

On Pre-generalized c^* -open sets and Pre-generalized c^* -open maps in topological spaces

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ABSTRACT

The aim of this paper is to introduce the notion of pre-generalized c^ -open sets in topological spaces and study their basic properties. Further the notion of pre-generalized c^* -open maps are introduced and their basic properties are discussed.*

Key words: pgc^* -open sets and pgc^* -open maps.

1. INTRODUCTION

In 1963, Norman Levine introduced semi-open sets in topological spaces. Also in 1970, he introduced the concept of generalized closed sets. Bhattacharya and Lahiri introduced and study semi-generalized closed (briefly, sg-closed) sets in 1987. Palaniappan and Rao introduced regular generalized closed (briefly, rg-closed) sets in 1993. In the year 1996, Andrijevic introduced and studied b-open sets. Gnanambal introduced generalized pre-regular closed (briefly gpr-closed) sets in 1997. In this paper we introduce pre-generalized c^* -open sets and pre-generalized c^* -open maps in topological spaces and study their basic properties.

Section 2 deals with the preliminary concepts. In section 3, pre-generalized c^* -open sets are introduced and their basic properties are discussed. The pre-generalized c^* -open maps in topological spaces are introduced in section 4.

2. PRELIMINARIES

Throughout this paper X denotes a topological space on which no separation axiom is assumed. For any subset A of X , $cl(A)$ denotes the closure of A , $int(A)$ denotes the interior of A , $pcl(A)$ denotes the pre-closure of A and $bcl(A)$ denotes the b-closure of A . Further $X \setminus A$ denotes the complement of A in X . The following definitions are very useful in the subsequent sections.

Definition 2.1: A subset A of a topological space X is called

- a semi-open set [8] if $A \subseteq cl(int(A))$ and a semi-closed set if $int(cl(A)) \subseteq A$.
- a pre-open set [16] if $A \subseteq int(cl(A))$ and a pre-closed set if $cl(int(A)) \subseteq A$.
- a regular-open set [18] if $A = int(cl(A))$ and a regular-closed set if $A = cl(int(A))$.
- A γ -open set [10] (b-open set [1]) if $A \subseteq cl(int(A)) \cup int(cl(A))$ and a γ -closed set (b-closed set) if $int(cl(A)) \cap cl(int(A)) \subseteq A$.
- a π -open set [22] if A is the finite union of regular-open sets and the complement of π -open set is said to be π -closed.

Definition 2.2: [12] A subset A of a topological space X is said to be a c^* -open set if $int(cl(A)) \subseteq A \subseteq cl(int(A))$.

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Definition 2.3: A subset A of a topological space X is called

- i. a generalized closed set (briefly, g -closed) [9] if $cl(A) \subseteq H$ whenever $A \subseteq H$ and H is open in X .
- ii. a regular-generalized closed set (briefly, rg -closed) [17] if $cl(A) \subseteq H$ whenever $A \subseteq H$ and H is regular-open in X .
- iii. a generalized pre-regular closed set (briefly, gpr -closed) [6] if $pcl(A) \subseteq H$ whenever $A \subseteq H$ and H is regular-open in X .
- iv. a regular generalized b -closed set (briefly, rgb -closed) [15] if $bcl(A) \subseteq H$ whenever $A \subseteq H$ and H is regular-open in X .
- v. a regular weakly generalized closed set (briefly, rwg -closed) [20] if $cl(int(A)) \subseteq H$ whenever $A \subseteq H$ and H is regular-open in X .
- vi. a semi-generalized b -closed set (briefly, sgb -closed) [7] if $bcl(A) \subseteq H$ whenever $A \subseteq H$ and H is semi-open in X .
- vii. a weakly closed (briefly, w -closed) set [19] (equivalently, \hat{g} -closed set [21]) if $cl(A) \subseteq H$ whenever $A \subseteq H$ and H is semi-open in X .
- viii. a semi-generalized closed set (briefly, sg -closed) [3] if $scl(A) \subseteq H$ whenever $A \subseteq H$ and H is semi-open in X .
- ix. a generalized semi-closed (briefly, gs -closed) set [2] if $scl(A) \subseteq H$ whenever $A \subseteq H$ and H is open in X .
- x. a $(gs)^*$ -closed set [5] if $cl(A) \subseteq H$ whenever $A \subseteq H$ and H is gs -open in X .

The complements of the above mentioned closed sets are their respectively open sets.

Definition 2.4: [12] A subset A of a topological space X is said to be a generalized c^* -closed set (briefly, gc^* -closed set) if $cl(A) \subseteq H$ whenever $A \subseteq H$ and H is c^* -open. The complement of the gc^* -closed set is gc^* -open [13].

Definition 2.5: A function $f: X \rightarrow Y$ is said to be

- i. a g -open map [11] if $f(U)$ is g -open in Y for every open set U of X .
- ii. a semi-generalized open (briefly, sg -open) [4] map if $f(U)$ is sg -open in Y for every open set U of X .
- iii. a \hat{g} -open map [21] if $f(U)$ is \hat{g} -open in Y for every open set U of X .
- iv. gc^* -open map [13] if $f(U)$ is gc^* -open in Y for every open set U of X .

Definition 2.6: [14] A subset A of a space X is said to be pre-generalized c^* -closed (briefly, pgc^* -closed) if $pcl(A) \subseteq H$ whenever $A \subseteq H$ and H is c^* -open.

3. Pre-generalized c^* -open sets

The complement of a pgc^* -closed set need not be pgc^* -closed. This leads to the definition of pgc^* -open sets. In this section we introduce pre-generalized c^* -open sets and study their basic properties.

Definition 3.1: A subset A of a space X is said to be pre-generalized c^* -open (briefly, pgc^* -open) if its complement is pgc^* -closed.

Example 3.2: Let $X = \{a, b, c\}$ with topology $\tau = \{\emptyset, \{b\}, \{c\}, \{b, c\}, X\}$. Then the pgc^* -open sets are $\emptyset, \{a\}, \{b\}, \{c\}, \{b, c\}, X$.

Proposition 3.3: Let X be a topological space. Then

1. Every w -open (resp. open, $(gs)^*$ -open, π -open, regular open, gc^* -open) set is pgc^* -open.
2. Every pgc^* -open set is gpr -open (resp. rgb -open).

The converse of the Proposition 3.3 need not be true as seen from the following example.

Example 3.4:

1. Let $X = \{a, b, c, d\}$ with topology $\tau = \{\emptyset, \{a\}, \{b\}, \{a, b\}, \{a, c\}, \{a, b, c\}, X\}$. Then the subset $\{a, b, d\}$ is pgc^* -open but not w -open (\hat{g} -open), $(gs)^*$ -open, open, π -open, regular-open and gc^* -open.
2. Let $X = \{a, b, c, d, e\}$ with topology $\tau = \{\emptyset, \{a\}, \{d\}, \{e\}, \{a, d\}, \{a, e\}, \{d, e\}, \{a, d, e\}, X\}$. Then the subset $\{a, c, d\}$ is gpr -open and rgb -open but not pgc^* -open.

Proposition 3.5: Let X be a topological space. Then for any element $p \in X$, the set $\{p\}$ is either pgc^* -open or c^* -open.

Proof: Suppose $\{p\}$ is not a c^* -open set. Then $X \setminus \{p\}$ is not a c^* -open set. By Proposition 3.20 [14], $X \setminus \{p\}$ is pgc^* -closed. Hence $\{p\}$ is a pgc^* -open.

The intersection of two pgc^* -open subsets of a space X need not be pgc^* -open. For example, let $X = \{a, b, c, d, e\}$ with topology $\tau = \{\emptyset, \{a, b\}, \{c, d\}, \{a, b, c, d\}, X\}$. Then the subsets $\{b, c, d, e\}$ and $\{a, c, d, e\}$ are pgc^* -open but their intersection $\{c, d, e\}$ is not a pgc^* -open set.

The union of two pgc^* -open subsets of a space X need not be pgc^* -open. For example, let $X = \{a, b, c, d, e\}$ with topology $\tau = \{\emptyset, \{a, b\}, \{c, d\}, \{a, b, c, d\}, X\}$. Then the subsets $\{a, d\}$ and $\{a, e\}$ are pgc^* -open but their union $\{a, d, e\}$ is not a pgc^* -open set.

Proposition 3.6: Let A be a subset of a space X . Then the following are equivalent.

- i. A is pgc^* -open.
- ii. $H \subseteq p\text{-int}(A)$ whenever $H \subseteq A$ and H is c^* -open.

Proof:

(i) \Rightarrow (ii): Assume that A is pgc^* -open. Then $X \setminus A$ is pgc^* -closed. Let H be a c^* -open set and $H \subseteq A$. Then $X \setminus H$ is a c^* -open set containing $X \setminus A$. Since $X \setminus A$ is pgc^* -closed, we have $pcl(X \setminus A) \subseteq X \setminus H$. This implies, $X \setminus (pcl(X \setminus A)) \supseteq H$. That is, $H \subseteq p\text{-int}(A)$.

(ii) \Rightarrow (i): Assume that H is a c^* -open set containing $X \setminus A$. Then $X \setminus H$ is a c^* -open set and $A \supseteq X \setminus H$. By hypothesis, $X \setminus H \subseteq p\text{-int}(A)$. This implies, $X \setminus (p\text{-int}(A)) \subseteq H$. That is, $pcl(X \setminus A) \subseteq H$. Therefore, $X \setminus A$ is pgc^* -closed. Hence, A is pgc^* -open.

Proposition 3.7: Let X be a topological space. If A is a pgc^* -open subset of X such that $p\text{-int}(A) \subseteq B \subseteq A$, then B is pgc^* -open.

Proof: Let A be a pgc^* -open set and $p\text{-int}(A) \subseteq B \subseteq A$. Then $X \setminus A$ is a pgc^* -closed set and $X \setminus A \subseteq X \setminus B \subseteq pcl(X \setminus A)$. Therefore, by Proposition 3.22 [14], $X \setminus B$ is pgc^* -closed. Therefore, B is pgc^* -open.

Proposition 3.8: A subset A of X is pgc^* -open if and only if for each $H \subseteq A$ and H is c^* -open, there exists a pre-open set G such that $H \subseteq G \subseteq A$.

Proof: Suppose that A is pgc^* -open. Assume that $H \subseteq A$ and H is c^* -open. Then, by Proposition 3.6, $H \subseteq p\text{-int}(A)$. If we put $G = p\text{-int}(A)$, then $H \subseteq G \subseteq A$. Conversely, assume that H is a c^* -open set contained in A . Then by hypothesis, there exists a pre-open set G such that $H \subseteq G \subseteq A$. Since $p\text{-int}(A)$ is the largest pre-open set contained in A , we have $G \subseteq p\text{-int}(A)$. Also, since $H \subseteq G$, we have $H \subseteq p\text{-int}(A)$. Therefore, by Proposition 3.6, A is pgc^* -open.

4. Pre-generalized c^* -open maps

In this section, we introduce pre-generalized c^* -open maps in topological spaces. Also, we derive some of their basic properties.

Definition 4.1: Let X and Y be two topological spaces. A function $f : X \rightarrow Y$ is said to be pre-generalized c^* -open map (briefly, pgc^* -open map) if $f(U)$ is pgc^* -open in Y for every open set U in X .

Example 4.2: Let $X = \{a, b, c\}$ with topology $\tau = \{\emptyset, \{a\}, X\}$ and $Y = \{1, 2, 3\}$ with topology $\sigma = \{\emptyset, \{1\}, \{1, 2\}, Y\}$. Define $f : X \rightarrow Y$ by $f(a) = 2, f(b) = 3, f(c) = 1$. Then f is pgc^* -open.

Proposition 4.3: Let X, Y be two topological spaces. A function $f : X \rightarrow Y$ is a pgc^* -open if and only if the image of each closed subset of X is pgc^* -closed in Y .

Proof: Assume that $f : X \rightarrow Y$ is a pgc^* -open map. Let V be a closed set in X . Then $X \setminus V$ is open in X . Therefore, by our assumption, $f(X \setminus V)$ is pgc^* -open in Y . This implies, $Y \setminus f(V)$ is pgc^* -open in Y . Hence, $f(V)$ is pgc^* -closed in Y . Conversely, assume that the image of each closed subset of X is pgc^* -closed in Y . Let U be an open set in X . Then $X \setminus U$ is closed in X . Therefore, by our assumption, $f(X \setminus U)$ is pgc^* -closed in Y . This implies, $Y \setminus f(U)$ is pgc^* -closed in Y . This implies, $f(U)$ is pgc^* -open in Y . Therefore, f is a pgc^* -open map.

Proposition 4.4: Let X, Y be two topological spaces. Then every open map is pgc^* -open.

Proof: Let $f : X \rightarrow Y$ be an open map and U be an open set in X . Then $f(U)$ is open in Y . By Proposition 3.3, $f(U)$ is a pgc^* -open set. Therefore, f is a pgc^* -open map.

The following example shows that the converse of the Proposition 4.4 is not true.

Example 4.5: Let $X = \{a, b, c\}$ and $Y = \{1, 2, 3\}$. Then, clearly $\tau = \{\emptyset, \{b\}, \{c\}, \{b, c\}, X\}$ is a topology on X and $\sigma = \{\emptyset, \{1\}, \{1, 2\}, \{1, 3\}, Y\}$ is a topology on Y . Define $f : X \rightarrow Y$ by $f(a) = 2, f(b) = 3, f(c) = 1$. Clearly, f is a pgc^* -open map. But f is not an open map, since the image of an open set $\{b\}$ under f is $\{3\}$, which is not open in Y .

Proposition 4.6: Let X, Y be two topological spaces. Then every \hat{g} -open map is pgc^* -open.

Proof: Let $f: X \rightarrow Y$ be a \hat{g} -open map. Let U be an open set in X . Then $f(U)$ is \hat{g} -open in Y . Therefore, by Proposition 3.3, $f(U)$ is a pgc^* -open set. Therefore, f is a pgc^* -open map.

The converse of the Proposition 4.6 need not be true, which can be verified from the following example.

Example 4.7: Let $X=\{a, b, c\}$ and $Y=\{1, 2, 3\}$. Then, clearly $\tau=\{\emptyset, \{b\}, \{c\}, \{b, c\}, X\}$ is a topology on X and $\sigma=\{\emptyset, \{1\}, \{1, 2\}, \{1, 3\}, Y\}$ is a topology on Y . Define $f: X \rightarrow Y$ by $f(a)=2, f(b)=3, f(c)=1$. Then f is a pgc^* -open map. Consider the open set $\{b\}$ in X . Then $f(\{b\})=\{3\}$, which is not a \hat{g} -open set in Y . Therefore, f is not a \hat{g} -open map.

The g -open and pgc^* -open maps are independent. For example, let $X=\{a, b, c, d\}$ and $Y=\{1, 2, 3, 4, 5\}$. Then, clearly $\tau=\{\emptyset, \{a\}, \{b\}, \{a, b\}, \{a, c\}, \{a, b, c\}, X\}$ is a topology on X and $\sigma=\{\emptyset, \{1\}, \{4\}, \{5\}, \{1, 4\}, \{1, 5\}, \{4, 5\}, \{1, 4, 5\}, Y\}$ is a topology on Y . Define $f: X \rightarrow Y$ by $f(a)=1, f(b)=2, f(c)=f(d)=3$. Then f is a g -open map. Consider the open set $\{a, c\}$ in X . Then $f(\{a, c\})=\{1, 3\}$, which is not a pgc^* -open set in Y . Hence f is not a pgc^* -open map. Define $g: X \rightarrow Y$ by $g(a)=g(b)=2, g(c)=3, g(d)=5$. Then $g: X \rightarrow Y$ is a pgc^* -open map. Consider the open set $\{a, c\}$ in X . Then $g(\{a, c\})=\{2, 3\}$, which is not a g -open set in Y . Therefore, g is not a g -open map.

The sg -open and pgc^* -open maps are independent. For example, let $X=\{a, b, c, d\}$ and $Y=\{1, 2, 3, 4, 5\}$. Then, clearly $\tau=\{\emptyset, \{a\}, \{b\}, \{a, b\}, \{a, c\}, \{a, b, c\}, X\}$ is a topology on X and $\sigma=\{\emptyset, \{1\}, \{4\}, \{5\}, \{1, 4\}, \{1, 5\}, \{4, 5\}, \{1, 4, 5\}, Y\}$ is a topology on Y . Define $f: X \rightarrow Y$ by $f(a)=1, f(b)=4, f(c)=f(d)=3$. Then f is a sg -open map. Consider the open set $\{a, c\}$ in X . Then $f(\{a, c\})=\{1, 3\}$, which is not a pgc^* -open set in Y . Hence f is not a pgc^* -open map. Define $g: X \rightarrow Y$ by $g(a)=g(b)=2, g(c)=3, g(d)=5$. Then $g: X \rightarrow Y$ is a pgc^* -open map. Consider the open set $\{b\}$ in X . Then $g(\{b\})=\{2\}$, which is not a sg -open set in Y . Therefore, g is not a sg -open map.

Proposition 4.8: Let X, Y and Z be topological spaces. If $f: X \rightarrow Y$ is an open map and $g: Y \rightarrow Z$ is a gc^* -open map, then $g \circ f$ is pgc^* -open map.

Proof: Let U be an open set in X . Since f is an open map, $f(U)$ is open in Y . Then $g(f(U))$ is a gc^* -open set in Z . That is, $(g \circ f)(U)$ is a gc^* -open set in Z . Therefore, by Proposition 3.3, $(g \circ f)(U)$ is a pgc^* -open set in Z . Therefore, $g \circ f$ is a pgc^* -open map.

Proposition 4.9: Let X, Y and Z be topological spaces. If $f: X \rightarrow Y$ and $g: Y \rightarrow Z$ are open maps, then $g \circ f: X \rightarrow Z$ is a pgc^* -open map.

Proof: Let U be an open set in X . Since f is an open map, $f(U)$ is open in Y . Also, since g is an open map, $g(f(U))$ is open in Z . That is, $(g \circ f)(U)$ is an open set in Z . By Proposition 3.3, $(g \circ f)(U)$ is a pgc^* -open set in Z . Therefore, $g \circ f$ is a pgc^* -open map.

Proposition 4.10: Let X, Y and Z be topological spaces. If $f: X \rightarrow Y$ is an open map and $g: Y \rightarrow Z$ is a pgc^* -open map, then $g \circ f$ is pgc^* -open map.

Proof: Let U be an open set in X . Since f is an open map, $f(U)$ is open in Y . Then $g(f(U))$ is a pgc^* -open set in Z . That is, $(g \circ f)(U)$ is a pgc^* -open set in Z . Therefore, $g \circ f$ is a pgc^* -open map.

Proposition 4.11: Let X, Y and Z be topological spaces. If $f: X \rightarrow Y$ is an open map and $g: Y \rightarrow Z$ is a \hat{g} -open map, then $g \circ f: X \rightarrow Z$ is a pgc^* -open map.

Proof: Let U be an open set in X . Since f is an open map, $f(U)$ is open in Y . Then $g(f(U))$ is a \hat{g} -open set in Z . That is, $(g \circ f)(U)$ is a \hat{g} -open set in Z . Therefore, by Proposition 3.3, $(g \circ f)(U)$ is a pgc^* -open set in Z . Hence $g \circ f: X \rightarrow Z$ is a pgc^* -open map.

Proposition 4.12: Let X, Y be two topological spaces. A surjective function $f: X \rightarrow Y$ is a pgc^* -open map if and only if for each subset B of Y and for each closed set U containing $f^{-1}(B)$, there is a pgc^* -closed set V of Y such that $B \subset V$ and $f^{-1}(V) \subset U$.

Proof: Suppose $f: X \rightarrow Y$ is a surjective pgc^* -open map and B is a subset of Y . Let U be a closed set in X such that $f^{-1}(B) \subset U$. Then $V=Y \setminus f(X \setminus U)$ is a pgc^* -closed subset of Y containing B and $f^{-1}(V) \subset U$. Conversely, suppose F is an open subset of X . Then $X \setminus F$ is closed in X . Also, $f^{-1}(Y \setminus f(F))=X \setminus f^{-1}(f(F)) \subset X \setminus F$. Therefore, by hypothesis, there exists a pgc^* -closed set V of Y such that $Y \setminus f(F) \subset V$ and $f^{-1}(V) \subset X \setminus F$. This implies, $F \subset X \setminus f^{-1}(V)$. Therefore, $f(F) \subset f(X \setminus f^{-1}(V)) \subset Y \setminus V$. Also, $Y \setminus V \subset f(F)$. This implies, $f(F)=Y \setminus V$, which is pgc^* -open in Y . Therefore, f is a pgc^* -open map.

CONCLUSION

In this paper we have introduced pgc^* -open sets and pgc^* -open maps in topological spaces and studied some of their basic properties. Also, we have studied the relationship between pgc^* -open sets with some generalized sets in topological spaces.

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