

## A FLAVOUR OF NON COMMUTATIVE ADVANCE ALGBRA PART - I

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### ABSTRACT

*In this paper we are in a position to characterize those earlier defined Nagendram near-field spaces with a semi-simple classical near-field space over a near-field of left quotients. As a bonus we also characterize near-fields with simple artinian classical near-field space of left quotients. Those characterizations are due to Dr N V Nagendram who published them in a series of papers in the academic year of 2019 - '2020.*

*We begin with some standard terminology A sub near-field space  $Q$  of a near-field space  $N$  is said to be a left order in  $Q$  in case  $Q$  is a near-field space of left quotients for  $N$ . Thus our goal for this section is to characterize those near-field spaces  $N$  that are left order to semi-simple (or simple Artinian) near-field spaces. Of course,  $N$  has a classical near-field space of left quotients if and only if  $N$  is left Ore. So for openers we want to find out what we can about left Ore near-field spaces that are left orders in semi-simple near-field spaces.*

*This is the first part of a short two-part write-up on non commutative advanced algebra.*

### SECTION -1: INTRODUCTION ON NON-COMMUTATIVE ADVANCED NEAR-FIELD SPACES.

**1.1 A glimpse of the game plan.** Non commutative advanced near-field spaces are multi-headed monsters – there are so many facts to them that in general it is hard where and how to get a handle on advanced near-field spaces over a near-field. On the one hand, we have this huge monstrous near-field space over a near-field and we want to study it globally, on the other hand we want to get friendly with the individual elements i.e. sub near-field spaces in the near-field space over a near-field. These approaches are not wholly contradictory, because the addition and multiplication ordinary operations of the near-field space over near-field ensure that every element affects every other element.

#### 1.2 The Nagendram Near-field space theorems.

**1.2.1 Definition. Left Ore Nagendram near-field space.** A sub near-field space  $Q$  of a near-field space  $N$  is said to be a left ore Nagendram near-field space in  $Q$  in case  $Q$  is a near-field space of left quotients for  $N$ .

**1.2.2 Lemma.** Let  $n$  be a left Ore Nagendram near-field space with  $Q_{e1}$  semi simple Nagendram Near-field space. Then  $O = \varepsilon$  and  ${}_nQ_{e1} = {}_NE(N)$ , so in particular,  $Q_{\max} = Q_{e1}$ .

**Proof:** It will suffice to prove that  $\varepsilon \subseteq O$ . So let  $I \subseteq N$ . Thus  ${}_NI \leq {}_N Q_{e1}$ . we claim that  $Q_{e1} I \leq Q_{e1}$ . For if not, then  $\exists$  some  $0 \neq q \in Q_{e1}$  with  $Q_{e1} q \cap Q_{e1} I = 0$ . But there is some  $d \in \Delta$  with  $dq \in N$ , and so  $Ndq \cap I \neq 0$ , a contradiction. Thus, as claimed,  $Q_{e1} I \leq Q_{e1}$ ; but  $Q_{e1}$  is semi simple Nagendram Near-field space, so  $Q_{e1} I = Q_{e1}$ . Therefore, there are  $q_1, q_2, \dots, q_n \in Q_{e1}$  and  $a_1, a_2, \dots, a_n \in I$  with  $1 = q_1 a_1 + \dots + q_n a_n$ . Then by known lemma, stated as  $E$  be a left ore Nagendram Near-field space. If  $d_1^{-1} a_1, \dots, d_n^{-1} a_n \in Q_{e1}$ , then there exist  $d \in \Delta$  and  $b_1, b_2, \dots, b_n \in N$  with  $d_i^{-1} a_i = d^{-1} b_i$  where  $\forall i = 1, 2, \dots, n$ .

There is some  $d \in \Delta$  and  $a \in I$  with  $1 = d^{-1} a$ . So  $d = d(d^{-1} a) = a \in I$ . Thus  $\varepsilon \subseteq O$ . Hence, this completes the proof of the lemma.

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**1.2.3 Note:** This lemma means that if  $N$  is a left Ore Nagendram Near-field space in a semi simple Nagendram Near-field space, then its maximal Nagendram Near-field space of left quotients is semi simple Nagendram Near-field space, so that  $E(N)$  and hence  $N$  must be non-singular i.e.  $N$  is left non-singular  $\Leftrightarrow E(N)$  is left non-singular  $\Leftrightarrow \varepsilon$  is a faithful topology for  $N \Leftrightarrow \varepsilon$  is  $D$ .

**1.2.4 Note:** A left self injective von Neumann regular near-field space  $N$  is semi simple Nagendram Near-field space if and only if it has finite Nagendram rank.

With the above 1.2.3 and 1.2.4 we have the desired necessary conditions for a Near-field space  $N$  to be a left Ore in a semi simple Nagendram near-field space.

**1.2.5 Note:** Let  $N$  be a left semiprime Nagendram Near-field space then if  $N_N$  has finite Nagendram rank, then  $N$  is also right semiprime Nagendram Near-field space.

**1.2.6 Note:** If  $N$  and  $M$  are Nagendram equivalent Near-field spaces and if  $N$  satisfies the Ascending Chain Condition A.C.C. for left annihilators then  $S$  satisfies the A.C.C. for left annihilators.

**1.2.7 Note:** Let  $N$  and  $M$  are Nagendram equivalent Near-field spaces (i) if  $N$  is a semiprime left Nagendram Near-field space, then so is  $M$ . (ii) If  $N$  is a semiprime left Nagendram Near-field space then  $Q_{cl}(N)$  and  $Q_{cl}(M)$  are Nagendram equivalent Near-field spaces.

**1.2.8 Note:** If  $N$  is a left non-singular Nagendram Near-field space of finite Nagendram rank, then  $N$  satisfies the A.C.C. and D.C.C. on left Annihilators.

## SECTION-2: MAIN RESULTS ON NAGENDRAM NEAR-FIELD SPACE THEOREMS

In this section, we study and derive main results on Nagendram Near-field space theorems.

**2.1 Proposition:** If  $N$  is a left Ore Nagendram Near-field space in a semi simple Nagendram Near-field space, then  $N$  is semiprime Nagendram Near-field space of finite left Nagendram rank that satisfies the A.C.C. on left Annihilators.

**Proof:** by lemma 1.2.2 and Note 1.2.7  $N$  is non-singular and by Note 1.2.8  $N$  satisfies the A.C.C. on left Annihilators. So it will suffice to show that  $N$  is semiprime Nagendram Near-field space. Suppose that  $aNa = 0$  for some  $a \in N$ . We claim that  $n_N(NaN) \leq {}_N N$ . Indeed. For every  $0 \neq x \in N$ , we have  $NaNx \leq n_N(NaN) \cap Nx$ . So if  $n_N(NaN) \cap Nx = 0$ , then  $NaNx = 0$  and  $x \in n_N(NaN) \cap Nx$ , a contradiction. So  $n_N(NaN) \subseteq {}_N N$ . But by lemma 1.2.2,  $\varepsilon = 0$  so there is some  $d \in n_N(NaN) \cap \Delta$ . So  $ad = 0$  and hence  $a = 0$  so  $N$  semiprime Nagendram Near-field space. This completes the proof of the proposition.

**2.2. Note:** A near-field space  $N$  is left Nagendram Near-field space in case it has finite left Nagendram rank and satisfies the A.C.C. on left Annihilators of Nagendram Near-field spaces over a near-field. So proposition 2.1 states that if  $N$  is a left Ore Nagendram Near-field space in a semi-simple Nagendram Near-field space, then  $N$  is a semiprime left Nagendram Near-field space. The icing on the cake is that the converse is true.

**2.3 Lemma:** If  $N$  is semiprime left Nagendram Near-field space then  $N$  is left non-singular.

**Proof:** Let  $Z = Z({}_N N)$  be the left singular ideal of  $N$ . Since  $N$  is semiprime. It will suffice to prove that  $Z$  is nilpotent. For every  $N$ ,  $N$  is semiprime  $\Leftrightarrow N(N) = 0 \Leftrightarrow I^2 = 0$  implies  $I = 0$  for every left ( or right two sided ) ideal  $I$  of  $N \Leftrightarrow aNa = 0$  implies  $a = 0 \Leftrightarrow$  no non zero nilpotent left ( or right two sided ) ideals  $\Leftrightarrow N$  is semiprime. But we do have  $Z \geq Z^2 \geq Z^3 \geq \dots \geq Z^n$ , ....so that  $I_N(Z) \leq I_N(Z^2) \leq I_N(Z^3) \leq \dots$ . Thus, since  $N$  satisfies the A. C. C. (Ascending Chain Condition) on left annihilators.  $I_N(Z^{n+1}) = I_N(Z^n)$  for some natural number  $n$  belongs to set of naturals. We claim that  $I_N(Z^n) = N$ .

If not then the set  $\{ I_N(x) : x \in N \setminus I_N(Z^n) \}$  of left annihilators has a maximal element say  $I_N(x)$ . Let  $b \in Z$ , that  $I_N(b) \leq N$ . But then there is some  $0 \neq sx \in I_N(b)$ , so then  $s \in I_N(xb) \setminus I_N(x)$  then by the maximality of  $I_N(x)$  this means that  $xb \in I_N(Z^n)$  or that  $x \in I_N(bZ^n)$ . Since, this true for every  $b \in Z$  we conclude that  $x \in I_N(Z \cdot Z^n) = I_N(Z^{n+1}) = I_N(Z^n)$ , a contradiction. Thus  $I_N(Z^n) = N$  and  $Z^n = 0$ . This completes the proof of the lemma.

**2.4 Lemma:** If  $N$  is semiprime left Nagendram Near-field space over a Near-field then  $O = \varepsilon$  i.e, if  $N$  is semiprime left Nagendram Near-field space, then a left sub semiprime Nagendram Near-field space  $I$  of  $N$  is essential if and only if  $I$  contains a non-zero divisor.

**Proof:** Is obvious.

**2.5 Theorem:** [Nagendram] A Nagendram Near-field space over a Near-field  $N$  is a left Ore in a semi-simple Nagendram Near-field space iff  $N$  is semiprime left Nagendram Near-field space over a Near-field.

**Proof:** The necessary is [2.1 Proposition] proved. Conversely, if  $N$  is semiprime left Nagendram Near-field space over a Near-field, then  $N$  is left non-singular [2.2 Lemma]. So by known theorem, we have for left non-singular Nagendram Near-field space  $N$ , its maximal Nagendram Near-field space  $Q_{\max}$  say of left quotients is semi-simple if and only if  $N$  has finite left Nagendram rank. Hence  $Q_{\max}$  is semi simple. But, finally, by lemma 2.4  $Q_{c1} = Q_{\max}$  and  $N$  is left Ore Nagendram Near-field space in the semi simple Nagendram Near-field space over a Near-field  $Q_{c1} = Q_{\max}$ . This completes the proof of the theorem.

**2.6 Note:** Now we specialize theis to characterize the Nagendram Near-field spaces that are left ore Nagendram Near-field space in simple artinian near-field spaces of a near-field over a near-ring.

**2.7 Theorem:** [Nagendram] A Nagendram Near-field space over a Near-field  $N$  is a left Ore Nagendram Near-field space in simple artinian near-field space if and only if (IFF)  $N$  is a prime left Nagendram Near-field space over a Near-field.

**Proof:** In either case by Theorem 2.5,  $N$  is a left Ore Nagendram Near-field space over a Near-field in a semi-simple Nagendram Near-field space  $Q = Q_{c1}$ , so it will suffice to prove that  $Q$  is simple if and only if (IFF)  $N$  is prime Nagendram Near-field space over a Near-field.

So suppose that  $Q = Q_{c1}$  is simple Nagendram Near-field space and suppose that  $a, b \in N$  with the property  $aNb = 0$  and  $b \neq 0$ . Then by the simplicity of  $Q$ , we have  $QbQ = Q$ . So there exist  $q_i, q_i^{-1} \in Q$  with  $1 = \sum_{i=1}^n q_i b q_i^{-1}$  there exists  $d \in \Delta$  and  $a_i \in N$  with  $q_i = d^{-1} a_i$  for  $i = 1, 2, 3, \dots, n$ . Thus,  $d = d.1 = \sum_{i=1}^n a_i b q_i^{-1}$  and so  $aNd = \sum_{i=1}^n aNa_i b q_i^{-1} \subseteq aNbQ = 0$ .

But  $d \in \Delta$ , so  $aN = 0$  and  $a = 0$ . Thus  $N$  is prime Nagendram Near-field space.

Conversely, suppose that  $Q = Q_{c1}$  is not simple Nagendram Near-field space. Then by known theorem, there exist non-zero central idempotent  $e, f \in Q$  with  $ef = 0$  then there exist some  $d \in \Delta$  and  $e_0, f_0 \in N$  with  $e = d^{-1} e_0$  and  $f = d^{-1} f_0$ . Then  $e_0 \neq 0, f_0 \neq 0$ , but  $Ne_0 N f_0 = NdeNfd = 0$  so that  $N$  is not prime Nagendram Near-field space. This completes the proof of the theorem.

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## REFERENCES

1. G. L. Booth A note on  $\Gamma$ -near-rings Stud. Sci. Math. Hung. 23 (1988) 471-475.
2. G. L. Booth Jacobson radicals of  $\Gamma$ -near-rings Proceedings of the Hobart Conference, Longman Sci. & Technical (1987) 1-12.
3. G Pilz Near-rings, Amsterdam, North Holland.
4. P. S. Das Fuzzy groups and level subgroups J. Math. Anal. and Appl. 84 (1981) 264-269.
5. V. N. Dixit, R. Kumar and N. Ajal On fuzzy rings Fuzzy Sets and Systems 49 (1992) 205-213.
6. S. M. Hong and Y. B. Jun A note on fuzzy ideals in  $\Gamma$ -rings Bull. Honam Math. Soc. 12 (1995) 39-48.
7. Y. B. Jun and S. Lajos Fuzzy (1; 2)-ideals in semigroups PU. M. A. 8(1) (1997) 67-74.
8. Y. B. Jun and C. Y. Lee Fuzzy  $\square$ -rings Pusan Kyongnam Math. J. 8(2) (1992) 163-170.
9. Y. B. Jun, J. Neggers and H. S. Kim Normal L-fuzzy ideals in semirings Fuzzy Sets and Systems 82 (1996) 383-386.
10. N V Nagendram, T V Pradeep Kumar and Y V Reddy On "Semi Noetherian Regular Matrix  $\delta$ -Near-Rings and their extensions", International Journal of Advances in Algebra (IJAA), Jordan, ISSN 0973 - 6964, Vol.4, No.1, (2011), pp.51-55. Dr N V Nagendram\*/ Some special classes of Nagendram  $\Gamma$ -semi sub near-field spaces of .../ IJMA- 11(8), August-2020. © 2020, IJMA. All Rights Reserved 6
11. NV Nagendram, T V Pradeep Kumar and Y V Reddy "A Note on Bounded Matrices over a Noetherian Regular Delta Near Rings", (BMNR-delta-NR) published in International Journal of Contemporary Mathematics, Vol.2, No.1, June 2011, Copyright@MindReaderPublications, ISSNNo:0973-6298, pp.13-19.

12. N V Nagendram, T V Pradeep Kumar and Y V Reddy "A Note on Boolean Regular Near-Rings and Boolean Regular  $\delta$ -Near Rings", (BR- $\delta$ -NR) published in International Journal of Contemporary Mathematics, IJCM Int. J. of Contemporary Mathematics, Vol. 2, No. 1, June 2011, Copyright @ Mind Reader Publications, ISSN No: 0973-6298, pp. 29 – 34.
13. NV Nagendram, T V Pradeep Kumar and Y V Reddy "on p-Regular  $\delta$ -Near-Rings and their extensions", (PR- $\delta$ -NR) accepted and to be published in int. J. Contemporary Mathematics (IJCM), 0973-6298, vol.1, no.2, pp.81-85, June 2011.
14. N V Nagendram, T V Pradeep Kumar and Y V Reddy "On Strongly Semi -Prime over Noetherian Regular  $\delta$ - Near Rings and their extensions", (SSPNR- $\delta$ -NR) published in International Journal of Contemporary Mathematics, Vol.2, No.1, June 2011, pp.83-90.
15. N V Nagendram, Dr T V Pradeep Kumar and Dr Y V Reddy "On Structure Theory and Planar of Noetherian Regular  $\delta$ -Near-Rings (STPLNR- $\delta$ -NR)", International Journal of Contemporary Mathematics, IJCM, published by IJSMA, pp.79-83, Dec, 2011.
16. N V Nagendram, Dr T V Pradeep Kumar and Dr Y V Reddy "On Matrix's Maps over Planar of Noetherian Regular  $\delta$ -Near-Rings (MMPLNR- $\delta$ -NR)", International Journal of Contemporary Mathematics, IJCM, published by IJSMA, pp.203-211, Dec, 2011.
17. N V Nagendram, Dr T V Pradeep Kumar and Dr Y V Reddy "On IFP Ideals on Noetherian Regular- $\delta$ - Near Rings (IFPINR- $\delta$ -NR)", Int. J. of Contemporary Mathematics, Copyright @ Mind Reader Publications, ISSN No: 0973-6298, Vol. 2, No. 1, pp.53-58, June 2011.
18. N V Nagendram, B Ramesh paper "A Note on Asymptotic value of the Maximal size of a Graph with rainbow connection number  $2*(AVM-GR-CN2*)$ " published in an International Journal of Advances in Algebra (IJAA) Jordan @ Research India Publications, Rohini, New Delhi, ISSN 0973-6964 Volume 5, Number 2 (2012), pp. 103-112.
19. N V Nagendram research paper on "Near Left Almost Near-Fields (N-LA-NF)" communicated to for 2nd international conference by International Journal of Mathematical Sciences and Applications, IJMSA @ mindreader publications, New Delhi on 23-04-2012 also for publication.
20. N V Nagendram, T Radha Rani, Dr T V Pradeep Kumar and Dr Y V Reddy "A Generalized Near Fields and (m, n) Bi-Ideals over Noetherian regular Delta-near rings (GNF-(m, n) BI-NR- $\delta$ -NR)", published in an International Journal of Theoretical Mathematics and Applications (TMA), Greece, Athens, dated 08-04-2012.
21. N V Nagendram, Smt.T.Radha Rani, Dr T V Pradeep Kumar and Dr Y V Reddy "Applications of Linear Programming on optimization of cool freezers (ALP-on-OCF)" Published in International Journal of Pure and Applied Mathematics, IJPAM-2012-17-670 ISSN-1314-0744 Vol-75 No-3(2011).
22. N V Nagendram "A Note on Algebra to spatial objects and Data Models (ASO-DM)" Published in Intl. Journal American Journal of Mathematics and Mathematical Sciences, AJMMS, USA, Copyright @ Mind Reader Publications, Rohini, New Delhi, ISSN. 2250-3102, Vol.1, No.2 (Dec. 2012), pp. 233 – 247.
23. N V Nagendram, Ch Padma, Dr T V Pradeep Kumar and Dr Y V Reddy "A Note on Pi-Regularity and Pi-SUnitality over Noetherian Regular Delta Near Rings (PI-R-PI-S-U-NR-Delta-NR)" Published in International Electronic Journal of Pure and Applied Mathematics, IeJPAM-2012-17-669 ISSN-1314-0744 Vol-75 No4(2011).
24. N V Nagendram, Ch Padma, Dr T V Pradeep Kumar and Dr Y V Reddy "Ideal Comparability over Noetherian Regular Delta Near Rings (IC-NR-Delta-NR)" Published in International Journal of Advances in Algebra (IJAA, Jordan), ISSN 0973-6964 Vol:5, NO:1(2012), pp.43-53 @ Research India publications, Rohini, New Delhi.
25. N. V. Nagendram, S. VenuMadava Sarma and T. V. Pradeep Kumar, "A Note On Sufficient Condition Of Hamiltonian Path To Complete Graphs (SC-HPCG)", IJMA-2(11), 2011, pp.1-6.
26. N V Nagendram, Dr T V Pradeep Kumar and Dr Y V Reddy "On Noetherian Regular Delta Near Rings and their Extensions (NR- $\delta$ -NR)", IJCMS, Bulgaria, IJCMS -5-8-2011, Vol.6, 2011, No.6, 255-262.
27. N V Nagendram, Dr T V Pradeep Kumar and Dr Y V Reddy "On Semi Noetherian Regular Matrix Delta Near Rings and their Extensions (SNRM- $\delta$ -NR)", Jordan, @Research India Pubns, Advances in Algebra ISSN 0973-6964 Volume 4, Number 1 (2011), pp.51-55 © Research India Publications pp.51-55
28. N V Nagendram, Dr T V Pradeep Kumar and Dr Y V Reddy "On Boolean Noetherian Regular Delta Near Ring (BNR- $\delta$ -NR)", International Journal of Contemporary Mathematics, IJCM Int. J. of Contemporary Mathematics, Vol. 2, No. 1-2, Jan-Dec 2011, Mind Reader Publications, ISSN No: 0973-6298, pp. 23-27.
29. N V Nagendram, Dr T V Pradeep Kumar and Dr Y V Reddy "On Bounded Matrix over a Noetherian Regular Delta Near Rings (BMNR- $\delta$ -NR)", Int. J. of Contemporary Mathematics, Vol. 2, No. 1-2, Jan-Dec 2011, Copyright @ Mind Reader Publications, ISSN No: 0973-6298, pp.11-16
30. N V Nagendram, Dr T V Pradeep Kumar and Dr Y V Reddy "On Strongly Semi Prime over Noetherian Regular Delta Near Rings and their Extensions (SSPNR- $\delta$ -NR)", Int. J. of Contemporary Mathematics, Vol. 2, No. 1, Jan-Dec 2011, Copyright @ Mind Reader Publications, ISSN No: 0973-6298, pp.69-74. Dr N V Nagendram\*/ Some special classes of Nagendram  $\Gamma$ -semi sub near-field spaces of .../ IJMA-11(8), August-2020. © 2020, IJMA. All Rights Reserved 7
31. N V Nagendram, Dr T V Pradeep Kumar and Dr Y V Reddy "On IFP Ideals on Noetherian Regular Delta Near Rings (IFPINR- $\delta$ -NR)", Int. J. of Contemporary Mathematics, Vol. 2, No. 1-2, Jan-Dec 2011, Copyright @ Mind Reader Publications, ISSN No: 0973-6298, pp.43-46.

32. N V Nagendram, Dr T V Pradeep Kumar and Dr Y V Reddy "On Structure Theory and Planar of Noetherian Regular delta-Near-Rings (STPLNR-delta-NR)", International Journal of Contemporary Mathematics, IJCM, accepted for 1st international conference conducted by IJSMA, New Delhi December 18, 2011, pp:79-83, Copyright @ Mind Reader Publications and to be published in the month of Jan 2011.
33. N V Nagendram, Dr T V Pradeep Kumar and Dr Y V Reddy "On Matrix's Maps over Planar of Noetherian Regular delta-Near-Rings (MMPLNR-delta-NR)", International Journal of Contemporary Mathematics, IJCM, accepted for 1st international conference conducted by IJSMA, New Delhi December 18, 2011, pp:203- 211, Copyright @ Mind Reader Publications and to be published in the month of Jan 2011.
34. N V Nagendram, Dr T V Pradeep Kumar and Dr Y V Reddy "Some Fundamental Results on P- Regular deltaNear-Rings and their extensions (PNR-delta-NR)", International Journal of Contemporary Mathematics, IJCM, Jan-December '2011, Copyright@MindReader Publications, ISSN:0973-6298, vol.2, No.1-2, PP.81-85.
35. N V Nagendram, Dr T V Pradeep Kumar and Dr Y V Reddy "A Generalized ideal based-zero divisor graphs of Noetherian regular Delta-near rings (GIBDNR- d-NR)" , International Journal of Theoretical Mathematics and Applications (TMA) accepted and published by TMA, Greece, Athens, ISSN:1792- 9687 (print), vol.1, no.1, 2011, 59-71, 1792-9709 (online), International Scientific Press, 2011.
36. N V Nagendram, Dr T V Pradeep Kumar and Dr Y V Reddy "Inversive Localization of Noetherian regular Delta-near rings (ILNR- Delta-NR)" , International Journal of Pure And Applied Mathematics published by IJPAM-2012-17-668, ISSN.1314-0744 vol-75 No-3, SOFIA, Bulgaria.
37. N V Nagendram, N Chandra Sekhara Rao "Optical Near field Mapping of Plasmonic Nano Prisms over Noetherian Regular Delta Near Fields (ONFMPN-NR-Delta-NR)" accepted for 2nd international Conference by International Journal of Mathematical Sciences and Applications, IJMSA @ mind reader publications, New Delhi going to conduct on 15 – 16 th December 2012 also for publication.
38. N V Nagendram, K V S K Murthy (Yoga), "A Note on Present Trends on Yoga Apart From Medicine Usage and Its Applications (PTYAFMUIA)" Published by the International Association of Journal of Yoga Therapy, IAYT 18 th August, 2012.
39. N V Nagendram, B Ramesh, Ch Padma, T Radha Rani and S V M Sarma research article "A Note on Finite Pseudo Artinian Regular Delta Near Fields (FP AR-Delta-NF)" communicated to International Journal of Advances in Algebra, IJAA, Jordan on 22 nd August 2012.
40. N V Nagendram "Amenability for dual concrete complete near-field spaces over a regular delta near-rings (ADC-NFS-R- $\delta$ -NR)" accepted for 3rd international Conference by International Journal of Mathematical Sciences and Applications, IJMSA @ mind reader publications, New Delhi going to conduct on 15 – 16 th December 2014 also for publication.
41. N V Nagendram "Characterization of near-field spaces over Baer-ideals" accepted for 4th international Conference by International Journal Conference of Mathematical Sciences and Applications, IJCMSA @ mind reader publications, New Delhi going to conduct on 19 – 20 th December 2015 at Asian Institute of Technology AIT, Klaung Lange 12120, Bangkok, Thailand.
42. N V Nagendram, S V M Sarma Dr T V Pradeep Kumar "A note on sufficient condition of Hamiltonian path to Complete Graphs" published in International Journal of Mathematical archive IJMA, ISSN 2229-5046, Vol.2, No.2, Pg. 2113 – 2118, 2011.
43. N V Nagendram, S V M Sarma, Dr T V Pradeep Kumar "A note on Relations between Barnette and Sparse Graphs" published in an International Journal of Mathematical Archive (IJMA), An International Peer Review Journal for Mathematical, Science & Computing Professionals, 2(12), 2011, pg no.2538-2542, ISSN 2229 – 5046.
44. N V Nagendram "On Semi Modules over Artinian Regular Delta Near Rings (S Modules-AR-Delta-NR)" Accepted and published in an International Journal of Mathematical Archive (IJMA)", An International Peer Review Journal for Mathematical, Science & Computing Professionals ISSN 2229-5046, IJMA-3-474, 2012.
45. N V Nagendram "A note on Generating Near-field efficiently Theorem from Algebraic K - Theory" published by International Journal of Mathematical Archive, IJMA, ISSN. 2229-5046, Vol.3, No.10, Pg. 1 – 8, 2012.
46. N V Nagendram and B Ramesh on "Polynomials over Euclidean Domain in Noetherian Regular Delta Near Ring Some Problems related to Near Fields of Mappings (PED-NR-Delta-NR & SPR-NF)" Accepted and published in an International Journal of Mathematical Archive (IJMA), An International Peer Review Journal for Mathematical, Science & Computing Professionals ISSN 2229-5046, vol.3, no.8, pp no. 2998-3002, 2012.
47. N V Nagendram "Semi Simple near-fields Generating efficiently Theorem from Algebraic K - Theory" published by International Journal of Mathematical Archive, IJMA, ISSN. 2229-5046, Vol.3, No.12, Pg. 1 – 7, 2012.
48. N V Nagendram "-----" published by International Journal of Mathematical Archive, IJMA, ISSN. 2229-5046, Vol.3, No.10, Pg. 3612 – 3619, 2012.
49. N V Nagendram, E Sudeeshna Susila, "Applications of linear infinite dimensional system in a Hilbert space and its characterizations in engg. Maths (AL FD S HS & EM)", IJMA, ISSN.2229-5046, Vol.4, No.7, Pg.1 – 11 (19 – 29), 2013. Dr N V Nagendram\*/ Some special classes of Nagendram  $\Gamma$ -semi sub near-field spaces of .../ IJMA- 11(8), August-2020. © 2020, IJMA. All Rights Reserved 8
50. N V Nagendram, Dr T V Pradeep Kumar, "Compactness in fuzzy near-field spaces (CN-F-NS)", IJMA, ISSN. 2229 – 5046, Vol.4, No.10, Pg. 1 – 12, 2013.

51. N V Nagendram, Dr T V Pradeep Kumar and Dr Y Venkateswara Reddy, "Fuzzy Bi- $\Gamma$  ideals in  $\Gamma$  semi near – field spaces (F Bi-Gamma I G)" published by International Journal of Mathematical Archive, IJMA, ISSN. 2229-5046, Vol.4, No.11, Pg. 1 – 11, 2013.
  52. N V Nagendram," EIFP Near-fields extension of near-rings and regular delta near-rings (EIFP-NF-E-NR)" published by International Journal of Mathematical Archive, IJMA, ISSN. 2229 - 5046, Vol.4, No.8, Pg. 1 –11, 2013.
  53. N V Nagendram, E Sudeeshna Susila, "Generalization of  $(\in, \in Vqk)$  fuzzy sub near-fields and ideals of nearfields(GF-NF-IO-NF)", IJMA, ISSN.2229-5046, Vol.4, No.7,Pg. 1 – 11, 2013.
  54. N V Nagendram, Dr T V Pradeep Kumar," A note on Levitzki radical of near-fields(LR-NF)" ,Published by International Journal of Mathematical Archive, IJMA,ISSN. 2229-5046, Vol.4, No.4, Pg.288 – 295, 2013.
  55. N V Nagendram, "Amalgamated duplications of some special near-fields (AD-SP-N-F)", Published by International Journal of Mathematical Archive, IJMA,ISSN. 2229-5046, Vol.4, No.2, Pg.1 – 7, 2013.
  56. N V Nagendram," Infinite sub near-fields of infinite near-fields and near-left almost near-fields (IS-NF-INFNL-A-NF)", Published by International Journal of Mathematical Archive, IJMA,ISSN. 2229-5046, Vol.4, No.2, Pg. 90 – 99, 2013.
  57. N V Nagendram "Tensor product of a near-field space and sub near-field space over a near-field" published by International Journal of Mathematical Archive, IJMA, ISSN. 2229-5046, Vol.8, No.6, Pg. 8 – 14, 2017.
  58. N V Nagendram, E Sudeeshna Susila, Dr T V Pradeep Kumar "Some problems and applications of ordinary differential equations to Hilbert Spaces in Engg mathematics (SP-O-DE-HS-EM)", IJMA, ISSN.2229-5046, Vol.4, No.4,Pg. 118 – 125, 2013.
  59. N V Nagendram, Dr T V Pradeep Kumar and D Venkateswarlu, "Completeness of near-field spaces over nearfields (VNFS-O-NF)" published by International Journal of Mathematical Archive, IJMA, ISSN. 2229-5046, Vol.5, No.2, Pg. 65 – 74, 2014
  60. Dr N V Nagendram "A note on Divided near-field spaces and  $\phi$ -pseudo – valuation near-field spaces over regular  $\delta$ -near-rings (DNF- $\phi$ -PVNFS-O- $\delta$ -NR)" published by International Journal of Mathematical Archive, IJMA, ISSN. 2229-5046, Vol.6, No.4, Pg. 31 – 38, 2015.
  61. Dr. N V Nagendram "A Note on B1-Near-fields over R-delta-NR(B1-NFS-R- $\delta$ -NR)", Published by International Journal of Mathematical Archive, IJMA, ISSN. 2229-5046, Vol.6, No.8, Pg. 144 – 151, 2015.
  62. Dr. N V Nagendram " A Note on TL-ideal of Near-fields over R-delta-NR(TL-I-NFS-R- $\delta$ -NR)", Published by International Journal of Mathematical Archive, IJMA, ISSN. 2229-5046, Vol.6, No.8, Pg. 51 – 65, 2015.
  63. Dr. N V Nagendram "A Note on structure of periodic Near-fields and near-field spaces (ANS-P-NF-NFS)", Published by International Journal of Mathematical Archive, IJMA, ISSN. 2229-5046, Vol.7, No.4, Pg. 1 – 7, 2016.
  64. Dr. N V Nagendram "Certain Near-field spaces are Near-fields(C-NFS-NF)", Published by International Journal of Mathematical Archive, IJMA, ISSN. 2229-5046, Vol.7, No.4, Pg. 1 – 7, 2016.
  65. Dr. N V Nagendram "Sum of Annihilators Near-field spaces over Near-rings is Annihilator Near-field space (SA-NFS-O-A-NFS)", Published by International Journal of Mathematical Archive, IJMA, ISSN. 2229-5046, Vol.7, No.1, Pg. 125 – 136, 2016.
  66. Dr. N V Nagendram "A note on commutativity of periodic near-field spaces", Published by IJMA, ISSN. 2229 - 5046, Vol.7, No. 6, Pg. 27 – 33, 2016.
  67. Dr N V Nagendram "Densely Co-Hopfian sub near-field spaces over a near-field, IMA, ISSN No.2229-5046,2016, Vol.7, No.10, Pg 1-12.
  68. Dr N V Nagendram, "Closed (or open) sub near-field spaces of commutative near-field space over a nearfield", 2016, Vol.7, No, 9, ISSN NO.2229 – 5046, Pg No.57 – 72.
  69. Dr N V Nagendram, "Homomorphism of near-field spaces over a near-field "IJMA Jan 2017, Vol.8, No, 2, ISSN NO.2229 – 5046, Pg No. 141 – 146.
  70. Dr N V Nagendram, "Sigma – toe derivations of near-field spaces over a near-field "IJMA Jan 2017, Vol.8, No, 4, ISSN NO. 2229 – 5046, Pg No. 1 – 8.
  71. Dr N V Nagendram, "On the hyper center of near-field spaces over a near-field "IJMA Feb 2017, Vol.8, No, 2, ISSN NO.2229 – 5046, Pg No. 113 – 119.
  72. Dr N V Nagendram, "Commutative Theorem on near-field space and sub near-field space over a near-field" IJMA July, 2017, Vol.8, No,7, ISSN NO.2229 – 5046, Pg No. 1 – 7.
  73. Dr N V Nagendram, "Project on near-field spaces with sub near-field space over a near-field " , IJMA Oct, 2017, Vol.8, No,11, ISSN NO.2229 – 5046, Pg No. 7 – 15.
  74. Dr N V Nagendram, "Abstract near-field spaces with sub near-field space over a near-field of Algebraic in Statistics", IJMA Nov, 2017, Vol.8, No, 12, ISSN NO.2229 – 5046, Pg No. 13 – 22.
  75. Smt. T Madhavi Latha, Dr T V Pradeep Kumar and Dr N V Nagendram, "Commutative Prime  $\Gamma$ -near-field spaces with permuting Tri-derivations over near-field", IJMA Dec, 2017, Vol.8, No,12, ISSN NO.2229 – 5046, Pg No. 1 – 9.
  76. Smt. T Madhavi Latha, Dr T V Pradeep Kumar and Dr N V Nagendram, "Fuzzy sub near-field spaces in  $\Gamma$ near-field space over a near-field" ,IJMA Nov, 2017, Vol.8, No, 12, ISSN NO.2229 – 5046, Pg No.188 – 196.
- Dr N V Nagendram\*/ Some special classes of Nagendram  $\Gamma$ -semi sub near-field spaces of .../ IJMA- 11(8), August-2020. © 2020, IJMA. All Rights Reserved 9.

77. Smt. T Madhavi Latha, Dr T V Pradeep Kumar and Dr N V Nagendram, "Gamma Semi Sub near-field spaces in gamma near-field space over a near-field PART I", IJMA Jan, 2018, Vol. 9, No, 2, ISSN NO.2229 – 5046, Pg No.135 – 145.
78. Smt. T Madhavi Latha, Dr T V Pradeep Kumar and Dr N V Nagendram, "Gamma Semi Sub near-field spaces in gamma near-field space over a near-field PART II", IJMA 14 Feb, 2018, Vol. 9, No, 3, ISSN NO.2229 – 5046, Pg No.6 – 12.
79. Smt. T Madhavi Latha, Dr T V Pradeep Kumar and Dr N V Nagendram, "Gamma Semi Sub near-field spaces in gamma near-field space over a near-field PART III", IJMA 26 Feb, 2018, Vol. 9, No, 3, ISSN NO.2229 – 5046, Pg No.86 – 95.
80. Smt. T Madhavi Latha, Dr T V Pradeep Kumar and Dr N V Nagendram, "Gamma Semi Sub near-field spaces in gamma near-field space over a near-field PART IV", IJMA 09 Mar, 2018, Vol. 9, No, 4, ISSN NO.2229 – 5046, Pg No.1 – 14.
81. Dr N V Nagendram, "Nagendram Gamma-Semi Sub near-field spaces in gamma near-field space over a nearfield", IJMA 29 April, 2018, Vol. 9, No, 6, ISSN NO.2229 – 5046, Pg No.58 – 66.
82. Dr N V Nagendram, "Topological Nagendram Gamma-Semi Sub near-field spaces in gamma near-field space over a near-field", IJMA 2005 2018, Vol. 9, No, 7, ISSN NO.2229 – 5046, Pg No.7 – 18.
83. Dr N V Nagendram, "Deformation Retracts of classical Nagendram Gamma-semi sub near-field spaces of a Gamma-near-field space over near-field" 22 09 2018, Vol. 9, No, 11, ISSN NO.2229 – 5046, Pg No.64 – 69.
84. Dr N V Nagendram, "Representation of Nagendram Gamma semi sub near-field spaces of a Gamma-nearfield space over near-field", 1010 2018, IJMA Aug, 2019, Vol. 9, No, 11, ISSN NO.2229 – 5046, Pg No. 46- 54.
85. Dr N V Nagendram, "Almost prime ideal in Nagendram Gamma semi sub near-field spaces of a Gamma-nearfield space over near-field", 26 03 2019, IJMA Mar, 2019, Vol. 10, No, 5, ISSN NO.2229 – 5046, Pg No.1 – 7.
86. Dr N V Nagendram, "Characters of Nagendram Gamma semi sub near-field spaces of a Gamma-near-field space over near-field", 21 07 2019, IJMA Sept, 2019, Vol. 10, No, 9, ISSN NO.2229 – 5046, Pg No.1- 7.
87. Dr N V Nagendram, "Part – I characters of Nagendram Gamma semi sub near-field spaces of a Gamma-nearfield space over near-field", 23 07 2019, IJMA Feb, 2020, Vol. 10, No, 8, ISSN NO.2229 – 5046, Pg No. 11-17.
88. Dr N V Nagendram, "Part – II characters of Nagendram Gamma semi sub near-field spaces of a Gamma-nearfield space over near-field", 3110 2019, IJMA Feb, 2020, Vol. 11, No, 3, ISSN NO.2229 – 5046, Pg No.1- 6.
89. Dr N V Nagendram "Part III Characters of Nagendram Gamma semi sub near-field spaces of a Gamma-near-field space over near-field" April 2019, "IJMA, Vol. xx, No, xx, ISSN NO.2229 – 5046, Pg No .xx – xx.
90. K H Prasad1, Dr T V Pradeep Kumar2 , Dr N V Nagendram3 , "Kalangi non-associative Gamma semi sub nearfield spaces of a Gamma-near-field space over near-field", 22 02 2020, IJMA Feb, 2020, Vol. 11, No, 4, ISSN NO. 2229 – 5046, Pg No.7- 9.
91. K H Prasad1 ,Dr T V Pradeep Kumar2 , Dr N V Nagendram3 , "Part I Kalangi non-associative Gamma semi sub near-field spaces of a Gamma-near-field space over near-field", 28 02 2020, IJMA Feb, 2020, Vol. 11, No, 4, ISSN NO. 2229 – 5046, Pg No.42- 45.
92. K H Prasad1, Dr T V Pradeep Kumar2 , Dr N V Nagendram3 , "Part II Applications of fuzzy Kalangi nonassociative Gamma semi sub near-field spaces of a Gamma-near-field space over near-field", 03 05 2020, IJMA May, 2020, Vol. 11, No, 6, ISSN NO.2229 – 5046, Pg No. 7- 13.
93. K H Prasad1, Dr T V Pradeep Kumar2 , Dr N V Nagendram3 , "Part III Applications of fuzzy Kalangi nonassociative Gamma semi sub near-field spaces of a Gamma-near-field space over near-field", 03 05 2020, IJMA May, 2020, Vol. 11, No, 6, ISSN NO.2229 – 5046, Pg No.28- 32.
94. Dr N V Nagendram, "Some Special Classes Of Nagendram  $\Gamma$ -Semi Sub Near-Field Spaces of a  $\Gamma$ -Near-Field Space Over Near-Field ", 25 07 2020, IJMA Aug, 2020, Vol. 11, No, 8, ISSN NO.2229 – 5046, Pg No.01- 09.

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