}{D}, \quad C = \frac{(C' - C_\infty')}{(C_w' - C_\infty')}
\end{align*}
\]
Equations (10), (11) and (12) are now subject to the boundary conditions

\[
\begin{align*}
    u &= 0, \quad \theta = 1, \quad C = 1 \quad \text{on} \quad y = 0 \\
    u &\rightarrow 1 + \varepsilon e^{\lambda t}, \quad \theta \rightarrow 0, \quad C \rightarrow 0 \quad \text{as} \quad y \rightarrow \infty
\end{align*}
\]

(14)

The skin friction, Nusselt number and Sherwood number are important physical parameters for this type of boundary layer flow. The skin friction at the plate, which in the non-dimensional form is given by

\[
\tau = \frac{\tau_w}{\rho U_o y} = \left( \frac{\partial u}{\partial y} \right)_{y=0} = \frac{\tau_w}{\rho U_o} \frac{1}{y}
\]

(15)

The rate of heat transfer coefficient, which in the non-dimensional form in terms of the Nusselt number is given by

\[
Nu = -x^i \left( \frac{\partial T'}{\partial y'} \right)_{y'=0} \Rightarrow Nu Re^{-1} = \left( \frac{\partial \theta}{\partial y} \right)_{y=0}
\]

(16)

The rate of mass transfer coefficient, which in the non-dimensional form in terms of the Sherwood number, is given by

\[
Sh = -x^i \left( \frac{\partial C'}{\partial y'} \right)_{y'=0} \Rightarrow Sh Re^{-1} = \left( \frac{\partial C}{\partial y} \right)_{y=0}
\]

(17)

Where \( Re = \frac{U_o x}{\nu} \) is the local Reynolds number.

The mathematical statement of the problem is now complete and embodies the solution of equations (10), (11) and (12) subject to boundary conditions (14).

3. Method of Solution

By applying Galerkin finite element method (Bathe [19] and Reddy [20]) for equation (10) over the element \((y_j \leq y \leq y_k)\) is:

\[
\int_{y_j}^{y_k} \left\{ N^{(e)T} \left[ 4 \frac{\partial^2 u^{(e)}}{\partial y^2} - \frac{\partial u^{(e)}}{\partial y} + 4B \frac{\partial u^{(e)}}{\partial y} - Du^{(e)} + P \right] \right\} dy = 0
\]

(18)

Where \( P = \frac{\partial U}{\partial t} + 4(Gr)\theta + 4(Ge)C + DU, \quad B = 1 + \varepsilon A e^{\lambda t}, \quad D = 4(M^2 + \chi^2) \);

Integrating the first term in equation (18) by parts one obtains

\[
4N^{(e)T} \left\{ \frac{\partial u^{(e)}}{\partial y} \right\} _{y_j}^{y_k} - \int_{y_j}^{y_k} \left\{ 4N^{(e)T} \frac{\partial u^{(e)}}{\partial y} + N^{(e)T} \left( \frac{\partial u^{(e)}}{\partial t} - 4B \frac{\partial u^{(e)}}{\partial y} + Du^{(e)} - P \right) \right\} dy = 0
\]

(19)

Neglecting the first term in equation (19), one gets:

\[
\int_{y_j}^{y_k} \left\{ 4N^{(e)T} \frac{\partial u^{(e)}}{\partial y} + N^{(e)T} \left( \frac{\partial u^{(e)}}{\partial t} - 4B \frac{\partial u^{(e)}}{\partial y} + Du^{(e)} - P \right) \right\} dy = 0
\]

Let \( u^{(e)} = N^{(e)} \phi^{(e)} \) be the linear piecewise approximation solution over the element \((e)(y_j \leq y \leq y_k)\) where

\[
N^{(e)} = \begin{bmatrix} N_j & N_k \end{bmatrix}, \quad \phi^{(e)} = \begin{bmatrix} u_j & u_k \end{bmatrix}^T \quad \text{and} \quad N_j = \frac{y_k - y}{y_k - y_j}, N_k = \frac{y - y_j}{y_k - y_j}
\]

are the basis functions. One obtains:
Applying the trapezoidal rule, following system of equations in Crank – Nicholson method are obtained:

\[
\begin{align*}
J \left[ \begin{array}{cc}
1 & -1 \\
-1 & 1 \\
0 & -1 \\
\end{array} \right] u_j + \frac{1}{6} \begin{array}{cc}
2 & 1 \\
1 & 4 \\
0 & 1 \\
\end{array} \begin{array}{c}
\cdot
\end{array} + \frac{4B}{2l}\begin{array}{c}
\cdot
\end{array} \left[ \begin{array}{c}
\cdot
\end{array} \\
\cdot
\end{array} - \frac{1}{6} \begin{array}{cc}
2 & 1 \\
1 & 4 \\
0 & 1 \\
\end{array} \begin{array}{c}
\cdot
\end{array} \left[ \begin{array}{c}
\cdot
\end{array} - \frac{1}{6} \begin{array}{cc}
2 & 1 \\
1 & 4 \\
0 & 1 \\
\end{array} \begin{array}{c}
\cdot
\end{array} \left[ \begin{array}{c}
\cdot
\end{array} \\
\cdot
\end{array} = \frac{P}{2} \left[ \begin{array}{c}
2 \\
1 \\
\end{array} \right]
\end{align*}
\]

Now put row corresponding to the node \( i \) to zero, from equation (20) the difference schemes with \( l^{(e)} = h \) is:

\[
\begin{align*}
\frac{4}{h^2} \left[ -u_{i-1} + 2u_i - u_{i+1} \right] + \frac{1}{6} \begin{array}{cc}
2 & 1 \\
1 & 4 \\
0 & 1 \\
\end{array} \begin{array}{c}
\cdot
\end{array} + \frac{4B}{2h} \left[ -u_{i-1} + u_{i+1} \right] + \frac{D}{6} \left[ u_{i-1} + 4u_i + u_{i+1} \right] = P
\end{align*}
\]

Applying the trapezoidal rule, following system of equations in Crank – Nicholson method are obtained:

\[
A_1u^{n+1}_{i-1} + A_2u^n_i + A_3u^n_{i+1} = A_4u^n_{i-1} + A_5u^n_i + A_6u^n_{i+1} + P^*
\]

Now from equations (11) and (12) following equations are obtained:

\[
B_1\theta^{n+1} = B_2\theta^n_i + B_3\theta^n_{i+1} = B_4\theta^n_{i-1} + B_5\theta^n_i + B_6\theta^n_{i+1}
\]

\[
C_1C^n_{i-1} + C_2C^n_i + C_3C^n_{i+1} = C_4C^n_{i-1} + C_5C^n_i + C_6C^n_{i+1}
\]

Where

\[
\begin{align*}
A_1 = 2 - 12Brh - Dh - 24r, & \quad A_2 = 8 + 4Drh + 48r, & \quad A_3 = 2 + 12Brh + Dh - 24r, \\
A_4 = 2 - 12Brh - Dh + 24r, & \quad A_5 = 8 - 4Drh - 48r, & \quad A_6 = 2 + 12Brh + Dh + 24r,
\end{align*}
\]

\[
\begin{align*}
B_1 = 2(Pr) - 12(Pr)Brh - 4R^2k - 24r - 4(Pr)Sk, & \quad B_2 = 8(Pr) + 48r + 16R^2k + 16(Pr)Sk, \\
B_3 = 2(Pr) + 12(Pr)Brh + 4R^2k - 24r + 4(Pr)Sk, & \quad B_4 = 2(Pr) - 12(Pr)Brh - 4R^2k + 24r - 4(Pr)Sk, \\
B_5 = 8(Pr) - 48r - 16R^2k - 16(Pr)Sk, & \quad B_6 = 2(Pr) + 12(Pr)Brh - 4R^2k + 24r - 4(Pr)Sk,
\end{align*}
\]

\[
\begin{align*}
C_1 = 2(Sc) - 12(Sc)Brh - 24r, & \quad C_2 = 8(Sc) + 48r, & \quad C_3 = 2(Sc) + 12(Sc)Brh - 24r, \\
C_4 = 2(Sc) - 12(Sc)Brh + 24r, & \quad C_5 = 8(Sc) - 48r, & \quad C_6 = 2(Sc) + 12(Sc)Brh + 24r,
\end{align*}
\]

\[
P^* = 12Pk = 12k \left( \frac{\partial U}{\partial t} + 4(Gr)\theta + DU \right)
\]
Here \( r = \frac{k}{h} \) and \( h, k \) are mesh sizes along \( y \) – direction and time – direction respectively. Index \( i \) refers to space and \( j \) refers to the time. In the equations (22), (23) and (24), taking \( i = 1(1)n \) and using boundary conditions (14), then the following system of equations are obtained:

\[
A_iX_i = B_i, \quad i = 1(1)3
\]

where \( A_i \)'s are matrices of order \( n \) and \( X_i, B_i \)'s are column matrices having \( n \) – components. The solutions of above system of equations are obtained by using Thomas algorithm for velocity, temperature and concentration. Also, numerical solutions for these equations are obtained by using \( C \) – programme. In order to prove the convergence and stability of Galerkin finite element method, the same \( C \) – programme was run with smaller values of \( h \) and \( k \) no significant change was observed in the values of \( u, \theta \) and \( C \). Hence the Galerkin finite element method is stable and convergent.

**4. RESULTS AND DISCUSSIONS**

In order to get physical insight into the problem, we have carried out numerical calculations for non-dimensional velocity field, temperature field, species concentration field, skin friction, Nusselt number and Sherwood number at the walls by assigning some specific values to the parameters entering into the problem and the effects of these values on the above fields are demonstrated graphically and tables. The following parameter values are adopted for computations unless otherwise indicated in the figures and table: \( Gr = 1.0, Gm = 1.0, M = 2.0, K = 1.0, Pr = 0.71, R = 2.0, S = 1.0, Sc = 0.22, \varepsilon = 0.1, \omega = 0.1, t = 1.0 \). The temperature and the species concentration are coupled to the velocity via Grashof number \((Gr)\) and Modified Grashof number \((Gc)\) as seen in equation (10). For various values of Grashof number and Modified Grashof number, the velocity profiles \( u \) are plotted in figures (2) and (3). The Grashof number \((Gr)\) signifies the relative effect of the thermal buoyancy force to the viscous hydrodynamic force in the boundary layer. As expected, it is observed that there is a rise in the velocity due to the enhancement of thermal buoyancy force. Also, as \( Gr \) increases, the peak values of the velocity increases rapidly near the porous plate and then decays smoothly to the free stream velocity. The Modified Grashof number \((Gc)\) defines the ratio of the species buoyancy force to the viscous hydrodynamic force. As expected, the fluid velocity increases and the peak value is more distinctive due to increase in the species buoyancy force. The velocity distribution attains a distinctive maximum value in the vicinity of the plate and then decreases properly to approach the free stream value. It is noticed that the velocity increases with increasing values of Modified Grashof number \((Gc)\).

![Figure-2: Velocity profiles for different values of thermal Grashof number Gr](image-url)
**Figure-3:** Velocity profiles for different values of solutal Grashof number $Gc$

Figure (4) illustrate the velocity profiles for different values of Prandtl number $Pr$. The numerical results show that the effect of increasing values of Prandtl number result in decreasing velocity. The nature of velocity profiles in presence of foreign species such as Hydrogen ($Sc = 0.22$), Helium ($Sc = 0.22$), Oxygen ($Sc = 0.60$) and Water vapour ($Sc = 0.66$) are shown in figure (5). The flow field suffers a decrease in primary velocity at all points in presence of heavier diffusing species.

**Figure-4:** Velocity profiles for different values of Prandtl number $Pr$

**Figure-5:** Velocity profiles for different values of Schmidt number $Sc$
The effect of the magnetic field parameter $M$ is shown in figure (6) in case of cooling of the plate. It is observed that the velocity of the fluid decreases with the increase of the magnetic field parameter values. The decrease in the velocity as the Hartmann number $M$ increases is because the presence of a magnetic field in an electrically conducting fluid introduces a force called the Lorentz force, which acts against the flow if the magnetic field is applied in the normal direction, as in the present study. This resistive force slows down the fluid velocity component as shown in figure (6).

The effect of the thermal radiation parameter $R$ on the primary velocity and temperature profiles in the boundary layer are illustrated in figures (7) and (8) respectively. Increasing the thermal radiation parameter $R$ produces significant increase in the thermal condition of the fluid and its thermal boundary layer. This increase in the fluid temperature induces more flow in the boundary layer causing the velocity of the fluid there to increase. Figure (9) and (10) has been plotted to depict the variation of velocity and temperature profiles against $y$ for different values of heat source parameter $S$ by fixing other physical parameters. From this Graph we observe that velocity and temperature decrease with increase in the heat source parameter $S$ because when heat is absorbed, the buoyancy force decreases the temperature profiles.
Figure -8: Temperature profiles for different values of Thermal radiation parameter $R$

Figure-9: Velocity profiles for different values of Heat source parameter $S$

Figure-10: Temperature profiles for different values of Heat source parameter $S$

Figure (11) illustrate the temperature profiles for different values of Prandtl number $Pr$. It is observed that the temperature decrease as an increasing the Prandtl number. The reason is that smaller values of $Pr$ are equivalent to increase in the thermal conductivity of the fluid and therefore heat is able to diffuse away from the heated surface more rapidly for higher values of $Pr$. Hence in the case of smaller Prandtl number the thermal boundary layer is thicker and the rate of heat transfer is reduced.
The effects of Schmidt number (Sc) on the concentration field are presented in figures (12). Figure (12) shows the concentration field due to variation in Schmidt number (Sc) for the gases Hydrogen, Helium, Water – vapour, Oxygen and Ammonia. It is observed that concentration field is steadily for Hydrogen and falls rapidly for Oxygen and Ammonia in comparison to Water – vapour. Thus Hydrogen can be used for maintaining effective concentration field and Water – vapour can be used for maintaining normal concentration field.

| Table – 1: Variation of numerical values of Skin – friction (τ) for different values of Gr, Gc, Sc, Pr, M, S and R |
|-----------------|----|----|----|----|----|----|
| Gr | Gc | Pr | Sc | M | S | R | τ |
| 1.0 | 1.0 | 0.71 | 0.22 | 2.0 | 1.0 | 1.0 | 3.2698 |
| 2.0 | 1.0 | 0.71 | 0.22 | 2.0 | 1.0 | 1.0 | 4.1059 |
| 1.0 | 2.0 | 0.71 | 0.22 | 2.0 | 1.0 | 1.0 | 4.5841 |
| 1.0 | 1.0 | 7.00 | 0.22 | 2.0 | 1.0 | 1.0 | 2.8520 |
| 1.0 | 1.0 | 0.71 | 0.60 | 2.0 | 1.0 | 1.0 | 2.8852 |
| 1.0 | 1.0 | 0.71 | 0.22 | 4.0 | 1.0 | 1.0 | 2.9543 |
| 1.0 | 1.0 | 0.71 | 0.22 | 2.0 | 2.0 | 2.0 | 2.9985 |
| 1.0 | 1.0 | 0.71 | 0.22 | 2.0 | 1.0 | 2.0 | 2.8546 |

| Table – 2: Variation of Nusselt number (Nu) for different values of Pr, S and R |
|-----------------|----|----|
| Pr | S | R | Nu |
| 0.71 | 1.0 | 1.0 | 1.9764 |
| 7.00 | 1.0 | 1.0 | 1.7530 |
| 0.71 | 2.0 | 1.0 | 1.6958 |
| 0.71 | 1.0 | 2.0 | 1.8682 |
Table – 3: Variation of Sherwood number (Sh) for different values of Sc

<table>
<thead>
<tr>
<th>Sc</th>
<th>Sh</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.22</td>
<td>1.6987</td>
</tr>
<tr>
<td>0.30</td>
<td>1.5209</td>
</tr>
<tr>
<td>0.60</td>
<td>1.3247</td>
</tr>
</tbody>
</table>

Table – (1) shows the variation of different values $Gr$, $Gc$, $Pr$, $Sc$, $M$, $S$ and $R$ on Skin – friction ($\tau$). From this table it is concluded that the Skin – friction ($\tau$) increases as the values of $Gr$ and $Gc$ increase and this behavior is found just reverse with the increase of $Pr$, $Sc$, $M$, $S$ and $R$. Table – (2) shows the variation of Nusselt number ($Nu$) different values of $Pr$, $S$ and $R$. From this table it is concluded that the Nusselt number ($Nu$) decreases as the value of $Pr$, $S$ and $R$ increases. Table – (3) shows the variation of Sherwood number ($Sh$) different values of $Sc$. From this table it is observed that Sherwood number ($Sh$) decreases as the value of $Sc$ increases.

5. CONCLUSIONS

An investigation of the heat and mass transfer in radiative magneto hydrodynamics fluid flow over a permeable vertical plate in the presence of the heat source is affected by the material parameters. The governing equations are approximated to a system of linear partial differential equations by using Galerkin finite element method. The results are presented graphically and we can conclude that the flow field and the quantities of physical interest are significantly influenced by these parameters.

1. The velocity increases as Grashof number $Gr$, Modified Grashof number $Gc$, increases. However, the velocity was found to decreases as the Hartmann number $M$, Prandtl number $Pr$, Schmidt number $Sc$, Thermal radiation parameter $R$, Heat source parameter $S$ are increases.
2. The fluid temperature was found to decreases as the thermal radiation parameter $R$, heat source parameter $S$ and Prandtl number $Pr$ are increases.
3. The fluid concentration was found to decreases as the Schmidt number $Sc$ increases.

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