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## FUZZY SUB NEAR-FIELD SPACES OF A Γ-NEAR-FIELD SPACE OVER NEAR-FIELD (FSNF-Γ-NF-O NF)

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#### **ABSTRACT**

T he object of this paper is to introduce notion of fuzzy left (respectively right) sub near-field spaces of a  $\Gamma$ -near-field space over a near-field and to study the related properties of fuzzy sub near-field spaces in a  $\Gamma$ -near-field space over a near-field.

**Keywords:**  $\Gamma$ -near-field space; Fuzzy sub near-field space of  $\Gamma$ -near-field space; Fuzzy near-field space of  $\Gamma$ -near-field space.

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#### **SECTION-1: INTRODUCTION**

In this paper we consider the fuzzification of left (resp. right) sub near-field spaces of  $\Gamma$ -near-filed spaces over a near-field, and we three Smt. Thurumella Madhavi Latha, Dr. T V Pradeep Kumar and Dr. N V Nagendram together investigate the related properties of left (resp. right) sub near-field spaces of  $\Gamma$ -near-filed spaces over a near-field.

In fact,  $\Gamma$ -near-rings were defined by Bhavanari Satyanarayana, who is the professor cum Head of the department of Mathematics, Acharya Nagarjuna University at present and also guide of Dr T V Pradeep Kumar and the ideal theory in  $\Gamma$ -near-rings was studied by Dr. Bhavanari Satyanarayana and G. L. Booth. Fuzzy ideals of rings were introduced by W. Liu, and it has been studied by several authors. The notion of fuzzy ideals and its properties were applied to various areas: semi-groups, BCK-algebras, and semi-rings.

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#### **SECTION-2: PRELIMINARIES**

A near-field space is a triple (N, +, .) such that (N, +) is a group, if (N, .) is a semi group, and "." Is left distributive over "+" i.e. w(x + z) = wx + wz for each  $w, x, y, z \in N$ . A near-field space N is d.g. if there exists  $T \subset N$  such that (T, .) is a semi sub near-field space of (N, .) each element of T is right distributive and T is an additive generating space for (N, +). The near-field space generated additively by all the endomorphism of a (not necessarily commutative) sub near-field space (G, +) is d.g. T being the space of endomorphisms. Such a near-field space will be called an endomorphism near-field space and will be denoted by E(G).

Dr N V Nagendram has shown that the near-field space generated by all the inner automorphisms of a finite simple, non-commutative, sub near-field space (G, +) is E(G). In fact, this near-field space generated by the inner automorphisms consists of all the mappings of G into G which leave G fixed and also has given a necessary and sufficient condition that the near-field space generated by the inner automorphisms of a sub near-field space of a near-field space be a near-field space. However, the more general endomorphism near-field space has not been studied.

If  $\alpha$  is an endomorphism of (G, +) and  $g \in G$ , the image of g under  $\alpha$  is denoted by  $g\alpha$ . Addition of functions on G is done point-wise and multiplication of such functions is composition.

**Definition 2.1:** A sub near-field space H of the near-field space N is a N-sub near-field space over a near-field if  $HN \subset H$ . The radical sub near-field space J(N) is the intersection of the right sub near-field spaces of N which are maximal N-sub near-field spaces over a near-field.

**Definition 2.2: closed (or open) sub near-field space.** More generally, for positive integers m, n we define M to be an (m, n)-closed (or open) sub near-field space of N if  $x^m \in M$  for  $x \in N \Rightarrow x^n \in M$ .

**Definition 2.3: radical sub near-field space.** M is a radical sub near-field space if and only if M is a (2, 1)-closed (or open) sub near-field space. In fact, an n-absorbing sub near-field space is (m, n)-closed (or open) sub near-field space for every positive integer m.

**Note 2.4:** clearly, a proper radical sub near-field space of N is (m, n)-closed (or open) radical sub near-field space for  $1 \le m \le n$ . So we often assume that  $1 \le n \le m$ .

**Definition 2.5:** A sub near-field space A of a  $\Gamma$ -near-filed spaces over a near-field M is called a *left* (resp. right) sub near-field space of M if (i) (A; +) is a normal divisor of (M; +), (ii)  $u\alpha(x + v) - u\alpha v \in A$  (resp.  $x\alpha u \in A$ ) for all  $x \in A$ ,  $\alpha \in \Gamma$  and  $u; v \in M$ .

We now review some fuzzy logic concepts.

**Definition 2.6:** A fuzzy sub near-field space in a  $\Gamma$ -near-filed space M is a function  $\mu: M \to [0; 1]$ .

**Definition 2.7:** We shall use the notation  $\mu_t$ , called a level sub near-field space of  $\mu_t$ , for  $\{x \in M / \mu(x) \ge t\}$  where  $t \in [0; 1]$ . If  $\mu_t$  is a fuzzy sub near-field space in a  $\Gamma$ -near-filed spaces over a near-field M and f is a function defined on M, then the fuzzy sub near-field space V in V is called the *image* of V under V.

**Definition 2.8:** if v is a fuzzy sub near-field space in f(M), then the fuzzy sub near-field space  $\mu = v \circ f$  in a Γ-near-field space over a near-field M (that is, the fuzzy sub near-field space defined by  $\mu(x) = v(f(x))$  for all  $x \in M$ ) is called the preimage of v under f. We say that a fuzzy sub near-field space  $\mu$  in a Γ-near-field space over a near-field M has the sup property if, for any sub near-field space T of a Γ-near-filed space over a near-field M, there exists  $t_0 \in T$  such that  $\mu(t_0) = \sup [\mu(t)]$  for all  $t \in T$ .

### SECTION-3: FUZZY SUB NEAR-FIELD SPACES OF $\Gamma$ -NEAR-FILED SPACE OVER A NEAR-FIELD

**Definition 3.1** A Fuzzy sub near-field space  $\mu$  in a Γ-near-filed space over a near-field M is called a fuzzy left (resp. right) sub near-field space of a Γ-near-filed space over near-field M if (i)  $\mu$  is a fuzzy normal divisor with respect to the addition, (ii)  $\mu(u\alpha(x+v)-u\alpha v) \ge \mu(x)$  (resp.  $\mu(x, u) \ge \mu(x)$ ) for all x; u;  $v \in M$  and  $\alpha \in \Gamma$ . The condition (i) of Definition 3.1 means that  $\mu$  satisfies: (i)  $\mu(x-y) \ge \min\{\mu(x); \mu(y)\}$ , and (ii)  $\mu(y+x-y) \ge \mu(x)$ ,  $\forall x; y \in M$ .

**Note 3.2:** If  $\mu$  is a fuzzy left (resp. right) sub near-field space of a  $\Gamma$ -near-filed space over a near-field M, then  $\mu(0) \ge \mu(x)$  for all  $x \in M$ , where 0 is the zero sub near-field space of M.

**Theorem 3.3:** Let M be a fuzzy left (resp. right) sub near-field space of a  $\Gamma$ -near-filed space over a near-field M. Then the set  $M_{\mu} = \{x \in M \mid \mu(x) = \mu(0)\}$  is a fuzzy left (resp. right) sub near-field space of a  $\Gamma$ -near-filed space over a near-field M.

**Proof:** Let  $\mu$  be a fuzzy left ideal and let x;  $y \in M_{\mu}$ . Then  $\mu(x-y) \ge \min \{\mu(x); \mu(y)\} = \mu(0)$ ; and so  $\mu(x-y) = \mu(0)$  or  $x-y \in M_{\mu}$ .

For every  $y \in M$  and  $x \in M_{\mu}$ , we have  $\mu(y+x-y) \ge \mu(x) = \mu(0)$ . Therefore, we have,  $y+x-y \in M_{\mu}$ , which shows that  $M_{\mu}$  is a fuzzy normal divisor left (resp. right) sub near-field space of a  $\Gamma$ -near-filed space M with respect to the addition. Let  $x \in M_{\mu}$ ,  $\alpha \in \Gamma$  and u;  $v \in M$ .

Then  $\mu(u\alpha(x+v)-u\alpha v) \ge \mu(x) = \mu(0)$ ; and hence  $\mu(u\alpha(x+v)-u\alpha v) = \mu(0)$ ; i.e.,  $u\alpha(x+v)-u\alpha v \in M_{\mu}$ . Therefore  $M_{\mu}$  is a fuzzy left (resp. right) sub near-field space of a  $\Gamma$ -near-field space over a near-field M. Similarly we have the desired result for the right case. This completes the proof of the theorem.

Theorem 3.4: Let A be a non-empty fuzzy sub near-field space of a Γ-near-field space over an near-field M and  $\mu_A$  be a fuzzy sub near-field space of a Γ-near-field space over an near-field in M defined by  $\mu_A(x) = \begin{cases} s & \text{if } x \in A \\ t & \text{Otherwise} \end{cases}$ , for

all  $x \in M$  and  $s, t \in [0; 1]$  with s > t. Then  $\mu_A$  is a fuzzy left (resp. right) sub near-field space of a  $\Gamma$ -near-field space over an near-field of M if and only A is a fuzzy left (resp. right) sub near-field space of a  $\Gamma$ -near-field space over an near-field of M. Moreover  $M_{\mu A} = A$ .

**Proof:** Let  $\mu_A$  be a fuzzy sub near-field space of a  $\Gamma$ -near-field space over an near-field of M and let  $x, y \in A$ . Then  $\mu_A(x-y) \geq \min \{\mu_A(x)/\mu_A(y)\} = s$ ; and so  $\mu_A(x-y) = s$ .

 $\Rightarrow$  x - y 2 A. For any y  $\in$  M and x  $\in$  A, we have  $\mu_A(y+x-y) \ge \mu_A(x) = s$  and so  $y+x-y \in A$ .

Now let  $x \in A$ ,  $\alpha \in \Gamma$  and  $u, v \in M$ .

Then  $\mu_A(u\alpha(x+v)-u\alpha v) \ge \mu_A(x) = s$  (resp.  $\mu_A(x\alpha u) \ge \mu_A(x) = s$ ), and therefore we have,  $\mu_A(u\alpha(x+v)-u\alpha v) = s$  (resp.  $\mu_A(x\alpha u) = s$ ).

Thus  $u\alpha(x + v) - u\alpha v \in A$  (resp.  $x\alpha u \in A$ ). This shows that A is a fuzzy sub near-field space of a  $\Gamma$ -near-field space over an near-field of M.

Conversely assume that A is a fuzzy sub near-field space of a  $\Gamma$ -near-field space over an near-field of M. Let  $x, y \in M$ . If at least one of x and y does not belong to A, then  $\mu_A(x-y) \ge t = \min \{\mu_A(x) : \mu_A(y) \}$ : If  $x, y \in A$ , then  $x-y \in A$  and so  $\mu_A(x-y) = s = \min \{\mu_A(x) : \mu_A(y) \}$ : If  $x \in A$ , then  $y+x-y \in A$  and hence  $\mu_A(y+x-y) = s = \mu_A(x)$ .

Clearly  $\mu_A(y+x-y) \ge t = \mu_A(x)$  for all  $x \notin A$  and  $y \in M$ . This shows that  $\mu_A$  is a fuzzy normal divisor fuzzy sub near-field space of a  $\Gamma$ -near-field space over an near-field of M with respect to the addition.

Now let x, u,  $v \in M$  and  $\alpha \in \Gamma$ . If  $x \in A$ , then  $u\alpha(x+v) - u\alpha v \in A$  (resp.  $x\alpha u \in A$ ) and thus  $\mu_A(u\alpha(x+v) - u\alpha v) = s = \mu_A(x)$  (resp.  $\mu_A(x\alpha u) = s = \mu_A(x)$ ). If  $x \notin A$ , then clearly  $\mu_A(u\alpha(x+v) - u\alpha v) \ge t = \mu_A(x)$  (resp.  $\mu_A(x\alpha u) \ge t = \mu_A(x)$ ). Hence  $\mu_A$  is a fuzzy sub near-field space of a  $\Gamma$ -near-field space over an near-field of M. Moreover  $M_{\mu A} = \{x \in M / \mu_A(x) = \mu_A(x) = x \in M / \mu_A(x) = x$ 

Corollary 3.5: Let M be a fuzzy sub near-field space of a  $\Gamma$ -near-field space over a near-field and  $\chi_A$  be the characteristic function of a sub near-field space of a  $\Gamma$ -near-field space over an near-field A  $\subset$  M. Then  $\chi A$  is a fuzzy left (resp. right) sub near-field space of a  $\Gamma$ -near-field space over an near-field of M if and only if A is a fuzzy left (resp. right) sub near-field space of a  $\Gamma$ -near-field space over an near-field of M.

**Theorem 3.6:** Let  $\mu$  be a fuzzy sub near-field space of a Γ-near-field space over a near-field in M. Then  $\mu$  is a fuzzy left (resp. right) sub near-field space of a Γ-near-field space over a near-field of M if and only if each level subset  $\mu_t$ , t ∈ Img( $\mu$ ), of  $\mu$  is a fuzzy left (resp. right) sub near-field space of a Γ-near-field space over a near-field of M. Here let us call  $\mu_t$  a level fuzzy left (resp. right) sub near-field space of a Γ-near-field space over a near-field  $\mu$ .

**Proof:** Let  $\mu$  be a fuzzy left (resp. right) sub near-field space of a  $\Gamma$ -near-field space over a near-field of M and let  $t \in Im(\mu)$ . For any  $x, y \in \mu_t$ , we have  $\mu(x-y) \ge \min\{\mu(x); \mu(y)\} \ge t$  and so  $x-y \in \mu_t$ . Let  $y \in M$  and  $x \in \mu_t$ . Then  $\mu(y+x-y) \ge \mu(x) \ge t$ ; whence  $y+x-y \in \mu_t$ . Now let  $x \in \mu_t$ ,  $\mu \in \Gamma$  and  $\mu(x) \in M$ . Then  $\mu(\mu(x)) = \mu(x) \ge t$  (resp.  $\mu(x) \ge t$ ), which implies that  $\mu(x) = \mu(x) = t$  (resp.  $\mu(x) \ge t$ ).

Hence  $\mu_t$  is a fuzzy left (resp. right) sub near-field space of a  $\Gamma$ -near-field space over a near-field of M. Conversely assume that  $\mu_t$  is a fuzzy left (resp. right) a fuzzy sub near-field space of a  $\Gamma$ -near-field space over a near-field M for every  $t \in Img(\mu)$ . If  $\mu(x_0 - y_0) < min\{\mu(x_0), \mu(y_0)\}$  for some  $x_0, y_0 \in M$ , then by taking  $t_0 = \frac{1}{2}[(\mu(x_0 - y_0) + min\{\mu(x_0); \mu(y_0)\})]$  we have  $\mu(x_0 - y_0) < t_0, \mu(x_0) > t_0$  and  $\mu(y_0) > t_0$ . Hence  $x_0 - y_0 \notin \mu_{t0}$ ,  $x_0 \in \mu_{t0}$  and  $y_0 \in \mu_{t0}$ . This is a contradiction,  $\otimes$  and so  $\mu(x - y) \ge min\{\mu(x), \mu(y)\}$  for all  $x, y \in M$ .

Assume that  $\mu(y_0+x_0-y_0)<\mu(x_0)$  for some  $x_0,y_0\in M$ . Putting  $s_0=1/2$  ( $\mu(y_0+x_0-y_0)+\mu(x_0)$ ); then  $\mu(y_0+x_0-y_0)< s_0<\mu(x_0)$ : It follows that  $x_0\in\mu_{s0}$  and  $y_0+x_0-y_0\not\in\mu_{s0}$  which is impossible. Hence,  $\mu(y+x-y)\geq\mu(x)$  for all  $x,y\in M$ . If the condition (ii) of Definition 3.1 is not true, then for a fixed  $\mu\in\Gamma$  there exist  $x,u,v\in M$  such that  $\mu(u\alpha(x+v)-u\alpha v)<\mu(x)$  (resp.  $\mu(x)$ ). Let  $\mu(x)$  (resp.  $\mu(x)$ ). Let  $\mu(x)$  (resp.  $\mu(x)$ ). Then  $\mu(x)$  (resp.  $\mu(x)$ ) and  $\mu(x)$ 0 (resp.  $\mu(x)$ 0). This is a contradiction, and we are done. This completes the proof of the theorem.

**Theorem 3.7:** Let A be a fuzzy left (resp. right) sub near-field space of a  $\Gamma$ -near-field space over a near-field M. Then for any  $t \in (0; 1]$  there exists a fuzzy left (resp. right) sub near-field space of a  $\Gamma$ -near-field space over a near-field  $\mu$  of M such that  $\mu_t = A$ .

**Proof:** Let  $\mu: M \to [0; 1]$  be a fuzzy sub near-field space of a  $\Gamma$ -near-field space over a near-field defined by

$$\mu(x) = \begin{cases} t & \text{if } x \in A \\ 0 & \text{otherwise} \end{cases} \text{ for all } x \in M, \text{ where } t \in (0; 1]. \text{ Then clearly } \mu_t = A.$$

It is easy to prove that  $\mu(x - y) \ge \min \{\mu(x), \mu(y)\}; x, y \in M$ :

Assume that  $\mu(y+x-y) < \mu(x)$  for some  $x; y \in M$ . Since  $\mu$  is two-valued, i.e.,  $|Img(\mu)| = 2$ ,  $\mu(y+x-y) = 0$  and  $\mu(x) = t$  and hence  $y+x-y \notin A$  and  $x \in A$ .

This contradicts the fact that (A, +) is a normal divisor sub near-field space of a  $\Gamma$ -near-field space over a near-field of (M, +).

Hence  $\mu(y+x-y) < \mu(x)$  for all  $x, y \in M$ . Now assume that  $\mu(u\alpha(x+v)-u\alpha v) < \mu(x)$  (resp.  $\mu(x\alpha u) < \mu(x)$ ) for some  $x, u, v \in M$  and  $\mu \in \Gamma$ .

Since  $|Img(\mu)|=2$ , we have  $\mu(u\alpha(x+v)-u\alpha v)=0$  and  $\mu(x)=t$  (resp.  $\mu(x\alpha u)=0$  and  $\mu(x)=t$ ); whence  $u\alpha(x+v)-u\alpha v\not\in A$  and  $x\in A$  (resp.  $x\alpha u\not\in A$  and  $x\in A$ ). This is impossible because A is a fuzzy left (resp. right) sub near-field space of a  $\Gamma$ -near-field space over a near-field of M, which proves the theorem.

**Theorem 3.8:** If  $\mu$  is a fuzzy left (resp. right) sub near-field space of a  $\Gamma$ -near-field space over a near-field of M, then  $\mu(x) = \sup\{t \in [0; 1]/x \in \mu_t\}; \ \forall \ x \in M$ :

**Proof:** Let  $s := \sup\{t \in [0; 1]/x \in \mu_t\}$  and let  $\epsilon > 0$  be given. Then  $s - \epsilon < t$  for some  $t \in [0; 1]$  such that  $x \in \mu_t$ , and so  $s - \epsilon < \mu(x)$ . Since  $\epsilon$  is arbitrary, it follows that  $s \le \mu(x)$ . Now let  $\mu(x) = u$ . Then  $x \in \mu_u$  and so  $u \in \{t \in [0; 1]/x \in \mu_t\}$ : Hence  $\mu(x) = u \le \sup\{t \in [0; 1]/x \in \mu_t\} = s$ . Therefore  $\mu(x) = s$ , as desired. 2 We now consider the converse of Theorem 3.8. Let A be a non-empty subset of [0; 1]. Without loss of generality, we may use A as an index set in the following:

**Theorem 3.9:** Let  $\{A_t/t \in A\}$  be a collection of fuzzy left (resp. right) sub near-field space of a  $\Gamma$ -near-field space over a near-field M such that

(i) 
$$M = \bigcup_{t \in A} A_t$$
, (ii)  $s > t$  if and only if  $A_s \subset A_t$  for all  $s$ ;  $t \in A$ . Define a fuzzy set  $\mu$  in  $M$  by  $\mu(x) = \sup\{t \in A/x \in A_t\}$ ;

 $\forall x \in M$ : Then  $\mu$  is a fuzzy left (resp. right) sub near-field space of a  $\Gamma$ -near-field space over a near-field of M.

**Proof:** By theorem 3.6, It is sufficient to show that  $\mu_p$  ( $\neq 0$ ) is a fuzzy left (resp. right) sub near-field space of a  $\Gamma$ -near-field space over a near-field of M for every  $p \in [0;1]$ . We consider the following two cases:

(1) 
$$p = \sup\{t \in \mu / t < p\}$$
 and (2)  $p \neq \sup\{t \in \mu / t < p\}$ :

Case (1) implies that  $x \in \mu p$ ,  $x \in A_t$  for all t < p,  $x \in A_t$  for all t < p, whence  $\mu_p = A_t$  for all t < p which is a fuzzy left (resp. right) sub near-field space of a  $\Gamma$ -near-field space over a near-field of M. For the case (2), there exists  $\epsilon > 0$ such that  $(p-\epsilon; p) \cap A = \phi$ . We claim that  $\mu_p = \bigcup_{r \geq p} A_r$ .

If  $x \in \bigcup_{t \geq p} A_t$ , then  $x \in A_t$  for some  $t \geq p$ . It follows that  $\mu(x) \leq p - \epsilon$  so that  $x \notin \mu_p$  Conversely if  $x \notin \mu_p$ ,  $\mu_p = \bigcup_{t \geq p} A_t$ 

then  $x \notin A_t$  for all  $t \ge p$ , which implies that  $x \notin A_t$  for all  $t > p - \epsilon$ , that is, if  $x \in A_t$  then  $t \le p - \epsilon$ . Thus  $\mu(x) \le p - \epsilon$  and so  $x \notin \mu_p$ . Consequently  $\mu_p = \mu_p = \bigcup_{i \in I} A_i$  At which is a fuzzy left (resp. right) sub near-field space of a  $\Gamma$ -near-field

space over a near-field of M. This completes the proof.

**Definition 3.10:** Let M and N be Γ-near-field spaces over near-field. A mapping  $\theta$ : M $\rightarrow$ N is called a Γ-near-field space over a near-field homomorphism if  $\theta(x + y) = \theta(x) + \theta(y)$  and  $\theta(x\alpha y) = \theta(x)\alpha\theta(y) \ \forall \ x, y \in M$  and  $\alpha \in \Gamma$ .

**Theorem 3.11:** A fuzzy Γ-near-field space over near-field homomorphic preimage of a fuzzy left (resp. right) sub nearfield space of a Γ-near-field space over a near-field is a fuzzy left (resp. right) sub near-field space of a Γ-near-field space over a near-field.

**Proof:** Let  $\theta: M \to N$  be a fuzzy  $\Gamma$ -near-field space over near-field homomorphism,  $\nu$  a fuzzy left (resp. right) fuzzy left (resp. right) sub near-field space of a  $\Gamma$ -near-field space over a near-field of N and  $\mu$  the preimage of v under  $\theta$ .

Then  $\mu(x-y) = \nu(\theta(x-y)) = \nu(\theta(x)-\theta(y)) \ge \min\{\nu(\theta(x)); \nu(\theta(y)) = \min\{\mu(x); \mu(y); \mu(y)\}\}$  $\mu(y+x-y) = \nu(\theta(y+x-y)) = \nu(\theta(y)+\theta(x)-\theta(y)) \ge \nu(\theta(x)) = \mu(x);$  and  $\mu(u\alpha(x+v)-u\alpha v)=\nu(\theta(u\alpha(x+v)-u\alpha v))=\nu(\theta(u)\alpha(\theta(x)+\theta(v))-\theta(u)\alpha\theta(v))\geq\nu(\theta(x))=\mu(x) \text{ (resp. }\mu(x\alpha u)=x^{2}+y^{$  $v(\theta(x\alpha u)) = v(\theta(x)\alpha\theta(u)) \ge v(\theta(x)) = \mu(x)$   $\forall x, y, u, v \in M$  and  $\mu \in \Gamma$ . Hence  $\mu$  is a fuzzy left (resp. right) sub nearfield space of a  $\Gamma$ -near-field space over a near-field of M.

Let  $\theta: M \to N$  be a fuzzy  $\Gamma$ -near-field space over near-field homomorphism. Assume that  $\mu$  is a fuzzy left sub nearfield space of a  $\Gamma$ -near-field space over a near-field of M with the sup property and let  $\nu$  be the image of  $\mu$  under  $\theta$ . Given  $\theta(x)$ ;  $\theta(y) \in \theta(M)$ , let  $x_0 \in \theta^{-1}(\theta(x))$ ,  $y_0 \in \theta^{-1}(\theta(y))$ ,  $u_0 \in \theta^{-1}(\theta(u))$  and

Given 
$$\theta(x)$$
;  $\theta(y) \in \theta(M)$ , let  $x_0 \in \theta^{-1}(\theta(x))$ ,  $y_0 \in \theta^{-1}(\theta(y))$ ,  $u_0 \in \theta^{-1}(\theta(u))$  and 
$$v_0 \in \theta^{-1}(\theta(v)) \text{ be such that } \mu(x_0) = \begin{cases} Sup & \mu(z) \\ z \in \theta^{-1}(\theta(x)) \end{cases}, \mu(y_0) = \begin{cases} Sup & \mu(z) \\ z \in \theta^{-1}(\theta(y)) \end{cases}, \mu(u_0) = \begin{cases} Sup & \mu(z) \\ z \in \theta^{-1}(\theta(y)) \end{cases}$$

$$\mu(u_0) = \begin{cases} Sup & \mu(z) \\ z \in \theta^{-1}(\theta(u)) \end{cases} \text{ and } \mu(v_0) = \begin{cases} Sup & \mu(z) \\ z \in \theta^{-1}(\theta(v)) \end{cases} \text{ respectively.}$$
Then

Then 
$$v(\theta(x) - \theta(y)) = \frac{Sup \ \mu(z)}{z \in \theta^{-1}(\theta(x) - \theta(y))} \ge \mu(x_0) - \mu(y_0) \ge \min\{\mu(x_0), \mu(y_0)\}$$

$$= \min \left\{ \begin{cases} Sup \ \mu(z) & Sup \ \mu(z) \\ z \in \theta^{-1}(\theta(x)), z \in \theta^{-1}(\theta(y)) \end{cases} \right\}$$

$$= \min \left\{ v(\theta(x)), v(\theta(y)), z \in \theta^{-1}(\theta(y)) \right\}$$

$$= \min \left\{ v(\theta(x)), v(\theta(y)), z \in \theta^{-1}(\theta(y)) \right\}$$

$$= \min \left\{ v(\theta(x)), v(\theta(y)), z \in \theta^{-1}(\theta(y)) \right\}$$

$$= \min \left\{ v(\theta(x)), v(\theta(y)), z \in \theta^{-1}(\theta(x)) \right\}$$

$$= \sup_{z \in \theta^{-1}(\theta(x)) + \theta(x) - \theta(y)} \ge \mu(x_0) = \begin{cases} Sup \ \mu(z) \\ z \in \theta^{-1}(\theta(x)) + \theta(x) - \theta(y) \end{cases}$$
and for any  $\alpha \in \Gamma$ ,  $v(\theta(u)\alpha(\theta(x) + \theta(v)) - \theta(u)\alpha(\theta(v)) = \begin{cases} Sup \ \mu(z) \\ z \in \theta^{-1}(\theta(u)\alpha(x) + \theta(v) - \theta(u)) \end{cases}$ 

$$\ge \mu(u_0\alpha(x_0 + v_0) - u_0\alpha v_0) \ge \mu(x_0) = \begin{cases} Sup \ \mu(z) \\ z \in \theta^{-1}(\theta(x)) = v(\theta(x)). \end{cases}$$

This proves that  $\nu$  is a fuzzy left sub near-field space of a  $\Gamma$ -near-field space over a near-field of N. Similarly if  $\mu$  is a fuzzy right sub near-field space of a  $\Gamma$ -near-field space over a near-field of M with the sup property, then the image  $\nu$  of  $\mu$  under  $\theta$  is a fuzzy right sub near-field space of a  $\Gamma$ -near-field space over a near-field of N. This completes the proof of the theorem.

**Theorem 3.12:** A fuzzy  $\Gamma$ -near-field space over near-field homomorphic image of a fuzzy left (resp. right) sub near-field space of a  $\Gamma$ -near-field space over a near-field of M possessing the sup property is a fuzzy left (resp. right) sub near-field space of a  $\Gamma$ -near-field space over a near-field.

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