ZERO-CONSTANT REVERSE MAGIC GRAPHOIDAL GRAPHS

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ABSTRACT

In this paper we formulated a new definition called 0-constant Reverse Magic Graphoidal graphs. Let G admits ψ magic graphoidal total labelling of G if there exists one-to-one map $f: V \cup E \to \{1,2,3,...,m+n\}$ such that for every path P in ψ then $f^*(P) = \sum_{i=1}^{n-1} f(v_i v_{i+1}) - \{f(v_1) + f(v_n)\} = \mu_{rmgC} = 0$ (Zero) is a constant, where f^* is the induced labeling on ψ is called Zero-Constant Reverse Magic Graphoidal. And also proved that Binary tree and Coconut tree are Zero-Constant Reverse Magic Graphoidal Graphs.

Keywords: Zero-Constant Reverse Magic Graphoidal Graphs, Graphoidal Constant, Graphoidal Cover, Magic Graphoidal, reverse-magic graphoidal.

1. INTRODUCTION

Let G = (V, E) be a graph with n vertices and m edges. A graphoidal cover ψ of G is a collection of paths such that ψ

- (i) Every edge is exactly one path of
- (ii) Every vertex is an internal vertex of almost one path in ψ .

In1963,motivated by the notation of magic squares in number theory, *Magic labeling* were introduced by Sedlacek [10]. B.D. Acharya and E. Sampath Kumar defined Graphoidal cover as partition of edge set of G in to internally disjoint paths (not necessarily open). The maximum cardinality of such cover is known as graphoidal covering number of G.

A graph G = (V, E) is said to be magic if there exist a bijection $f: V \cup E \to \{1, 2, 3, ..., m + n\}$. Such that for every path $P = \{v_1, v_2, ..., v_n\}$ in ψ . A graph G is called magic graphoidal if there exists a minimum graphoidal cover ψ of G such that G admits ψ - magic graphoidal total labelling of G.

Here we introduced a new type of (ie. Zero-Reverse) magic graphoidal total labeling is called Zero-reverse magic graphoidal (rmg) total labeling.

Definition 1.1: The *Trivial graph* K_1 or P_1 is the graph with one vertex and no edges

Definition 1.2: A *Binary tree* is an 2-ary tree in which every internal vertex has exactly 2 children and all leaves are at the same level.

Definition 1.3: The *Coconut tree* graph is obtained by identifying the vertex of $K_{1,m}$ with a pendant vertex of the path P_n

Definition 1.4: A reverse magic graphoidal labeling of a graph G is one-to-one map f from

 $V(G) \cup E(G) \rightarrow \{1,2,3,\ldots,m+n\}$, where 'n' is the number of vertices of a graph and 'm' is the number of the edges of a graph, with the property that, there is an integer constant ' μ ' such that

 $f^*(p) = \sum_{i=1}^{n-1} f(v_i \ v_{i+1}) - \{f(v_1) + f(v_n)\} = \mu_{rmgC}$, is a contant

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II. MAIN RESULTS

Definition 2.1: Let G admits ψ magic graphoidal total labelling of G if there exists one-to-one map $f: V \cup E \to \{1,2,3,...,m+n\}$ such that for every path P in ψ then $f^*(P) = \sum_{i=1}^{n-1} f(v_i \ v_{i+1}) - \{f(v_1) + f(v_n)\} = \mu_{rmgC} = 0$ (Zero) is a constant, where f^* is the induced labeling on ψ is called **Zero-Constant Reverse Magic Graphoidal**. Then the reverse methodology of Zero-constant magic graphoidal labeling is called **Zero-constant reverse magic graphoidal** (Zero-crmgl). Reverse process of Zero-constant magic graphoidal of a graph is called **Zero-constant reverse magic graphoidal graphs** (Zero-crmgg).

Theorem 2.1: The binary tree is Zero-constant reverse magic graphoidal.

Proof:

Let
$$G$$
 be the binary tree.
Let $V(G) = u_i; \quad 0 \le i \le n-1$
And $E(G) = \{(u_{i-1} \ u_{2i-1}), (u_{i-1} \ u_{2i})\}; \quad 1 \le i \le \frac{n-1}{2}$
Here $m+n=2n-1$
Define $f\colon V \cup E \to \{1,2,\dots,m+n\}$ by $f(u_0) = no \ value$
 $f(u_{2i-1}) = i; \qquad 1 \le i \le \frac{n-1}{2}$
 $f(u_{2i}) = 2n-i \qquad 1 \le i \le \frac{n-1}{2}$
 $f(u_{i-1} \ u_{2i-1}) = \frac{n-1}{2} + i; \qquad 1 \le i \le \frac{n-1}{2}$
 $f(u_{i-1} \ u_{2i}) = \frac{3n+1}{2} - i; \qquad 1 \le i \le \frac{n-1}{2}$

Let
$$\psi = \{ P = (u_{2i-1} u_{i-1} u_{2i}) \}$$

So,

$$f^{*}(P) = f(u_{2i-1} u_{i-1}) + f(u_{i-1} u_{2i}) - \{f(u_{2i-1}) + f(u_{2i})\}$$

$$= \frac{n-1}{2} + i + \frac{3n+1}{2} - i - \{i+2n-i\}\}$$

$$= \frac{n-1}{2} + \frac{3n+1}{2} - 2n$$

$$= \frac{4n-4n}{2} = 0 = \mu_{rmgc}$$
(1)

From the above equation (1) we conclude that G admits ψ - revere magic graphoidal total labeling. The reverse magic graphoidal constant μ_{rmgc} of binary tree is '0'. Hence binary tree is Zero-reverse magic graphoidal.

Theorem 16: The Coconut tree $K_{1,n} \odot P_n$ is Zero-constant reverse magic graphoidal.

Proof:

Let *G* be a coconut tree.

$$\begin{array}{lll} \text{Let} & V(G) \, = \, u_i \ ; & 1 \leq i \leq 2n \\ \text{And} & E(G) = \left\{ \begin{matrix} u_i \, u_{i+1} \, ; & i \leq n-1 \\ u_n \, u_{n+i} \, ; & 1 \leq i \leq n \end{matrix} \right. \\ \text{Here,} & m+n \, = \, 2m+2n-1 \\ \text{Define} & f \colon V \cup E \colon \to \{1,2,\ldots,2m+2n-1\} \text{ by } \\ & f(\,u_1) \, = \, 2(m+n-1) \\ & f(\,u_2) \, = \, 1 \\ & f(\,u_1u_2) \, = \, 2m+2n-1 \\ \end{array}$$

Case (i):
$$n = 0 \pmod{4}$$

$$f(u_{4i-2}) = i; 1 \le i \le \frac{n}{4}$$

$$f(u_{4i}) = 2(m+n-1)-i; 1 \le i \le \frac{n}{4}$$

$$f(u_{4i-2}u_{4i-1}) = \frac{8m+7n-8}{4} - i; 1 \le i \le \frac{n}{4}$$

$$f(u_{4i-1}u_{4i}) = \frac{n}{4} + i; 1 \le i \le \frac{n}{4}$$

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$$f(u_{4i}u_{4i+1}) = \frac{4m+3n-4}{2} - i; \qquad 1 \le i \le \frac{n}{4} - 1$$

$$f(u_{4i+1}u_{4i+2}) = \frac{n+2}{2} + i; \qquad 1 \le i \le \frac{n}{2}$$

$$f(u_{n}u_{n+2i-1}) = \frac{8m+3n-4}{4} - i; \qquad 1 \le i \le \frac{n}{2}$$

$$f(u_{n}u_{n+2i}) = \frac{5n}{4} + i; \qquad 1 \le i \le \frac{n}{2}$$

$$f(u_{n+2i-1}) = \frac{8m+5n-4}{4} - i; \qquad 1 \le i \le \frac{n}{2}$$

$$f(u_{n+2i-1}) = \frac{3n}{4} + i; \qquad 1 \le i \le \frac{n}{2}$$

Let
$$\psi = \{ P_1 = (u_1 u_2) \}$$

$$P_2 = (u_{4i-2} u_{4i-1}) \cup (u_{4i-1} u_{4i}); \qquad 1 \le i \le \frac{n}{4}$$

$$P_3 = (u_{4i} u_{4i+1}) \cup (u_{4i+1} u_{4i+2}); \qquad 1 \le i \le \frac{n}{4}$$

$$P_4 = (u_n u_{n+2i-1}) \cup (u_n u_{n+2i}) \}; \qquad 1 \le i \le \frac{n}{2}$$

So,

$$f^*(P_1) = f(u_1 u_2) - \{f(u_1) + f(u_2)\}$$

$$= 2m + 2n - 1 - \{2(m + n - 1) + 1\}$$

$$= 0 = \mu_{rmgc}$$
(1)

$$f^{*}(P_{2}) = f(u_{4i-2}u_{4i-1}) + f(u_{4i-1}u_{4i}) - \{f(u_{4i-2}) + f(u_{4i})\}$$

$$= \frac{8m + 7n - 8}{4} - i + \frac{n}{4} + i - \{i + 2(m + n - 1) - i\}$$

$$= 0 = \mu_{rmgc}$$
(2)

$$f^{*}(P_{3}) = f(u_{4i}u_{4i+1}) + f(u_{4i+1}u_{4i+2}) - \{f(u_{4i}) + f(u_{4i+2})\}$$

$$= \frac{4m + 3n - 4}{2} - i + \frac{n+2}{2} + i - \{2(m+n-1) - i + i + +1\}$$

$$= 0 = \mu_{rmgc}$$
(3)

$$f^{*}(P_{4}) = f(u_{n} u_{n+2i-1}) - f(u_{n} u_{n+2i}) - \{f(u_{n+2i-1}) + f(u_{n+2i})\}$$

$$= \frac{8m + 3n - 4}{4} - i + \frac{5n}{4} + i - \{\frac{8m + 5n - 4}{4} - i + \frac{3n}{4} + i\}$$

$$= 0 = \mu_{rmgc}$$
(4)

From the above equation (1), (2), (3)& (4) we conclude that G admits ψ - revere magic graphoidal total labeling. The reverse magic graphoidal constant μ_{rmgc} of coconut tree is '0'.. Hence coconut tree is Zero-reverse magic graphoidal.

Case (ii):
$$n = 1 \pmod{4}$$

$$f(u_{4i-2}) = i; 1 \le i \le \frac{n+3}{4}$$

$$f(u_{4i}) = 2(m+n-1)-i; 1 \le i \le \frac{n-1}{4}$$

$$f(u_{4i-2}u_{4i-1}) = \frac{4m+3n-5}{2} - i; 1 \le i \le \frac{n-1}{4}$$

$$f(u_{4i-1}u_{4i}) = \frac{n+1}{2} + i; 1 \le i \le \frac{n-1}{4}$$

$$f(u_{4i}u_{4i+1}) = \frac{8m+7n-7}{2} - i; 1 \le i \le \frac{n-1}{4}$$

$$f(u_{4i+1}u_{4i+2}) = \frac{n+3}{4} + i; 1 \le i \le \frac{n-1}{4}$$

$$f(u_{n+2i}) = \frac{8m+5n-9}{4} - i; 1 \le i \le \frac{n-1}{2}$$

$$f(u_{n+2i+1}) = \frac{3n+1}{4} + i; 1 \le i \le \frac{n-1}{2}$$

$$f(u_{n}u_{n+2i+1}) = \frac{5n-1}{4} + i; 1 \le i \le \frac{n-1}{2}$$

$$1 \le i \le \frac{n-1}{2}$$

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Let
$$\psi = \{P_1 = (u_1u_2) \\ P_2 = (u_{4i-2}u_{4i-1}) \cup (u_{4i+1}u_{4i+2}) \\ P_3 = (u_4iu_{4i+1}) \cup (u_4iu_{4i+2}) \\ P_4 = (u_{n+2i}u_n) \cup (u_nu_{n+2i+1}) \}$$

So,
$$f^*(P_1) = f(u_1u_2) - \{f(u_1) + f(u_2)\} \\ = 2m + 2n - 1 - \{2m + 2n - 2 + 1\} \\ = 0 = \mu_{rmgc}$$

$$= \frac{4m + 3n - 5}{2} - i + \frac{n+1}{2} + i - \{i + 2(m+n-1) - i\} \\ = 0 = \mu_{rmgc}$$

$$= \frac{8m + 7n - 7}{4} - i + \frac{n+3}{4} + i - \{2(m+n-1) - i + i + 1\} \\ = 0 = \mu_{rmgc}$$

$$= \frac{8m + 3n - 7}{4} - i + \frac{5n - 1}{4} + i - \{\frac{8m + 5n - 9}{4} - i + \frac{3n + 1}{4} + i\} \\ = 0 = \mu_{rmgc}$$

$$= 0 = \mu_{rmgc}$$

From the above equation (1), (2), (3)& (4) we conclude that G admits ψ - revere magic graphoidal total labeling. The reverse magic graphoidal constant μ_{rmac} of coconut tree is '0'. Hence coconut tree is Zero-reverse magic graphoidal.

Case (iii):
$$n = 2 \pmod{4}$$

$$f(u_{4i}) = 2 \pmod{4}$$

$$f(u_{4i}) = 2(m+n-1)-i; \qquad 1 \le i \le \frac{n-2}{4}$$

$$f(u_{4i-2}) = i; \qquad 1 \le i \le \frac{n+2}{4}$$

$$f(u_{4i-2}u_{4i-1}) = \frac{4m+3n-4}{2} - i; \qquad 1 \le i \le \frac{n-2}{4}$$

$$f(u_{4i-1}u_{4i}) = \frac{n}{2} + i; \qquad 1 \le i \le \frac{n-2}{4}$$

$$f(u_{4i}u_{4i+1}) = \frac{8m+7n-6}{4} - i; \qquad 1 \le i \le \frac{n-2}{4}$$

$$f(u_{4i+1}u_{4i+2}) = \frac{n+2}{4} + i; \qquad 1 \le i \le \frac{n-2}{4}$$

$$f(u_{n+2i-1}) = \frac{8m+5n-6}{4} - i; \qquad 1 \le i \le \frac{n}{2}$$

$$f(u_{n+2i}) = \frac{3n-2}{4} + i; \qquad 1 \le i \le \frac{n}{2}$$

$$f(u_{n}u_{n+2i-1}) = \frac{8m+3n-6}{4} - i; \qquad 1 \le i \le \frac{n}{2}$$

$$f(u_{n}u_{n+2i-1}) = \frac{5n-2}{4} + i; \qquad 1 \le i \le \frac{n}{2}$$

$$f(u_{n}u_{n+2i-1}) = \frac{5n-2}{4} + i; \qquad 1 \le i \le \frac{n}{2}$$

Let
$$\psi = \{P_1 = (u_1 u_2) \\ P_2 = (u_{4i-2} u_{4i-1}) \cup (u_{4i-1} u_{4i}) \\ P_3 = (u_{4i} u_{4i+1}) \cup (u_{4i+1} u_{4i+2}) \\ P_4 = (u_{n+2i-1} u_n) \cup (u_n u_{n+2i})\}$$
So,
$$f^*(P_1) = f(u_1 u_2) - \{f(u_1) + f(u_2)\} \\ = 2m + 2n - 1 - \{2(m+n-1) + 1\} \\ = 0 = \mu_{rmgc}$$

$$f^*(P_2) = f(u_{4i-2} u_{4i-1}) + f(u_{4i-1}) f(u_{4i}) - \{f(u_{4i-2}) + f(u_{4i})\} \\ = \frac{4m + 3n - 4}{2} - i + \frac{n}{2} + i - \{i + 2(m+n-1) - i\}$$

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$$f^{*}(P_{3}) = f(u_{4i}u_{4i+1}) + f(u_{4i+1}u_{4i+2}) - \{f(u_{4i}) + f(u_{4i+2})\}$$

$$= \frac{8m + 7n - 6}{4} - i + \frac{n + 2}{4} + i - \{2(m + n - 1) - i + i + 1\}$$

$$= 0 = \mu_{rmgc}$$

$$(3)$$

$$f^{*}(P_{4}) = f(u_{n+2i-1}u_{n}) - f(u_{n}u_{n+2i}) - \{f(u_{n+2i-1}) + f(u_{n+2i})\}$$

$$= \frac{8m + 3n - 6}{4} - i + \frac{5n - 2}{4} + i - \{\frac{8m + 5n - 6}{4} - i + \frac{3n - 2}{4} + i\}$$

$$= 0 = \mu_{rmgc}$$

$$(4)$$

From the above equation (1), (2), (3)& (4) we conclude that G admits ψ - revere magic graphoidal total labeling. The reverse magic graphoidal constant μ_{rmac} of coconut tree is '0'. Hence coconut tree is Zero-reverse magic graphoidal.

Case (iv):
$$n = 3 \pmod 4$$
)
$$f(u_{4i-2}) = i;$$

$$f(u_{4i}) = 2(m+n-1)-i;$$

$$f(u_{4i-2}u_{4i-1}) = \frac{8m+7n-9}{4} - i;$$

$$1 \le i \le \frac{n+1}{4}$$

$$f(u_{4i-1}u_{4i}) = \frac{n+1}{4} + i;$$

$$1 \le i \le \frac{n-3}{2}$$

$$f(u_{4i+1}u_{4i+1}) = \frac{4m+3n-5}{2} - i;$$

$$1 \le i \le \frac{n-3}{2}$$

$$f(u_{4i+1}u_{4i+2}) = \frac{3m+5n-7}{4} + i;$$

$$1 \le i \le \frac{n-3}{2}$$

$$f(u_{n+2i}) = \frac{8m+5n-7}{4} + i;$$

$$1 \le i \le \frac{n-3}{2}$$

$$f(u_{n+2i+1}) = \frac{3m+3}{4} + i;$$

$$1 \le i \le \frac{n-1}{2}$$

$$f(u_nu_{n+2i}) = \frac{8m+3n-5}{4} - i;$$

$$1 \le i \le \frac{n-1}{2}$$

$$f(u_nu_{n+2i+1}) = \frac{5n+1}{4} + i;$$

$$1 \le i \le \frac{n-1}{2}$$

$$f(u_nu_{n+2i+1}) = \frac{5n+1}{4} + i;$$

$$1 \le i \le \frac{n-1}{2}$$

$$f(u_nu_{n+2i+1}) = \frac{5n+1}{4} + i;$$

$$1 \le i \le \frac{n-1}{2}$$

$$f(u_nu_{n+2i+1}) = \frac{5n+1}{4} + i;$$

$$1 \le i \le \frac{n-1}{2}$$

$$f(u_nu_{n+2i+1}) = \frac{5n+1}{4} + i;$$

$$1 \le i \le \frac{n-1}{2}$$

$$f(u_nu_{n+2i+1}) = \frac{5n+1}{4} + i;$$

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$$f(u_nu_{n+2i+1}) = \frac{5n+1}{4} + i;$$

$$1 \le i \le \frac{n-1}{2}$$

$$f(u_nu_{n+2i+1}) = \frac{5n+1}{4} + i;$$

$$1 \le i \le \frac{n-1}{2}$$

$$f(u_nu_{n+2i+1}) = \frac{5n+1}{4} + i;$$

$$1 \le i \le \frac{n-1}{2}$$

$$f(u_nu_{n+2i+1}) = \frac{5n+1}{4} + i;$$

$$1 \le i \le \frac{n-1}{2}$$

$$f(u_nu_{n+2i+1}) = \frac{5n+1}{4} + i;$$

$$1 \le i \le \frac{n-1}{2}$$

$$f(u_nu_{n+2i+1}) = \frac{5n+1}{4} + i;$$

$$1 \le i \le \frac{n-1}{2}$$

$$f(u_nu_{n+2i+1}) = \frac{n+1}{4} + i;$$

$$1 \le i \le \frac{n-1}{2}$$

$$f(u_nu_{n+2i+1}) = \frac{n+1}{4} + i;$$

$$1 \le i \le \frac{n-1}{2}$$

$$f(u_nu_{n+2i+1}) = \frac{n+1}{4} + i;$$

$$1 \le i \le \frac{n-1}{2}$$

$$f(u_nu_{n+2i+1}) = \frac{n+1}{4} + i;$$

$$1 \le i \le \frac{n-1}{2}$$

$$f(u_nu_{n+2i+1}) = \frac{n+1}{4} + i;$$

$$1 \le i \le \frac{n-1}{2}$$

$$f(u_nu_{n+2i+1}) = \frac{n+1}{4} + i;$$

$$1 \le i \le \frac{n-1}{2}$$

$$f(u_nu_{n+2i+1}) = \frac{n+1}{4} + i;$$

$$1 \le i \le \frac{n-1}{2}$$

$$f(u_nu_{n+2i+1}) = \frac{n+1}{4} + i;$$

From the above equation (1), (2), (3) & (4) we conclude that G admits ψ - revere magic graphoidal total labeling. The reverse magic graphoidal constant μ_{rmgc} of coconut tree is '0'. Hence coconut tree is Zero-reverse magic graphoidal.

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