Volume 9, No. 1, Jan. - 2018 (Special Issue) International Journal of Mathematical Archive-9(1), 2018, 47-53 MAAvailable online through www.ijma.info ISSN 2229 - 5046

ON INTUITIONISTIC b - OPEN SETS

A. PRABHU¹, A. VADIVEL² AND J. SATHIYARAJ³

¹Research Scholar, Annamalai University, Annamalai Nagar, Chidambaram, Cuddalore 608001.

^{2,3}Assistant Professor, Department of Mathematics, Government Arts College (Autonomous), Karur – 639005,

E- mail: 1983mrp@gmail.com¹, avmaths@gmail.com²

ABSTRACT

In this paper, we introduce a new types of sets called intuitionistic b-open sets in intuitionistic topological space. Also intuitionistic b-interior and intuitionistic b-closure of an intuitionistic sets are defined and their properties are investigated with other existing forms of intuitionistic open sets.

Key words and phrases: Intuitionistic b-open (closed) sets, intuitionistic b-interior and intuitionistic b-closure.

AMS (2000) subject classification: 54A99.

1. INTRODUCTION

Ever since the introduction of fuzzy sets by Zadeh [8], the fuzzy concept has invaded almost all branches of mathematics, Atanassov [2], introduced the notion of intuitionistic fuzzy sets. Using this notion Coker [[3], [4], [5]] defined and studied intuitionistic topological spaces, intuitionistic open sets, intuitionistic closed sets and compactness on intuitionistic topological spaces. Also, he defined the closure and interior operators in intuitionistic topological spaces and established their properties. Many different forms of open sets have been introduced over the years in general topology. Andrijevic [1] introduced and studied about b-open sets in general topology. Palaniswamy $et\ al.$, [7] introduced the concept of intuitionistic semi-open, intuitionistic α -open, intuitionistic pre-open and intuitionistic β -open sets in 2016. In this paper, is to define and study the intuitionistic b-open sets in intuitionistic topological spaces. Also some properties of these are discussed.

2. PRELIMINARIES

The following definitions and results are essential to proceed further.

Definition 2.1: [3] Let X be a non empty fixed set. An intuitionistic set (briefly. IS) A is an object of the form $A = (X, A_1, A_2)$, where A_1 and A_2 are subsets of X satisfying $A_1 \cap A_2 = \emptyset$. The set A_1 is called the set of members of A, while A_2 is called the set of non-members of A.

The family of all IS 's in X will be denoted by IS(X). Every crisp set A on a non-empty set X is obviously an intuitionistic set.

Definition 2.2: [3] Let X be a non-empty set, $A = (X, A_1, A_2)$ and $B = (X, B_1, B_2)$ be intuitionistic sets on X, then

1. $A \subseteq B$ if and only if $A_1 \subseteq B_1$ and $B_2 \subseteq A_2$.

International Journal of Mathematical Archive- 9(1), Jan. – 2018

47

CONFERENCE PAPER

- 2. A = B if and only if $A \subseteq B$ and $B \subseteq A$.
- 3. $A \subset B$ if and only if $A_1 \cup A_2 \supseteq B_1 \cup B_2$.
- 4. $\overline{A} = (X, A_2, A_1).$
- 5. $A \cup B = (X, A_1 \cup B_1, A_2 \cap B_2)$.
- 6. $A \cap B = (X, A_1 \cap B_1, A_2 \cup B_2)$.
- 7. $A-B=A\cap \overline{B}$
- 8. $\widetilde{\phi} = (X, \phi, X)$ and $\widetilde{X} = (X, X, \phi)$

Corollary 2.1: [3] Let A, B, C and A_i be IS 's in X. Then

- 1. $A_i \subseteq B$ for each i implies that $\bigcup A_i \subseteq B$.
- 2. $B \subseteq A_i$ for each i implies that $B \subseteq \bigcap A_i$.
- 3. $\overline{\bigcup} A_i = \bigcap \overline{A}_i$ and $\overline{\bigcap} A_i = \bigcup \overline{A}_i$.
- 4. $A \subseteq B \Leftarrow \overline{B} \subseteq \overline{A}$.
- 5. $\overline{(\overline{A})} = A, \overline{\widetilde{\phi}} = \widetilde{X} \text{ and } \overline{\widetilde{X}} = \widetilde{\phi}$

Definition 2.3: [5] An intuitionistic topology (briefly IT) on a non-empty set X is a family τ of IS 's in X satisfying the following axioms

- 1. $\widetilde{\phi}$, $\widetilde{X} \in \tau$.
- 2. $A \cap B \in \tau$ for any $A, B \in \tau$.
- 3. $A_i \in \tau$ for an arbitrary family in τ .

In this case the pair (X,τ) is called intuitionistic topological space (briefly ITS) and the IS 's in τ are called the intuitionistic open set in X denoted by $I^{(\tau)}O$ and the complement of an $I^{(\tau)}O$ is called Intuitionistic closed set in X denoted by $I^{(\tau)}C$. The family of all $I^{(\tau)}O$ (resp. $I^{(\tau)}C$) sets in X will be denoted by $I^{(\tau)}O(X)$ (resp. $I^{(\tau)}C(X)$.)

Definition 2.4: [5] Let (X,τ) be an ITS and $A \in IS(X)$. Then the intuitionistic interior (resp. intuitionistic closure) of A are defined by $int(A) = \bigcup \{K : K \in I^{(\tau)}O(X) \text{ and } K \subseteq A\}$ (resp. $cl(A) = \bigcap \{K : K \in I^{(\tau)}C(X) \text{ and } A \subseteq K\}$)

In this study we use $I^{(\tau)}i(A)$ (resp. $I^{(\tau)}c(A)$) instead of int(A) (resp. cl(A)).

Definition 2.5: Let (X,τ) be an ITS and an IS A in X is said to be

- 1. intuitionistic regular-open [6] (briefly $I^{(\tau)}RO$) if $A = I^{(\tau)}i(I^{(\tau)}c(A))$ and intuitionistic regular-closed (briefly $I^{(\tau)}RC$) if $I^{(\tau)}c(I^{(\tau)}i(A)) = A$.
- 2. intuitionistic pre-open [6] (briefly $I^{(\tau)}PO$) if $A \subseteq I^{(\tau)}i(I^{(\tau)}c(A))$ and intuitionistic pre-closed (briefly $I^{(\tau)}PC$) if $I^{(\tau)}c(I^{(\tau)}i(A)) \subseteq A$.
- 3. intuitionistic semi-open [6] (briefly $I^{(\tau)}SO$) if $A \subseteq I^{(\tau)}c(I^{(\tau)}i(A))$ and intuitionistic semi-closed (briefly $I^{(\tau)}SC$) if $I^{(\tau)}i(I^{(\tau)}c(A)) \subseteq A$.
- 4. intuitionistic α -open [7] (briefly $I^{(\tau)}\alpha O$) if $A\subseteq I^{(\tau)}i(I^{(\tau)}c(I^{(\tau)}i(A)))$ and intuitionistic α -closed (briefly $I^{(\tau)}\alpha C$) if $I^{(\tau)}c(I^{(\tau)}i(I^{(\tau)}c(A)))\subseteq A$.

© 2018, IJMA. All Rights Reserved

5. intuitionistic β -open [7] (briefly $I^{(\tau)}\beta O$) if $A \subseteq I^{(\tau)}c(I^{(\tau)}i(I^{(\tau)}c(A)))$ and intuitionistic β -closed (briefly $I^{(\tau)}\beta C$) if $I^{(\tau)}i(I^{(\tau)}c(I^{(\tau)}i(A))) \subseteq A$.

The family of all $I^{(\tau)}RO$ (resp. $I^{(\tau)}RC$, $I^{(\tau)}PO$, $I^{(\tau)}PC$, $I^{(\tau)}SO$, $I^{(\tau)}SC$, $I^{(\tau)}\alpha O$, $I^{(\tau)}\alpha C$, $I^{(\tau)}\beta O$ and $I^{(\tau)}\beta C$) sets in X will be denoted by $I^{(\tau)}RO(X)$ (resp. $I^{(\tau)}RC(X)$, $I^{(\tau)}PO(X)$, $I^{(\tau)}PC(X)$, $I^{(\tau)}SO(X)$, $I^{(\tau)}SC(X)$, $I^{(\tau)}\alpha O(X)$, $I^{(\tau)}\alpha O(X)$, $I^{(\tau)}\beta O(X)$ and $I^{(\tau)}\beta C(X)$.)

Definition 2.6: [6, 7] Let (X, τ) be an ITS and A be an IS(X), then

1. intuitionistic regular-interior (resp. intuitionistic pre- interior, intuitionistic semi-interior, intuitionistic α -interior and intuitionistic β -interior) of A is the union of all $I^{(\tau)}RO(X)$ (resp. $I^{(\tau)}PO(X)$, $I^{(\tau)}SO(X)$, $I^{(\tau)}\alpha O(X)$ and $I^{(\tau)}\beta O(X)$) contained in A, and is denoted by $I^{(\tau)}Ri(A)$ (resp. $I^{(\tau)}Pi(A)$, $I^{(\tau)}Si(A)$, $I^{(\tau)}\alpha i(A)$ and $I^{(\tau)}\beta i(A)$.

i.e.
$$I^{(\tau)}Ri(A) = \bigcup \{G : G \in I^{(\tau)}RO(X) \text{ and } G \subseteq A\},$$

$$I^{(\tau)}Pi(A) = \bigcup \{G : G \in I^{(\tau)}PO(X) \text{ and } G \subseteq A\},$$

$$I^{(\tau)}Si(A) = \bigcup \{G : G \in I^{(\tau)}SO(X) \text{ and } G \subseteq A\},$$

$$I^{(\tau)}\alpha i(A) = \bigcup \{G : G \in I^{(\tau)}\alpha O(X) \text{ and } G \subseteq A\},$$

$$I^{(\tau)}\beta i(A) = \bigcup \{G : G \in I^{(\tau)}\beta O(X) \text{ and } G \subseteq A\}.$$

- 2. intuitionistic regular-closure (resp. intuitionistic pre-closure, intuitionistic semi-closure, intuitionistic α -closure, intuitionistic β -closure) of A is the intersection of all $I^{(\tau)}RC(X)$ (resp. $I^{(\tau)}PC(X)$, $I^{(\tau)}SC(X)$, $I^{(\tau)}\alpha C(X)$, $I^{(\tau)}\beta C(X)$) containing A, and is denoted by $I^{(\tau)}Rc(A)$ (resp. $I^{(\tau)}Pc(A)$, $I^{(\tau)}Sc(A)$, $I^{(\tau)}\alpha c(A)$, $I^{(\tau)}\beta c(A)$.)
 - i.e. $I^{(\tau)}Rc(A) = \bigcap \{G : G \in I^{(\tau)}RC(X) \text{ and } G \supseteq A\},$ $I^{(\tau)}Pc(A) = \bigcap \{G : G \in I^{(\tau)}PC(X) \text{ and } G \supseteq A\}$ $I^{(\tau)}Sc(A) = \bigcap \{G : G \in I^{(\tau)}SC(X) \text{ and } G \supseteq A\},$ $I^{(\tau)}\alpha c(A) = \bigcap \{G : G \in I^{(\tau)}\alpha C(X) \text{ and } G \supseteq A\},$ $I^{(\tau)}\beta c(A) = \bigcap \{G : G \in I^{(\tau)}\beta C(X) \text{ and } G \supseteq A\}.$

Proposition 2.1: [7] Let $A \in IS(X)$, then

- 1. $I^{(\tau)}S(iA) = A \cap I^{(\tau)}c(I^{(\tau)}i(A)).$
- 2. $I^{(\tau)}Pi(A) = A \cap I^{(\tau)}i(I^{(\tau)}c(A)).$
- 3. $I^{(\tau)}S(A) = A \cup I^{(\tau)}i(I^{(\tau)}c(A)).$
- 4. $I^{(\tau)}Pc(A) = A \cup I^{(\tau)}c(I^{(\tau)}i(A)).$
- 5. $I^{(\tau)}Pc(I^{(\tau)}Pi(A)) = I^{(\tau)}Pi(A) \cup I^{(\tau)}c(I^{(\tau)}i(A)).$

3. ON INTUITIONISTIC b-OPEN SETS

Here intuitionistic b-open sets is defined and its relation with existing intuitionistic sets and basic properties are studied.

Definition 3.1: A subset A of an intuitionistic topological space X is said to be

- 1. intuitionistic (briefly $I^{(\tau)}bO$) b-open set if $A \subseteq I^{(\tau)}i(I^{(\tau)}c(A)) \cup I^{(\tau)}c(I^{(\tau)}i(A))$.
- 2. intuitionistic b-closed (briefly $I^{(\tau)}bC$) set if $I^{(\tau)}i(I^{(\tau)}c(A)) \cap I^{(\tau)}c(I^{(\tau)}i(A)) \subset A$.

© 2018, IJMA. All Rights Reserved

The family of all intuitionistic b-open (resp. b-closed) in X will be denoted by $I^{(\tau)}bO(X)$ (resp. $I^{(\tau)}bC(X)$.)

Remark 3.1 The complement of intuitionistic b-open sets are intuitionistic b-closed.

Theorem 3.1:

- 1. Every intuitionistic regular open (resp. open, semi-open, pre-open and α -open) set is intuitionistic b -open.
- 2. Every intuitionistic b-open set is intuitionistic β -open.

Proof:

1. Let
$$A \in I^{(\tau)}RO(X)$$
, this implies that $A = I^{(\tau)}i(I^{(\tau)}c(A))$ which gives $A \subset I^{(\tau)}i(I^{(\tau)}c(A)) \cup I^{(\tau)}c(I^{(\tau)}i(A))$.

Let
$$A \in I^{(\tau)}O(X)$$
, this implies that $A = I^{(\tau)}i(A)$ which gives $A \subseteq I^{(\tau)}c(I^{(\tau)}i(A))$ and also $A \subseteq I^{(\tau)}i(I^{(\tau)}c(A)) \cup I^{(\tau)}c(I^{(\tau)}i(A))$.

Let
$$A \in I^{(\tau)}SO(X)$$
, this implies that $A \subseteq I^{(\tau)}c(I^{(\tau)}i(A))$ which gives $A \subseteq I^{(\tau)}i(I^{(\tau)}c(A)) \cup I^{(\tau)}c(I^{(\tau)}i(A))$.

Let
$$A \in I^{(\tau)}PO(X)$$
, this implies that $A \subseteq I^{(\tau)}i(I^{(\tau)}c(A))$ which gives $A \subseteq I^{(\tau)}i(I^{(\tau)}c(A)) \cup I^{(\tau)}c(I^{(\tau)}i(A))$.

Let
$$A \in I^{(\tau)} \alpha O(X)$$
, this implies that $A \subseteq I^{(\tau)} i(I^{(\tau)} c(I^{\tau} i(A)))$ which gives $A \subseteq I^{(\tau)} i(I^{(\tau)} c(A)) \cup I^{(\tau)} c(I^{(\tau)} i(A))$.

2. Let $A \in I^{(\tau)}bO(X)$, this implies that $A \subseteq I^{(\tau)}i(I^{(\tau)}c(A)) \cup I^{(\tau)}c(I^{(\tau)}i(A))$, that is either $A \subseteq I^{(\tau)}i(I^{(\tau)}c(A))$ or $A \subseteq I^{(\tau)}c(I^{(\tau)}i(A))$, in the first case, it is direct that $A \in i^{(\tau)}\beta O(X)$ and in the other case using $A \subseteq I^{(\tau)}c(A)$ implies the remaining notion.

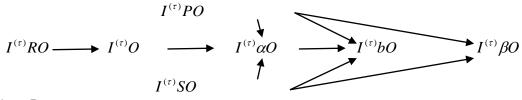
The converse of above theorem need not be true. It can be seen in the following examples.

Example 3.1: Let $X = \{a,b,c\}$ and $\tau = \{(X,\phi,X),(X,X,\phi),(X,\phi,\{a,b\}), (X,\phi,\{b\}), (X,\phi,\{b,c\}), (X,\{c\},\{a,b\}),(X,\{c\},\{b\}),(X,\{a,c\},\{b\})\}$. Then the IS

- 1. $(X,\{b\},\{c\}) \in I^{(\tau)}bO(X)$ but $(X,\{b\},\{c\}) \notin I^{(\tau)}RO(X)$.
- 2. $(X,\{b\},\{c\}) \in I^{(\tau)}bO(X)$ but $(X,\{b\},\{c\}) \notin I^{(\tau)}OS(X)$.
- 3. $(X,\{b,c\},\{a\}) \in I^{(\tau)}bO(X)$ but $(X,\{b\},\{c\}) \notin I^{(\tau)}PO(X)$.
- 4. $(X,\{b,c\},\phi) \in I^{(\tau)}bO(X)$ but $(X,\{b\},\{c\}) \notin I^{(\tau)}\alpha O(X)$.

Example 3.2: Let $X = \{a,b\}$ and $\tau = \{(X,\phi,X),(X,X,\phi),(X,\{a\},\phi)\}$ then the IS $(X,\{a\},\{b\}) \in I^{(\tau)}bO(X)$ but $(X,\{b\},\{c\}) \notin I^{(\tau)}SO(X)$.

The following diagram shows that the relationship between $I^{(\tau)}bO$ and some other intuitionistic sets.



 $A \rightarrow B$ represents A implies B, but not conversely.

© 2018, IJMA. All Rights Reserved

Theorem 3.2: Let (X,τ) be an ITS and $\{A_i\}_{i\in J}$ be any arbitrary family of members from $I^{(\tau)}bO(X)$ then $\bigcup A_i \in I^{(\tau)}bO(X)$.

Proof. Let $A_i \in I^{(\tau)}bO(X)$ then $A_i \subseteq I^{(\tau)}c(I^{(\tau)}i(A_i)) \cup I^{(\tau)}i(I^{(\tau)}c(A_i))$. Now we decompose the family into two sub families such that $B_i = \{K : K \text{ is a member } inA_i \text{ and } K \subseteq I^{(\tau)}c(I^{(\tau)}i(K))\}$ and $C_i = \{G : G \text{ is a member } in A_i \text{ and } G \subseteq I^{(\tau)}i(I^{(\tau)}c(G))\}$ Clearly $\bigcup A_i = (\bigcup B_i) \cup (\bigcup C_i)$ and we have $\bigcup B_i \in I^{(\tau)}SO(X)$ and $\bigcup C_i \in I^{(\tau)}PO(X)$. Union of an $I^{(\tau)}SO$ and $I^{(\tau)}PO$ is in $I^{(\tau)}bO(X)$.

Corollary 3.1: Let (X,τ) be an ITS and $\{A_i\}_{i\in J}$ be any arbitrary family of members from $I^{(\tau)}bC(X)$ then $\bigcap A_i \in I^{(\tau)}bC(X)$.

Remark 3.2: The intersection of two $I^{(\tau)}bO(X)$ need not be $I^{(\tau)}bO(X)$ as shown by the following example.

Example 3.3: Let $X = \{a,b,c\}$ and $\tau = \{(X,\phi,X),(X,X,\phi),(X,\{\phi\},\{b\}),(X,\{\phi\},\{a,b\}),(X,\{\phi\},\{a,b\}),(X,\{c\},\{a,b\}),(X,\{c\},\{b\}),(X,\{a,c\},\{b\})\}$ then the IS $(X,\{\phi\},\{a\})$ and $(X,\{\phi\},\{c\})$ are $I^{(\tau)}bO(X)$ but the intersection $(X,\{\phi\},\{a,c\})$ is not a b-open.

Theorem 3.3: Let (X,τ) be an ITS and $A \subset X$, then

- 1. $(I^{(\tau)}bc(A))^C = I^{(\tau)}bi(A^C)$.
- 2. $(I^{(\tau)}bi(A))^C = I^{(\tau)}bc(A^C)$.

Proof.

(i) Let $A \in IS(X)$ and (X, τ) be an ITS. Now $I^{(\tau)}bc(A) = \bigcap \{G : G \in I^{(\tau)}bC(X) \text{ and } G \supseteq A\}$ $(I^{(\tau)}bc(A))^C = \left[\bigcap \{G : G \in I^{(\tau)}bC(X) \text{ and } G \supseteq A\}\right]^C$ $= \bigcup \{G^C : G^C \in I^{(\tau)}bO(X) \text{ and } G^C \subseteq A^C\}$ $(I^{(\tau)}bc(A))^C = I^{(\tau)}bi(A^C).$

(ii) The similar proof can be given.

Theorem 3.4 In an ITS (X, τ) , for an $A \in IS(X)$, the following are equivalent:

- 1. $A \in I^{(\tau)}bO(X)$.
- 2. $A = I^{(\tau)}Pi(A) \cup I^{(\tau)}Si(A)$.
- 3. $A \subset I^{(\tau)}Pc(I^{(\tau)}Pi(A))$.

Proof. Let $A \in IS(X)$ in an $ITS(X, \tau)$

(i)
$$\Rightarrow$$
 (ii): Suppose that $A \in I^{(\tau)}bO(X)$, so that $A \subseteq I^{(\tau)}c(I^{(\tau)}i(A)) \cup I^{(\tau)}i(I^{(\tau)}c(A))$. Now,
$$I^{(\tau)}Pi(A) \cup I^{(\tau)}Si(A) = (A \cap I^{(\tau)}i(I^{(\tau)}c(A))) \cup (A \cap I^{(\tau)}c(I^{(\tau)}i(A)))$$
$$= A \cap (I^{(\tau)}i(I^{(\tau)}c(I^{(\tau)}i(A))))$$
$$= A.$$

$$A = I^{(\tau)}Pi(A) \cup I^{(\tau)}Si(A)$$

$$= I^{(\tau)}Pi(A) \cup (A \cap I^{(\tau)}c(I^{(\tau)}i(A)))$$

$$\subseteq I^{(\tau)}Pi(A) \cup I^{(\tau)}c(I^{(\tau)}i(A))$$

$$= I^{(\tau)}Pc(I^{(\tau)}Pi(A))$$
i.e., $A \subseteq I^{(\tau)}Pc(I^{(\tau)}Pi(A))$.

(iii) ⇒ (i): Consider

$$A \subseteq I^{(\tau)}Pc(I^{(\tau)}Pi(A))$$

$$= I^{(\tau)}Pi(A) \cup I^{(\tau)}c(I^{(\tau)}i(A))$$

$$= (A \cap I^{(\tau)}i(I^{(\tau)}c(A))) \cup I^{(\tau)}c(I^{(\tau)}i(A))$$

$$\subseteq I^{(\tau)}i(I^{(\tau)}c(A)) \cup I^{(\tau)}c(I^{(\tau)}i(A))$$

$$A \subseteq I^{(\tau)}i(I^{(\tau)}c(A)) \cup I^{(\tau)}c(I^{(\tau)}i(A))$$
i.e., $A \in I^{(\tau)}bO(X)$.

This completes the proof.

Theorem 3.5: Let A be an IS in X, then

1.
$$I^{(\tau)}bi(A) = I^{(\tau)}Si(A) \cup I^{(\tau)}Pi(A)$$

2.
$$I^{(\tau)}bc(A) = I^{(\tau)}Sc(A) \cap I^{(\tau)}Pc(A)$$
.

Proof:

(a) Let
$$A \in IS(X)$$
, (X, τ) be an ITS . Since $I^{(\tau)}bi(A) \in I^{(\tau)}bO(X)$, we have, $I^{(\tau)}bi(A) \subseteq I^{(\tau)}c(I^{(\tau)}i(I^{(\tau)}bi(A))) \cup I^{(\tau)}i(I^{(\tau)}c(I^{(\tau)}bi(A)))$
$$\subseteq I^{(\tau)}c(I^{(\tau)}i(A)) \cup I^{(\tau)}i(I^{(\tau)}c(A))$$

$$A \cap I^{(\tau)}bi(A) \subseteq A \cap [I^{(\tau)}c(I^{(\tau)}i(A)) \cup I^{(\tau)}i(I^{(\tau)}c(A))]$$

$$= [A \cap I^{(\tau)}c(I^{(\tau)}i(A))] \cup [A \cap I^{(\tau)}i(I^{(\tau)}c(A))]$$

$$= I^{(\tau)}Si(A) \cup I^{(\tau)}Pi(A) \quad (by\ Proposition(2.1))$$

$$I^{(\tau)}bi(A) \subset I^{(\tau)}Si(A) \cup I^{(\tau)}Pi(A).$$

But
$$I^{(\tau)}Si(A) \subseteq I^{(\tau)}bi(A)$$
 and $I^{(\tau)}Pi(A) \subseteq I^{(\tau)}bi(A)$, hence $I^{(\tau)}Si(A) \cup I^{(\tau)}Pi(A) \subseteq I^{(\tau)}bi(A)$.
Therefore $I^{(\tau)}bi(A) = I^{(\tau)}Si(A) \cup I^{(\tau)}Pi(A)$.

(b) Since
$$I^{(\tau)}bc(A) \in I^{(\tau)}bC(X)$$
, we have,

$$\begin{split} &I^{(\tau)}c(I^{(\tau)}i(I^{(\tau)}bc(A))) \cap I^{(\tau)}i(I^{(\tau)}c(I^{(\tau)}bc(A))) \subseteq I^{(\tau)}bc(A) \\ &I^{(\tau)}c(I^{(\tau)}i(A)) \cap I^{(\tau)}i(I^{(\tau)}c(A)) \subseteq I^{(\tau)}c(I^{(\tau)}bc(A))) \cap I^{(\tau)}i(I^{(\tau)}c(I^{(\tau)}bc(A))) \subseteq I^{(\tau)}bc(A) \\ &A \cup [I^{(\tau)}c(I^{(\tau)}i(A)) \cap I^{(\tau)}i(I^{(\tau)}c(A))] \subseteq A \cup I^{(\tau)}bc(A) \cap [A \cup I^{(\tau)}i(I^{(\tau)}c(A))] \subseteq I^{(\tau)}bc(A) \\ &I^{(\tau)}Sc(A) \cap I^{(\tau)}Pc(A) \subseteq I^{(\tau)}bc(A). \quad (by\ Proposition(2.1)) \end{split}$$

But
$$I^{(\tau)}bc(A) \subseteq I^{(\tau)}Sc(A)$$
 and $I^{(\tau)}bc(A) \subseteq I^{(\tau)}Pc(A)$, hence $I^{(\tau)}bc(A) \subseteq I^{(\tau)}Sc(A) \cap I^{(\tau)}Pc(A)$. Therefore $I^{(\tau)}bc(A) = I^{(\tau)}Sc(A) \cup I^{(\tau)}Pc(A)$.

REFERENCES

- 1. Andrijevic D., *On b-open sets*, Mat. Vesnik, 48 (1996), 59-64.
- 2. Atanassov K., Intuitionistic fuzzy sets, Fuzzy Sets and Systems, 20 (1)(1986), 84-96.
- 3. Coker D., A note on intuitionistic sets and intuitionistic points, Turkish Journal of Mathematics, 20 (3) (1996), 343-351.
- 4. Coker D., An introduction to intuitionistic fuzzy topological spaces, Fuzzy Sets and Systems, 88 (1997), 81-89.
- 5. Coker D., An introduction to intuitionistic topological spaces, BUSEFAL, 81 (2000), 51-56.
- 6. Girija S. and Ilango G, *Some more results on intuitionistic semi open sets*, Int. Journal of Engineering Research and Applications, 4(11) (2014), 70-74.
- 7. Palaniswamy B. and Varadharajan K.., On $I^{(\tau)}\alpha$ -open set and $I^{(\tau)}\beta$ -open set in intuitionistic topological spaces, Maejo International Journal of Science and Technology, 10 (2) (2016), 187-196.
- 8. Zadeh L. A., Fuzzy sets, Information and Control, 8 (1965), 338-353.

Source of support: Proceedings of UGC Funded International Conference on Intuitionistic Fuzzy Sets and Systems (ICIFSS-2018), Organized by: Vellalar College for Women (Autonomous), Erode, Tamil Nadu, India.